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An Analytical Conserved Adjustment Scheme for Stabilization of Hydrographic Profiles

Peter C. Chu and C.W. Fan
Naval Postgraduate School
Monterey, CA 93943
pcchu@nps.edu; http://faculty.nps.edu/pcchu

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Problems

- (1) False static instability in (T, S) climatological data

- (2) False static instability in (T, S) data assimilation

Requirements for Stabilization of (T, S) Casts

- (1) Minimal Adjustment
- (2) Heat and Salt Conservation
- (3) Well-Posed (Easy to Get Results)

Minimal Adjustment Method (Jackett and McDougal,1995) JM Method

$$\mathbf{x} = \begin{pmatrix} \mathbf{S} \\ \boldsymbol{\Theta} \end{pmatrix}$$

$$\text{minimize } \|\Delta \mathbf{x}\|^2 \text{ subject to } \mathbf{A}(\mathbf{x} + \Delta \mathbf{x}) \geqslant \mathbf{n}^2,$$

S–θ curve

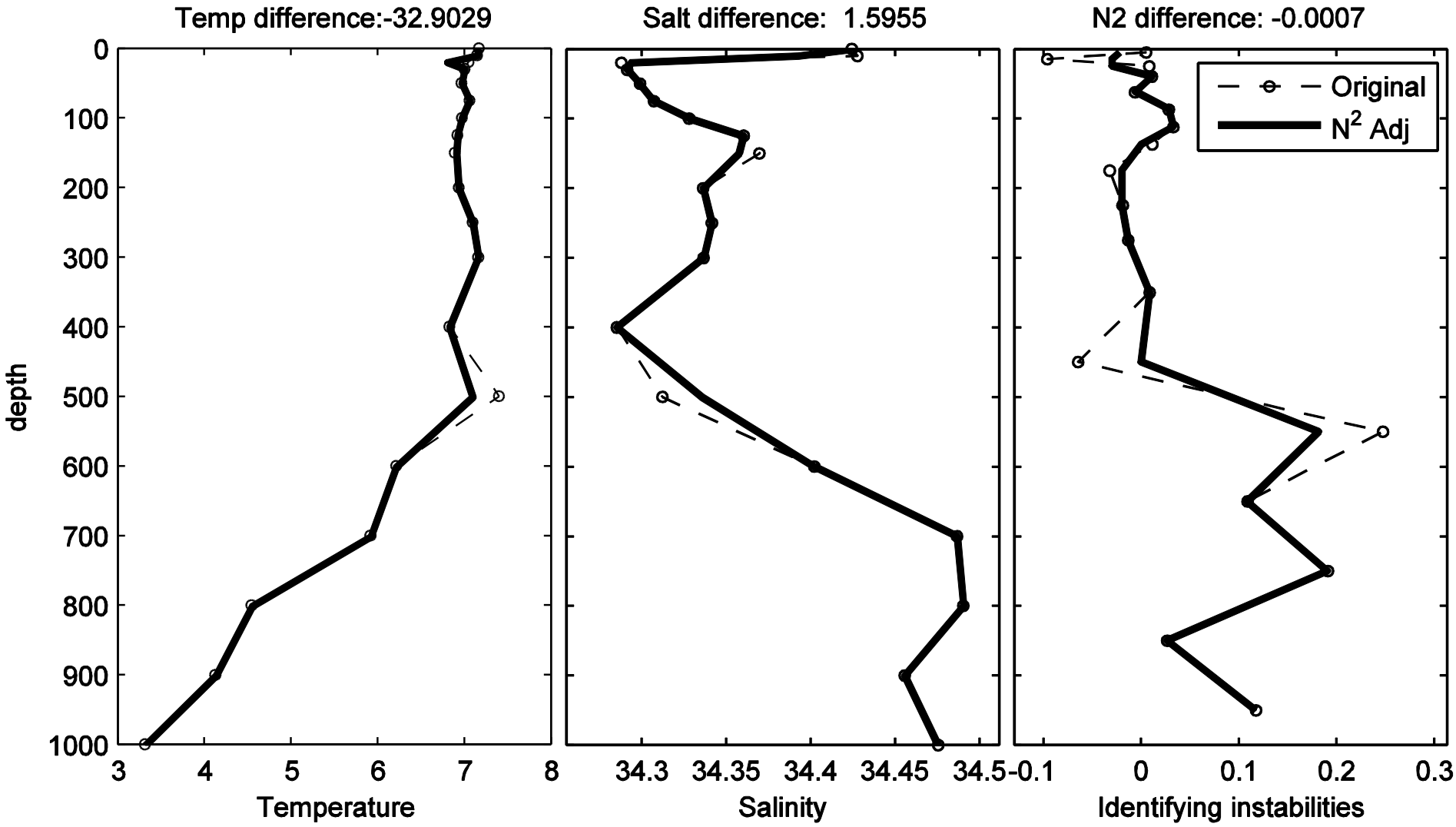
Elements of Matrix **A**

$$
\begin{aligned}
a_{k,k} &= -\beta(S_k^*, \theta_k^*, p_k^*)(p_k - p_{k+1})^{-1} \\
a_{k,k+1} &= -a_{k,k} \\
a_{k,n+k} &= \alpha(S_k^*, \theta_k^*, p_k^*)(p_k - p_{k+1})^{-1} \\
a_{k,n+k+1} &= -a_{k,n+k} \\
a_{k,j} &= 0, \quad j \notin \{k, k+1, n+k, n+k+1\}
\end{aligned}
\tag{7}
$$

for $k = 1, 2, \cdots, n-1$, and the values marked by the asterisk are the midbottle values obtained by linearly interpolating S and θ at $p_k^* = 0.5(p_k + p_{k+1})$.

World Ocean Atlas 2005 (Locarnini et al., 2006, ed: Levitus)

- Stabilization of (T, S) casts using the JM method



Original (dashed) and adjusted (solid) profiles temperature (T_k), salinity (S_k), and static stability (E_k) at the grid box 171.5°E, 53.5°E using the JM method (Locarnini et al. 2006).

Grid-box 171.5°E, 53.5°S WOA98 profiles before stabilization (from Locarnini et al. 2006, Table B1). Here the symbol '*' in the last column indicates the static instability.

k	Depth (m)	T (°C)	S (ppt)	$\rho(S_{k+1}, T_{k+1}, z_k)$ (kg m^{-3})	$\rho(S_k, T_k, z_k)$ (kg m^{-3})	E_k (kg m^{-3})
1	0	7.1667	34.4243	26.9476	26.9423	0.0054
2	10	7.1489	34.4278	26.8982	26.9939	-0.0957*
3	20	7.0465	34.2880	26.9529	26.9443	0.0085
4	30	7.0050	34.2914	27.0104	26.9990	0.0114
5	50	6.9686	34.2991	27.0967	27.1028	-0.0061*
6	75	7.0604	34.3073	27.2406	27.2120	0.0286
7	100	6.9753	34.3280	27.3892	27.3560	0.0332
8	125	6.9218	34.3604	27.5164	27.5046	0.0117
9	150	6.8919	34.3697	27.6000	27.6316	-0.0316*
10	200	6.9363	34.3364	27.8123	27.8302	-0.0179*
11	250	7.0962	34.3415	28.0295	28.0421	-0.0126*
12	300	7.1622	34.3367	28.2684	28.2593	0.0092
13	400	6.8275	34.2852	28.6664	28.7281	-0.0618*
14	500	7.4001	34.3123	29.3699	29.1238	0.2461
15	600	6.2133	34.4022	29.9386	29.8292	0.1094
16	700	5.9186	34.4868	30.5869	30.3978	0.1891
17	800	4.5426	34.4904	31.0754	31.0488	0.0266
18	900	4.1263	34.4558	31.6539	31.5377	0.1162
19	1000	3.3112	34.4755		32.1176	

Grid-box 171.5° E, 53.5° S WOA98 profiles after stabilization using the JM method (from Locarnini et al. 2006, Table B2).

k	Depth (m)	T (°C)	S (ppt)	$\rho(S_{k+1}, T_{k+1}, z_k)$ (kg m^{-3})	$\rho(S_k, T_k, z_k)$ (kg m^{-3})	E_k (kg m^{-3})
1	0	7.1667	34.3096	26.8521	26.8519	0.0002
2	10	7.1489	34.3063	26.8982	26.8982	0.0000
3	20	7.0465	34.2880	26.9529	26.9443	0.0085
4	30	7.0050	34.2914	27.0042	26.9990	0.0051
5	50	7.0132	34.2991	27.0967	27.0967	0.0000
6	75	7.0604	34.3073	27.2361	27.2120	0.0240
7	100	6.9796	34.3228	27.3513	27.3513	0.0000
8	125	6.9897	34.3243	27.4667	27.4667	0.0000
9	150	7.0242	34.3301	27.5820	27.5820	0.0000
10	200	7.0628	34.3364	27.8123	27.8123	0.0000
11	250	7.0962	34.3415	28.0422	28.0421	0.0000
12	300	7.0748	34.3367	28.2719	28.2719	0.0001
13	400	6.8275	34.2894	28.7314	28.7314	0.0000
14	500	6.9604	34.3123	29.3699	29.1899	0.1799
15	600	6.2133	34.4022	29.9386	29.8292	0.1094
16	700	5.9186	34.4868	30.5869	30.3978	0.1891
17	800	4.5426	34.4904	31.0754	31.0488	0.0266
18	900	4.1263	34.4558	31.6539	31.5377	0.1162
19	1000	3.3112	34.4755		32.1176	

Relative root mean adjustment (RRMA)

$$\mathrm{RRMA} =$$

$$\frac{\sqrt{\frac{1}{K}\sum_{k=1}^{K}(\Delta T_k)^2}}{\max(T_k)-\min(T_k)} + \frac{\sqrt{\frac{1}{K}\sum_{k=1}^{K}(\Delta S_k)^2}}{\max(S_k)-\min(S_k)}$$

$$= 0.0712.$$

Weakness of the JM Method → Heat and Salt not Conserved

$$\Delta Q = A\rho_0 c_p \int_{-H}^{0} \Delta T dz$$

$$\Delta(\text{Salt}) = A \int_{-H}^{0} \Delta S dz$$

1° X 1° Area → $A = (\frac{\pi}{180} R)^2 \cos\varphi$

Heat and Salt Change for the (1° X 1°) grid cell

$$\Delta Q = -7.0411 \times 10^{17}\,\mathrm{J}$$

$$\Delta(\mathrm{salt}) \simeq -0.5443 \times 10^{10}\,\mathrm{kg}$$

An Analytical Conserved Adjustment Scheme

Static stability (E)
Lynn and Reid (1968)

- Discrete samples (T_k, S_k) at depth z_k, k = 1, 2, …, K (k increasing downward)

$$E_k = \rho(S_{k+1}, T_{k+1}, z_k) - \rho(S_k, T_k, z_k),$$

$$E_k \geq E_{\min}, \quad k = 1, 2, \ldots, K$$

$E_{\min}$ is the reference value for the minimum static stability

Stabilization

- (a) stability increasing at unstable levels to
- $$E^*_{k_l} = E_{\min} \quad \rightarrow \quad \Delta E_{k_l} = E_{\min} - E_{k_l}$$
- (b) stability decreasing at stable levels

$$E^*_{k_l \pm n} = \begin{cases} E_{k_l \pm n} - \Delta E_{k_l} / 2^{m+1} & \text{if } E_{k_l \pm n} - \Delta E_{k_l} / 2^{m+1} \geq E_{\min} \\ E_{\min} & \text{if } E_{k_l \pm n} - \Delta E_{k_l} / 2^{m+1} < E_{\min} \end{cases}$$

- (c) normalization for conservation of stability for the cast.

$$I = \sum_{k=1}^{K} E_k, \quad I^* = \sum_{k=1}^{K} E^*_k \qquad E^{**}_k = \frac{I}{I^*} E^*_k$$

2*K* Basic Algebraic Equations for Adjustment

$$\rho(S_{k+1}+\Delta S_{k+1}, T_{k+1}+\Delta T_{k+1}, z_k)-\rho(S_k+\Delta S_k, T_k+\Delta T_k, z_k)=E_k^{**},$$
$$k=1,\ 2,\ \ldots,\ K\text{-}1.$$

Heat Conservation → $$\sum_{k=1}^{K-1}\frac{(\Delta T_k+\Delta T_{k+1})}{2}(z_k-z_{k+1})=0$$

Salt Conservation →

Assigned (T, S) Adjustment Ratio y_k → $$\Delta T_k+y_k\Delta S_k=0$$

k = 1, 2, … *K*-1

$$\mathbf{P} \equiv \begin{bmatrix} p_1 \\ p_2 \\ p_3 \\ p_4 \\ \vdots \\ \vdots \\ \vdots \\ p_{M-1} \\ p_M \end{bmatrix} = \begin{bmatrix} \Delta T_1 \\ \Delta S_1 \\ \Delta T_2 \\ \Delta S_2 \\ \vdots \\ \vdots \\ \vdots \\ \Delta T_K \\ \Delta S_K \end{bmatrix}, \qquad M = 2K.$$

2K Basic Algebraic Equations

$$\mathbf{F}(\mathbf{P}) = \mathbf{0} \qquad (1)$$

F has the dimension of 2*K*

Combination of (*K* -1) Nonlinear

and (*K*+1) Linear Equations

Newton Method to Solve (1)

$$\mathbf{P}^{(j+1)} = \mathbf{P}^{(j)} - \mathbf{J}_F^{-1}(\mathbf{P}^{(j)})\mathbf{F}(\mathbf{P}^{(j)})$$

$$j = 0,\ 1,\ 2,...$$

$$\mathbf{P}^{(j+1)} = \mathbf{P}^{(j)} + \mathbf{d}^{(j)}$$

$$\mathbf{J}_F(\mathbf{P}^{(j)}) \bullet \mathbf{d}^{(j)} = \mathbf{b}^{(j)}$$

$$\mathbf{b}^{(j)} \equiv -\mathbf{F}(\mathbf{P}^{(j)})$$

$$\mathbf{J}_F(\mathbf{P}^{(j)}) = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1M} \\ a_{21} & a_{22} & \cdots & a_{2M} \\ \cdots & \cdots & \cdots & \cdots \\ a_{M1} & a_{M2} & \cdots & a_{MM} \end{bmatrix}$$

$$\mathbf{J}_F(\mathbf{P}^{(j)}) = \begin{bmatrix} * & 0 & * & 0 & * & 0 & \dots & \dots & * & 0 \\ 0 & * & 0 & * & 0 & * & \dots & \dots & 0 & * \\ * & * & 0 & 0 & 0 & 0 & \dots & \dots & 0 & 0 \\ * & * & * & * & 0 & 0 & \dots & \dots & 0 & 0 \\ 0 & 0 & * & * & 0 & 0 & \dots & \dots & 0 & 0 \\ 0 & 0 & * & * & * & * & \dots & \dots & 0 & 0 \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & 0 & 0 & \dots & \dots & * & * & 0 & 0 \\ 0 & 0 & 0 & 0 & \dots & \dots & * & * & * & * \end{bmatrix}$$

$$a_{11} = \frac{\Delta z_1}{2}, a_{13} = \frac{\Delta z_1 + \Delta z_2}{2}, \ldots, a_{1,M-3} = \frac{\Delta z_{N-2} + \Delta z_{N-1}}{2}, a_{1,M-1} = \frac{\Delta z_{N-1}}{2},$$

$$a_{12} = a_{14} = a_{16} = \ldots\ldots = a_{1M} = 0,$$

$$a_{22} = \frac{\Delta z_1}{2}, a_{24} = \frac{\Delta z_1 + \Delta z_2}{2}, \ldots, a_{2,M-2} = \frac{\Delta z_{N-2} + \Delta z_{N-1}}{2}, a_{2M} = \frac{\Delta z_{N-1}}{2}$$

$$a_{21} = a_{23} = a_{25} = \ldots = a_{2,M-1} = 0,$$

$$a_{31} = 1,\ a_{32} = \gamma_1,\ \ a_{33} = a_{34} = a_{35} = \ldots = a_{3M} = 0$$

$$a_{41} = \frac{\partial \rho\left(S_1 + \Delta S_1^{(j)}, T_1 + T_1^{(j)}, z_2\right)}{\partial T}$$

$$= -\rho\left(S_1 + \Delta S_1^{(j)}, T_1 + \Delta T_1^{(j)}, z_2\right)\alpha\left(S_1 + \Delta S_1^{(j)}, T_1 + \Delta T_1^{(j)}, z_2\right),$$

$$a_{42} = \frac{\partial \rho\left(S_1 + \Delta S_1^{(j)}, T_1 + \Delta T_1^{(j)}, z_2\right)}{\partial S}$$

$$= \rho\left(S_1 + \Delta S_1^{(j)}, T_1 + \Delta T_1^{(j)}, z_2\right)\beta\left(S_1 + \Delta S_1^{(j)}, T_1 + \Delta T_1^{(j)}, z_2\right),$$

$$a_{43} = -\frac{\partial \rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_2\right)}{\partial T}$$

$$= \rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_2\right)\alpha\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_2\right),$$

$$a_{44} = -\frac{\partial \rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_2\right)}{\partial S}$$

$$= -\rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_2\right)\beta\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_2\right),$$

$$a_{45} = a_{46} = ... = a_{4M} = 0,$$

$$a_{53} = 1, \quad a_{54} = \gamma_2,$$

$$a_{51} = a_{52} = a_{55} = a_{56} = a_{57} = ... = a_{5M} = 0,$$

$$a_{63} = \frac{\partial \rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_3\right)}{\partial T}$$

$$= -\rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_3\right)\alpha\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_3\right),$$

$$a_{64} = \frac{\partial \rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_3\right)}{\partial S}$$

$$= \rho\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_3\right)\beta\left(S_2 + \Delta S_2^{(j)}, T_2 + \Delta T_2^{(j)}, z_3\right),$$

$$a_{65} = -\frac{\partial \rho\left(S_3 + \Delta S_3^{(j)}, T_3 + \Delta T_3^{(j)}, z_3\right)}{\partial T}$$

$$= \rho\left(S_3 + \Delta S_3^{(j)}, T_3 + \Delta T_3^{(j)}, z_3\right)\alpha\left(S_3 + \Delta S_3^{(j)}, T_3 + \Delta T_3^{(j)}, z_3\right),$$

$$a_{66} = -\frac{\partial \rho\left(S_3 + \Delta S_3^{(j)}, T_3 + \Delta T_3^{(j)}, z_3\right)}{\partial S}$$

$$= -\rho\left(S_3 + \Delta S_3^{(j)}, T_3 + \Delta T_3^{(j)}, z_3\right)\beta\left(S_3 + \Delta S_3^{(j)}, T_3 + \Delta T_3^{(j)}, z_3\right),$$

$$a_{61} = a_{62} = a_{67} = a_{68} = \ldots\ldots = a_{6M} = 0,$$

……

$$a_{M-1,M-3}=1,\quad a_{M-1,M-2}=y_{N-1},$$

$$a_{M-1,1}=a_{M-1,2}=\cdots\cdots=a_{M-1,M-4}=a_{M-1,M-1}=a_{M-1,M}=0,$$

$$a_{M,M-3}=\frac{\partial\rho\left(S_{K-1}+\Delta S_{K-1}^{(j)},T_{K-1}+\Delta T_{K-1}^{(j)},z_K\right)}{\partial T}$$

$$=-\rho\left(S_{K-1}+\Delta S_{K-1}^{(j)},T_{K-1}+\Delta T_{K-1}^{(j)},z_K\right)\alpha\left(S_{K-1}+\Delta S_{K-1}^{(j)},T_{K-1}+\Delta T_{K-1}^{(j)},z_K\right),$$

$$a_{M,M-2}=\frac{\partial\rho\left(S_{K-1}+\Delta S_{K-1}^{(j)},T_{K-1}+\Delta T_{K-1}^{(j)},z_K\right)}{\partial S}$$

$$=\rho\left(S_{K-1}+\Delta S_{K-1}^{(j)},T_{K-1}+\Delta T_{K-1}^{(j)},z_K\right)\beta\left(S_{K-1}+\Delta S_{K-1}^{(j)},T_{K-1}+\Delta T_{K-1}^{(j)},z_K\right),$$

$$a_{M,M-1}=-\frac{\partial\rho\left(S_K+\Delta S_K^{(j)},T_K+\Delta T_K^{(j)},z_K\right)}{\partial T}$$

$$=\rho\left(S_K+\Delta S_K^{(j)},T_K+\Delta T_K^{(j)},z_K\right)\alpha\left(S_K+\Delta S_K^{(j)},T_K+\Delta T_K^{(j)},z_K\right),$$

$$a_{MM}=-\frac{\partial\rho\left(S_K+\Delta S_K^{(j)},T_K+\Delta T_K^{(j)},z_K\right)}{\partial S}$$

$$=-\rho\left(S_K+\Delta S_K^{(j)},T_K+\Delta T_K^{(j)},z_K\right)\beta\left(S_K+\Delta S_K^{(j)},T_K+\Delta T_K^{(j)},z_K\right),$$

$$b_1 = 0, \quad b_2 = 0, \quad b_3 = 0,$$

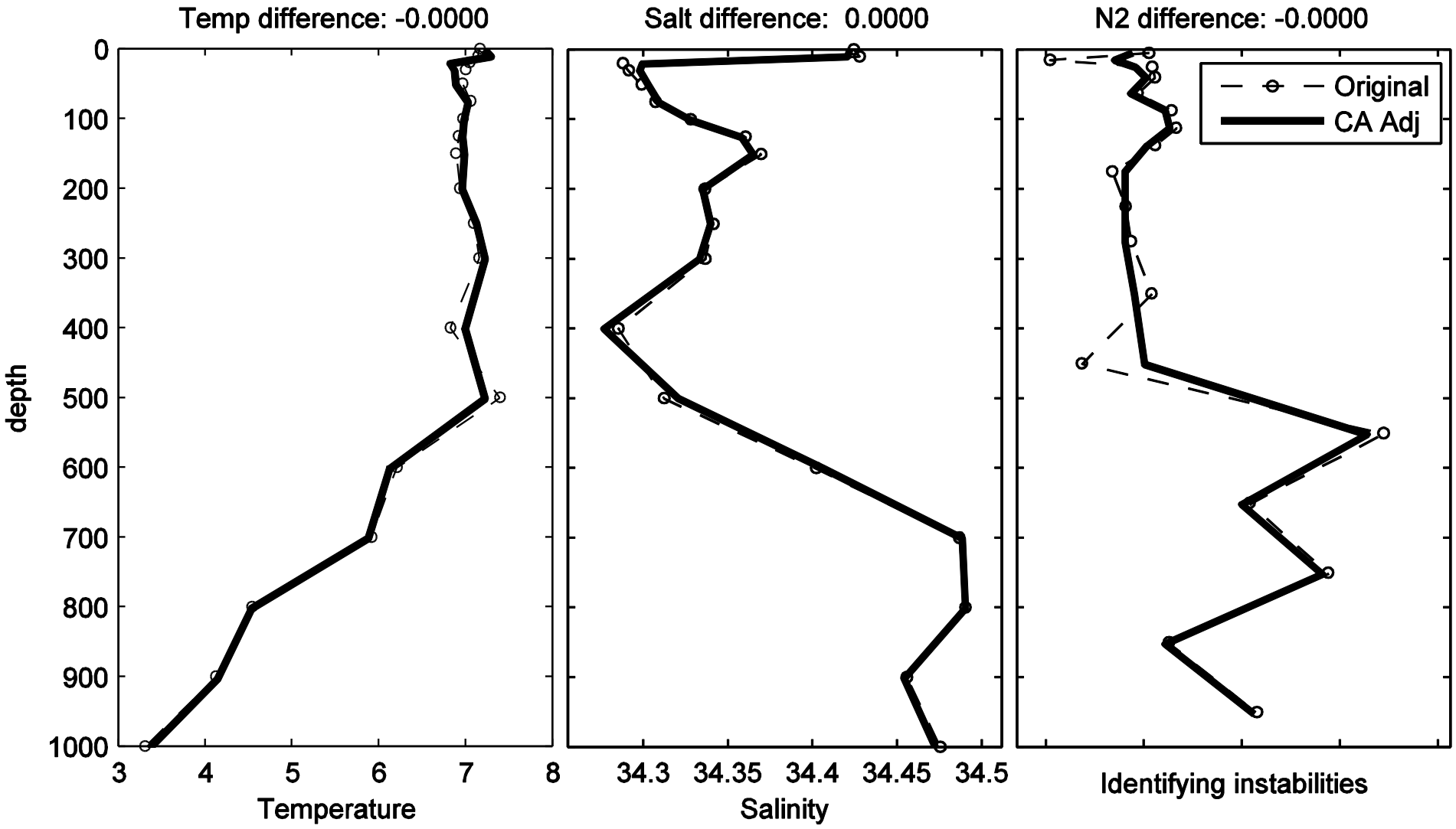
$$b_4 = E_1^{**} - \rho\left(S_1 + \Delta S_1^{(J)}, T_1 + \Delta T_1^{(J)}, z_1\right) + \rho\left(S_2 + \Delta S_2^{(J)}, T_2 + \Delta T_2^{(J)}, z_2\right),$$

$$b_5 = 0,$$

$$b_6 = E_2^{**} - \rho\left(S_2 + \Delta S_2^{(J)}, T_2 + \Delta T_2^{(J)}, z_2\right) + \rho\left(S_3 + \Delta S_3^{(J)}, T_3 + \Delta T_3^{(J)}, z_2\right), \ldots,$$

$$b_{M-1} = 0,$$

$$b_M = E_{K-1}^{**} - \rho\left(S_{K-1} + \Delta S_{K-1}^{(J)}, T_K + \Delta T_{K-1}^{(J)}, z_{K-1}\right) + \rho\left(S_K + \Delta S_K^{(J)}, T_K + \Delta T_K^{(J)}, z_{K-1}\right).$$



Original (dashed) and adjusted (solid) profiles temperature (T_k), salinity (S_k), and static stability (E_k) at the grid box 171.5°E, 53.5°E using the analytical conserved method.

Performance

- Heat and Salt Conserved
- Minimal Adjustment

RRMA = 0.0482 < 0.0712 (JM Method)

- Analytical → Well-Posed

Ocean Data Assimilation

Major Methods of Ocean Data Assimilation

- Optimal Interpolation (OI)
- Kalman Filter
- Variational Methods

Ocean Variables

$\mathbf{x}_t \rightarrow$ "true"

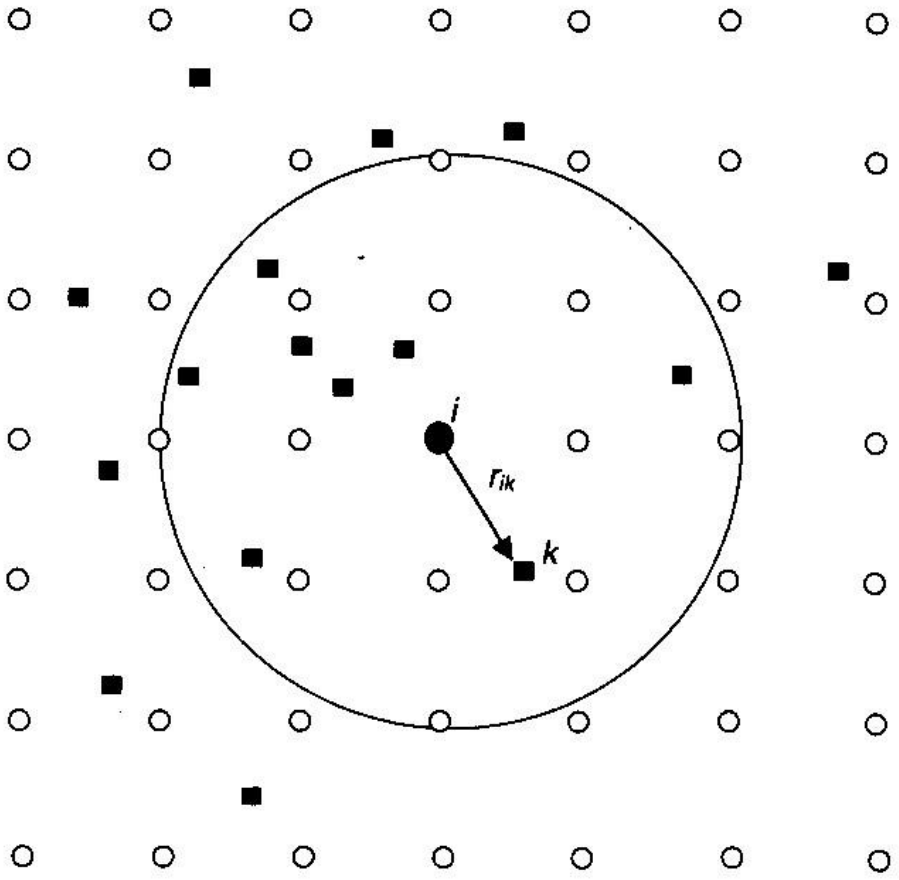
$\mathbf{x}_a \rightarrow$ analysis (model variables)

$\mathbf{x}_b \rightarrow$ background (or forecast)

$(\mathbf{x}_t, \mathbf{x}_a, \mathbf{x}_b) \rightarrow$ grid point (i)

$\mathbf{y}_o \rightarrow$ Observation $\rightarrow$ grid point (k)

Grid point (i)
Observational Point (k)



Data Analysis/Data Assimilation

→ Conducted in the Physical Space (**i**, **j**, **k**)

$$\mathbf{x}_a = \mathbf{x}_b + \mathbf{W} \bullet \mathbf{d},$$

Innovation → $\mathbf{d} = \mathbf{y}_o - H(\mathbf{x}_b)$

Various ways → **W** - Matrix

→ Different Data Assimilation Schemes

W → Gain Matrix (OI)

$$\min\left(\boldsymbol{\varepsilon}_a^T \bullet \boldsymbol{\varepsilon}_a\right) \quad \rightarrow$$

$$\mathbf{W} = \mathbf{B}\mathbf{H}^T\left(\mathbf{R} + \mathbf{H}\mathbf{B}\mathbf{H}^T\right)^{-1}$$

→Depends on **B**

R (usually assumed given)

W – Gain Matrix (3D-Var)

Minimizing Cost Function → $\nabla J(\mathrm{x}) = 0$

$$2J(\mathbf{x}) = (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b)$$
$$+[\mathbf{y}_o - H(\mathbf{x})]^T \mathbf{R}^{-1}[\mathbf{y}_o - H(\mathbf{x})]$$

$$\mathbf{W} = (\mathbf{B}^{-1} + \mathbf{H}^T\mathbf{R}^{-1}\mathbf{H})^{-1}\mathbf{H}^T\mathrm{P}^{-1}$$

→Depends on **B**

R (usually given)

W – Gain Matrix (Kalman Filter)

W – Matrix is called Kalman Gain

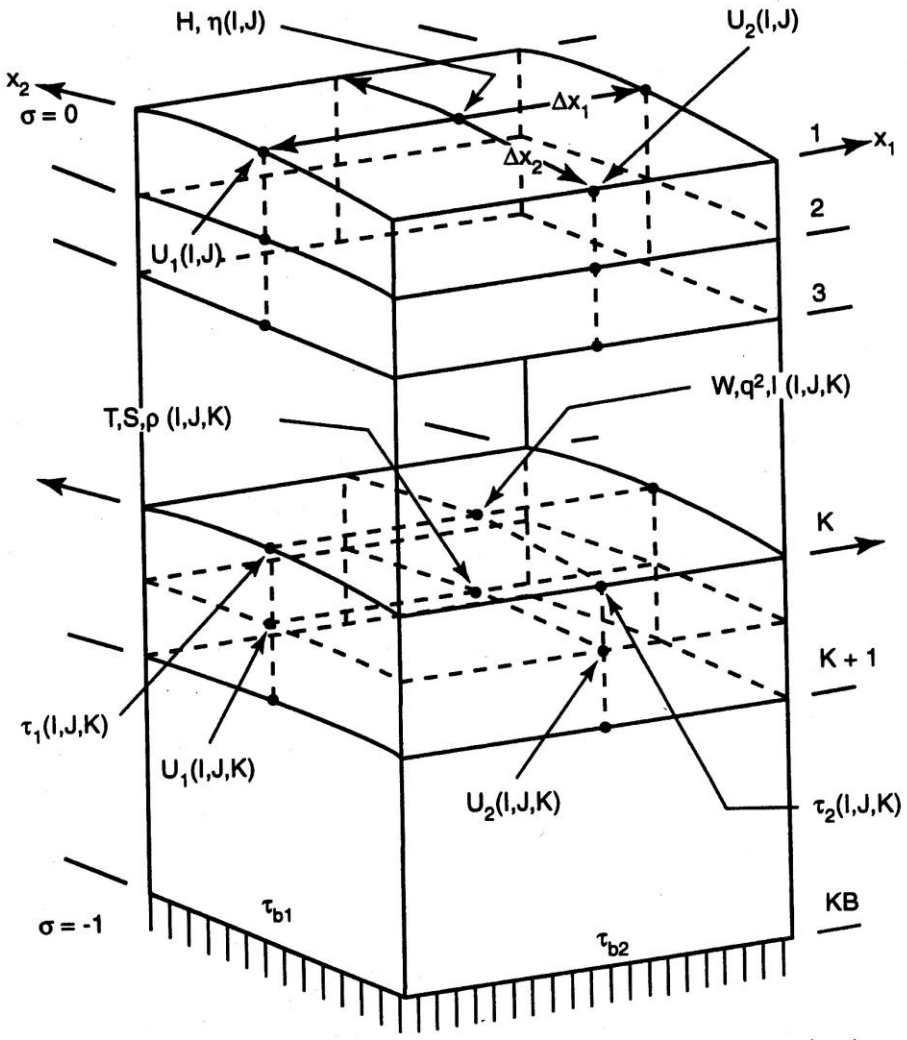
$$\mathbf{W}_i = \mathbf{P}^f(t_i)\mathbf{H}^T[\mathbf{R}_i + \mathbf{H}_i\mathbf{P}^f(t_i)\mathbf{H}^T]^{-1}$$

→Depends on forecast error covariance matrix

$$\mathbf{P}^f(t_i)$$

R (known)

Data Assimilation → Horizontal Planes



- Ocean observational (*T*, *S*) profile data has different sizes in vertical. The number of observational data may vary with horizontal level, i.e., more data points are assimilated in some levels than others. Due to nonlinearity of the Equation of State, such a treatment may lead to artificial static instability.

Density Difference

$$\rho_k^a(n) - \rho_k^a(n+1) = \Delta\rho$$

$n \rightarrow$ z-level $\rightarrow$ z_n

Here, n increases downward.

NODC Static Stability Criterion

- Density inversion → Depth-decrease of density of two consecutive z-levels

$\Delta\rho$ < 0.03 kg m^{-3} (-30 m $\leq$ z < 0)

< 0.02 kg m^{-3} (-400 m < z < -30 m)

< 0 kg m^{-3} (z < -400 m)

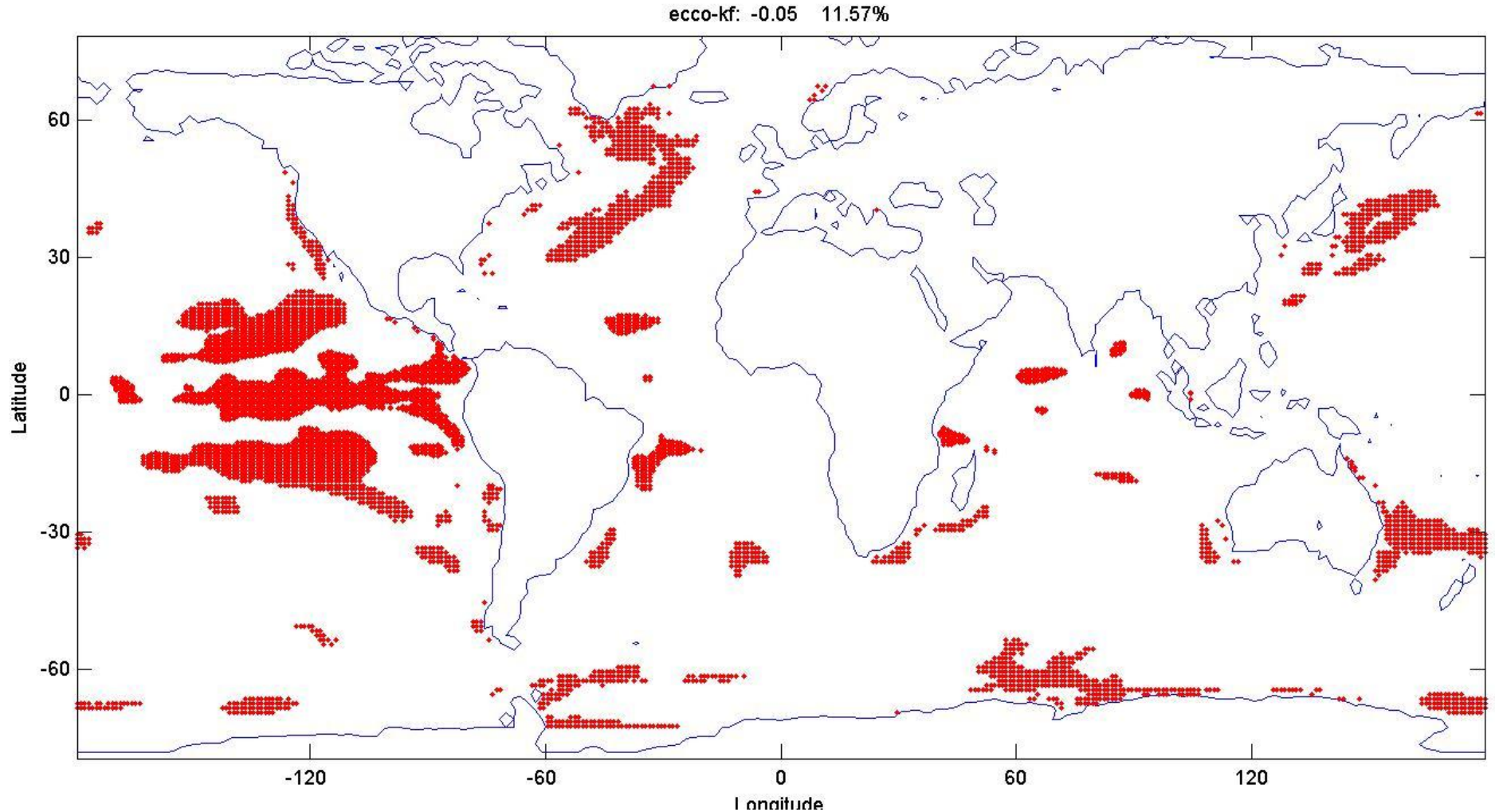
Example
JPL Estimating the Circulation and Climate of the Ocean (JPL-ECCO) 10 day

MIT General Circulation Model
+ Kalman Filter

JPL-ECCO 2007 (10-day)

Centered on Dec 31, 2008

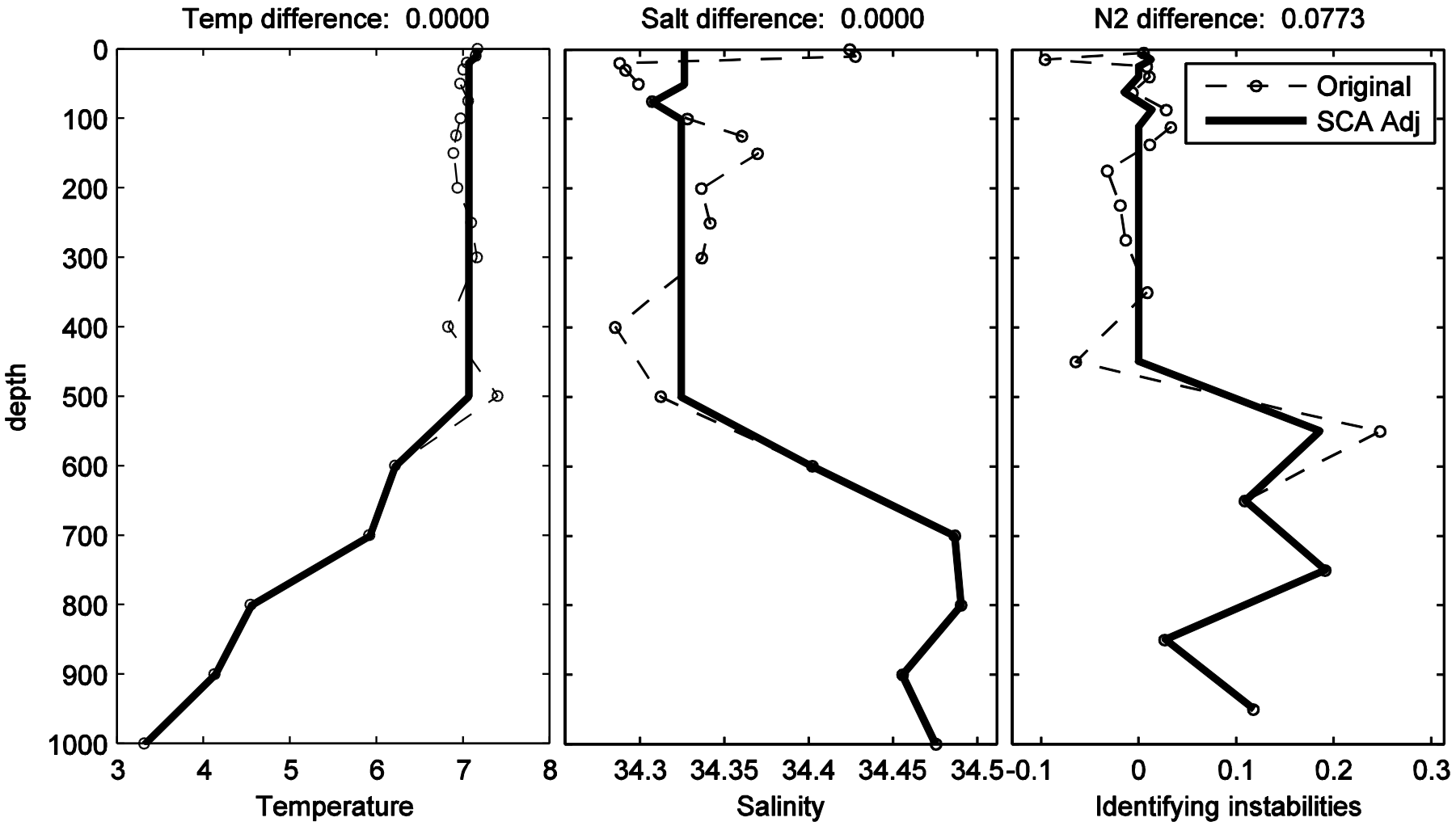
Unstable Profiles → 11.57%



Convective Adjustment in Ocean Models

- Whenever a water column is statically unstable, temperature and salinity are vertically adjusted to make the water column neutrally stable, with heat and salt conserved in the process.

- For ocean data assimilation, it may over-adjust since there is no convection. Unstable stratification is caused by combination of modeled and observed data.



Original (dashed) and adjusted (solid) profiles temperature (T_k), salinity (S_k), and static stability (E_k) at the grid box 171.5°E, 53.5°E using the complete convective adjustment method (Yin and Sarachik Locarnini 1994).

Performance

- Heat and Salt Conserved
- Large Adjustment

RRMA = 0.2192 > 0.0712 (JM Method)
> 0.0482 (Analytical Method)

- Analytical → Well-Posed

Conclusions

- This scheme has the following features:
  - (1) Heat and salt conservation
  - (2) Removal of static instabilities with small (T, S) adjustments
  - (3) analytical form

Monthly Temperature (10 m) in the Pacific Ocean since 1990



Monthly Temperature (1000 m) in the Pacific Ocean since 1990



Monthly Temperature (10 m) in the Atlantic Ocean since 1990



Monthly Temperature (1000 m) in the Atlantic Ocean since 1990



Conclusions

- (1) False static instability in ocean climate (T, S) datasets with data analysis and assimilation on z-levels due to nonlinearity of the equation of state.
- (2) Assimilation of (T, S) data should keep the vertical structure such as the treatments in building GDEM and the OSD method.
- (3) It is urgent to reprocess the (T, S) datasets with false static instability.
- (4) Numerical model results need to be re-evaluated if the (T, S) datasets with false static instability were used.