

**Variability of the Antarctic Intermediate Water  
across the Equatorial Atlantic in 2004 Detected from  
ARGO Float Trajectory Data**

**Rapid Change of Mid-Depth North  
Atlantic Circulations in Tropics**

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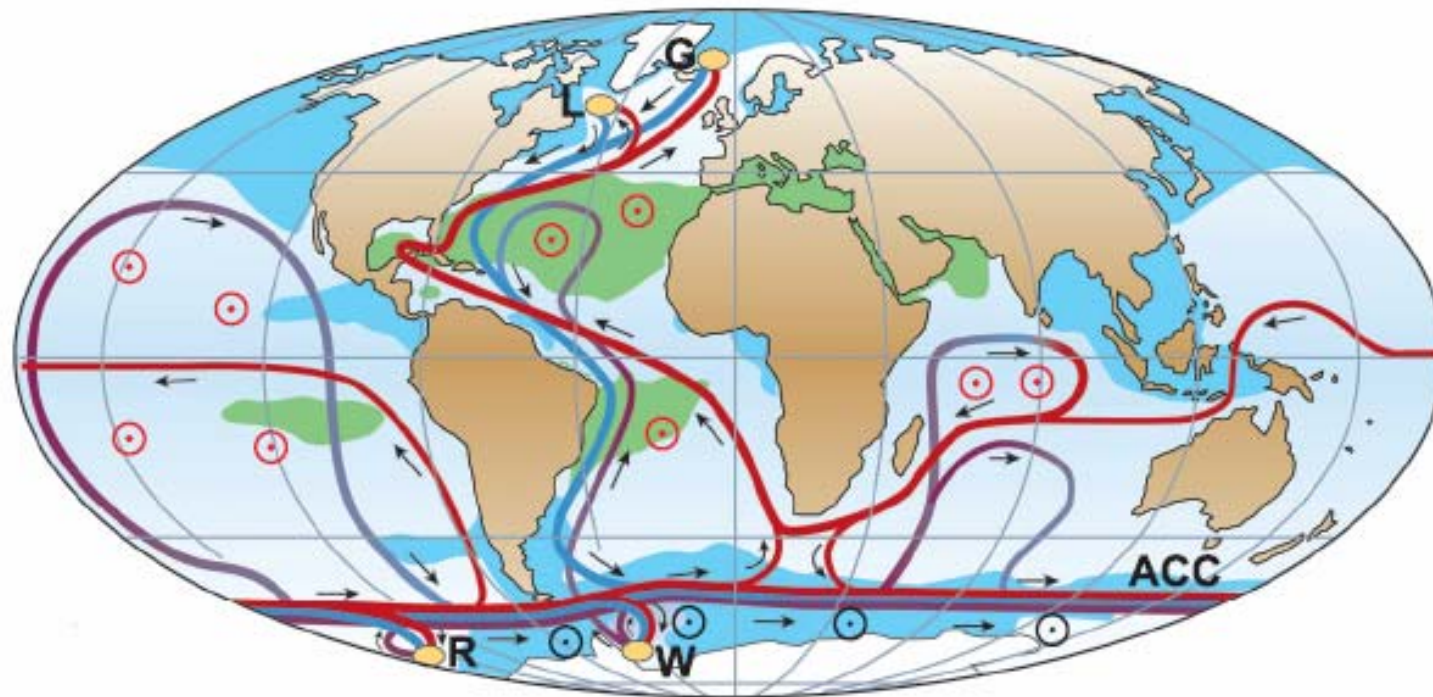
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# Important Element in Climate System

## Meridional Overturning Circulation (MOC)

(Rahmstorf 2006)



- Surface flow
- Deep flow
- Bottom flow
- Deep Water Formation

- ⊙ Wind-driven upwelling
- ⊗ Mixing-driven upwelling
- Salinity > 36 ‰
- Salinity < 34 ‰

- L Labrador Sea
- G Greenland Sea
- W Weddell Sea
- R Ross Sea

MOC Variation →

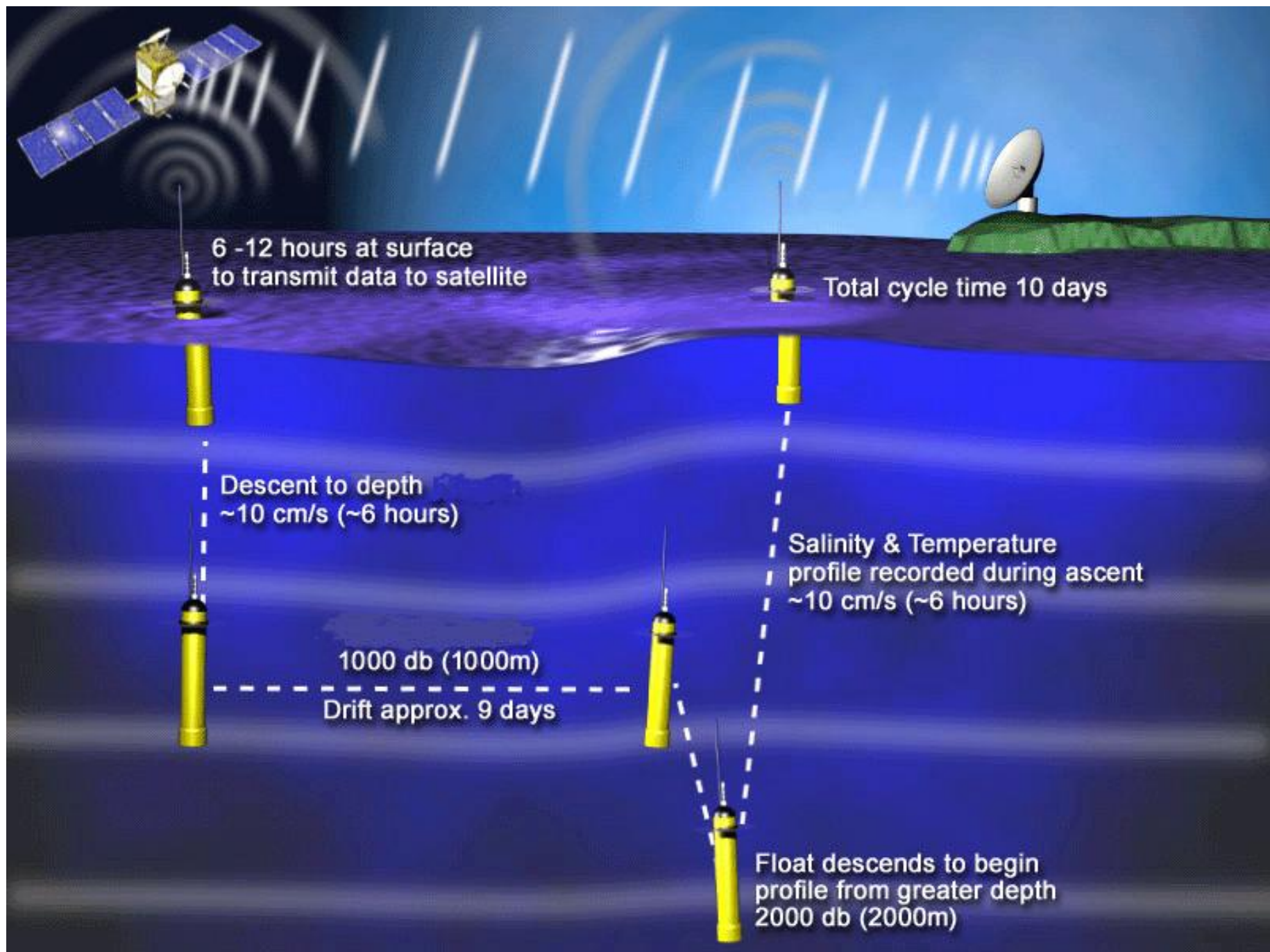
Heat Transport Variation →

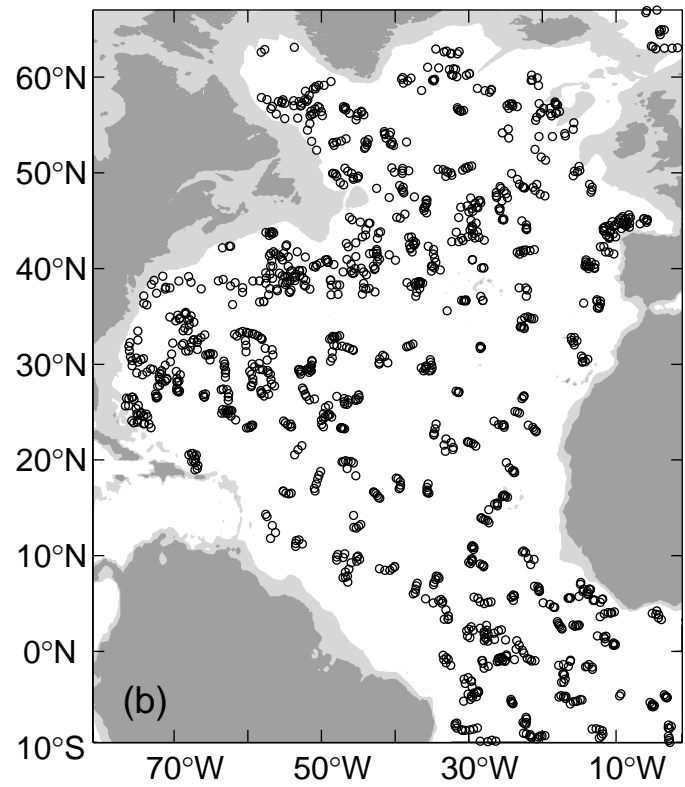
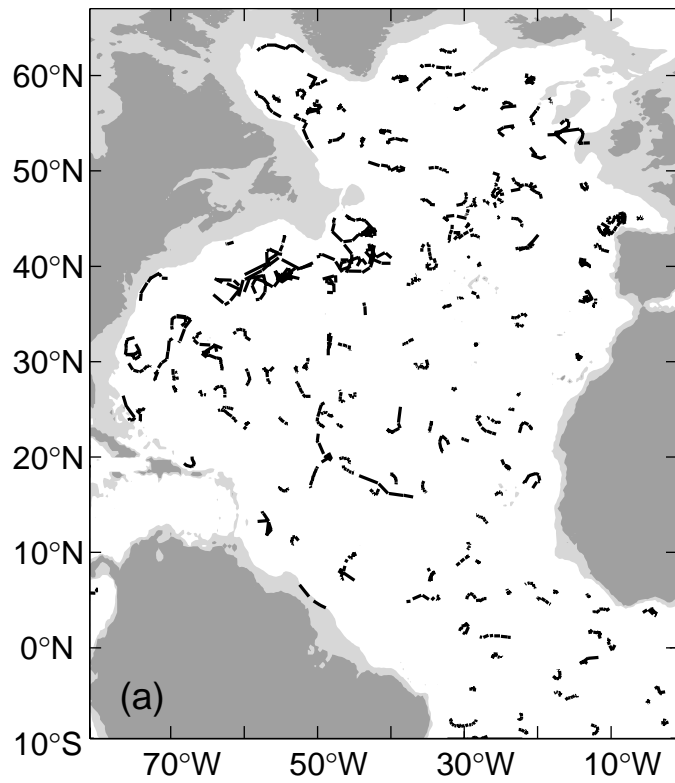
Climate Change

- Are mid-depth (~1000 m) ocean circulations steady?
- If not,  
what mechanisms cause the change? (Rossby wave propagation)

(I will answer this question at  
1:45 pm on Thursday at 11 IOAS-AOLS)

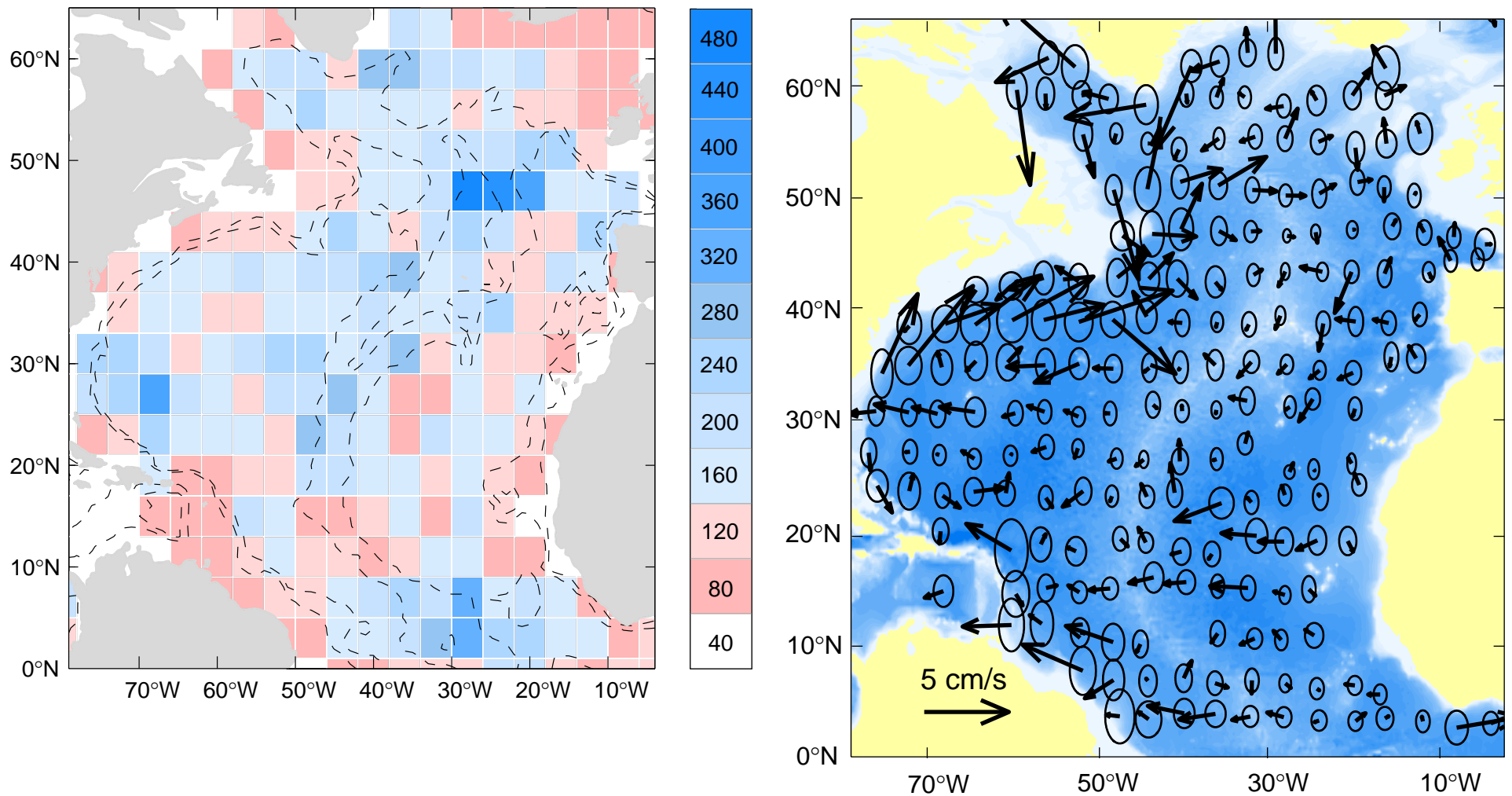






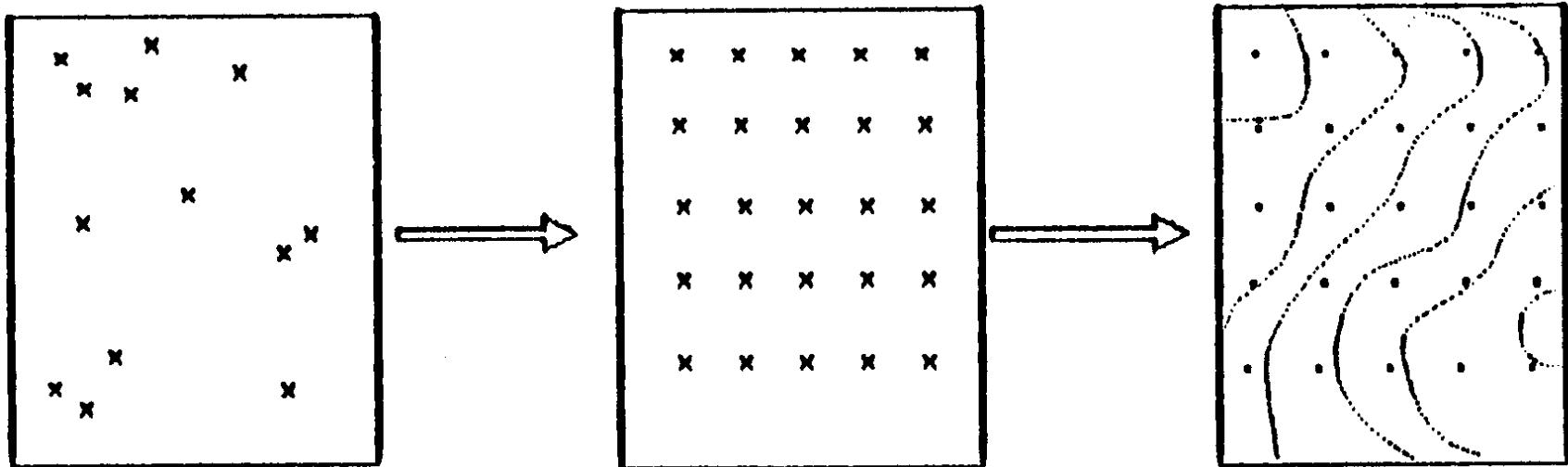
# Circulations at 1000 m estimated from the original ARGO float tracks (bin method)

## April 2004 – April 2005



# Most Popular Method for Ocean Data Analysis

## Optimum Interpolation (OI)



# OI Method Requires:

- (1) First guess field
- (2) Known statistics  
such as the autocorrelation function

# Ocean velocity data

- (1) First guess field (?)
- (2) Unknown autocorrelation function

# Two Ways Out

- (1) Using numerical model to calculate the first guess field and autocorrelation function (Davis, 2002, 2004)
- (2) Using the OSD method

# OSD

## Spectral Representation

$$c(\mathbf{x}, z_k, t) = A_0(z_k, t) + \sum_{m=1}^M A_m(z_k, t) \Psi_m(\mathbf{x}, z_k),$$

**Spatial Variability is represented  
by the basis functions**



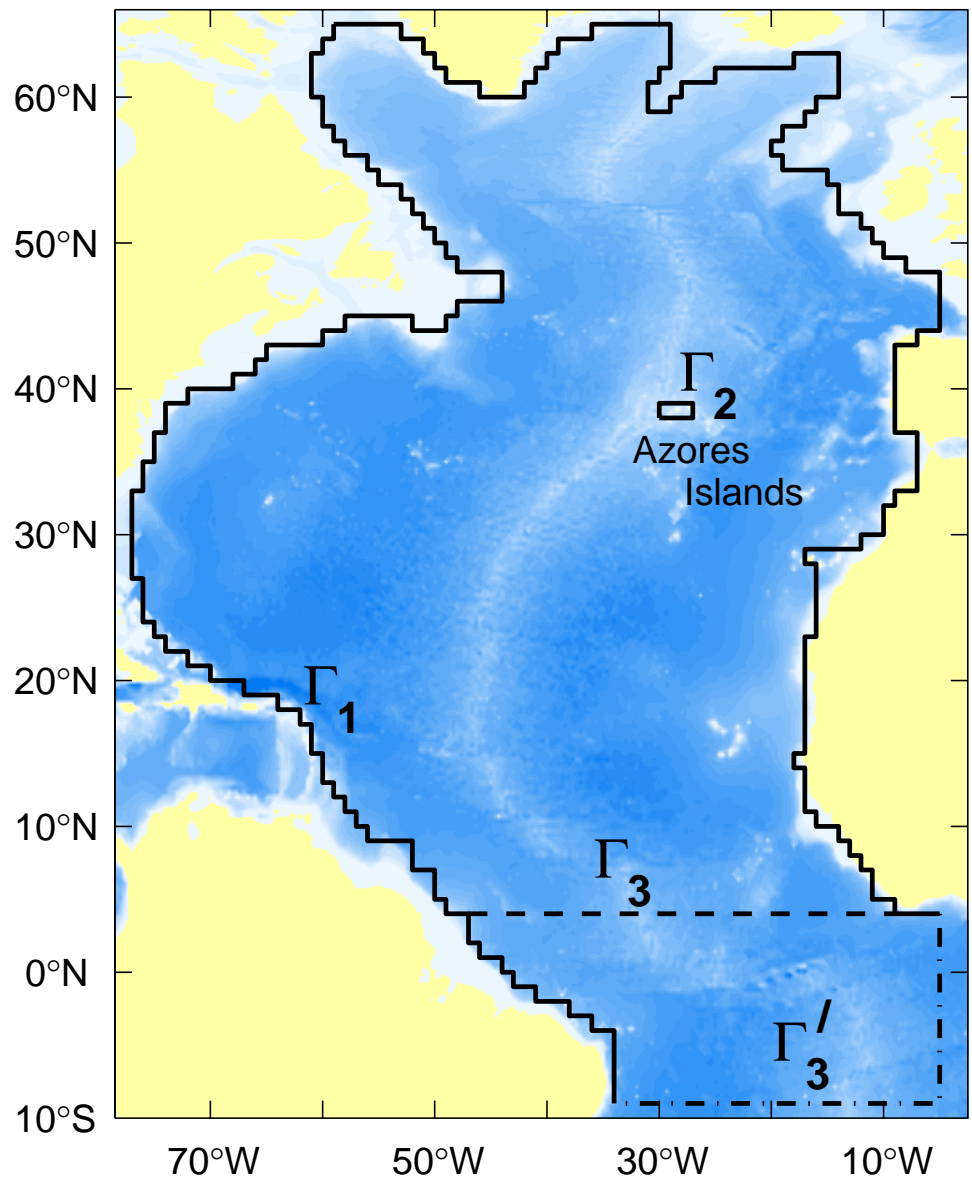
# References

- Chu, P.C., L.M. Ivanov, T.P. Korzhova, T.M. Margolina, and O.M. Melnichenko, 2003a: Analysis of sparse and noisy ocean current data using flow decomposition. Part 1: Theory. *Journal of Atmospheric and Oceanic Technology*, 20 (4), 478-491.
- Chu, P.C., L.M. Ivanov, T.P. Korzhova, T.M. Margolina, and O.M. Melnichenko, 2003b: Analysis of sparse and noisy ocean current data using flow decomposition. Part 2: Application to Eulerian and Lagrangian data. *Journal of Atmospheric and Oceanic Technology*, 20 (4), 492-512.
- Chu, P.C., L.M. Ivanov, and T.M. Margolina, 2004: Rotation method for reconstructing process and field from imperfect data. *International Journal of Bifurcation and Chaos*, 14(8), 2991-2997.
- Chu, P.C., L.M. Ivanov, and O.M. Melnichenko, 2005: Fall-winter current reversals on the Texas-Louisiana continental shelf. *Journal of Physical Oceanography*, 35, 902-910
- Chu, P.C., L.M. Ivanov, O.M. Melnichenko, and N.C. Wells, 2007: On long baroclinic Rossby Waves in the tropical North Atlantic observed from profiling floats. *Journal of Geophysical Research – Oceans*, in press.
- These papers can be downloaded from:
- <http://www.oc.nps.navy.mil/~chu>

# Two approaches to obtain basis functions

- EOFs
- Eigenfunctions of Laplace Operator
- (closed lateral boundary)

$$\nabla_h^2 \Psi_m = -\lambda_m \Psi_m, \quad \Psi_m|_{\Gamma} = 0, \quad m = 1, 2, \dots, M.$$



# Basis Functions of Laplace Operator (Open Boundaries)

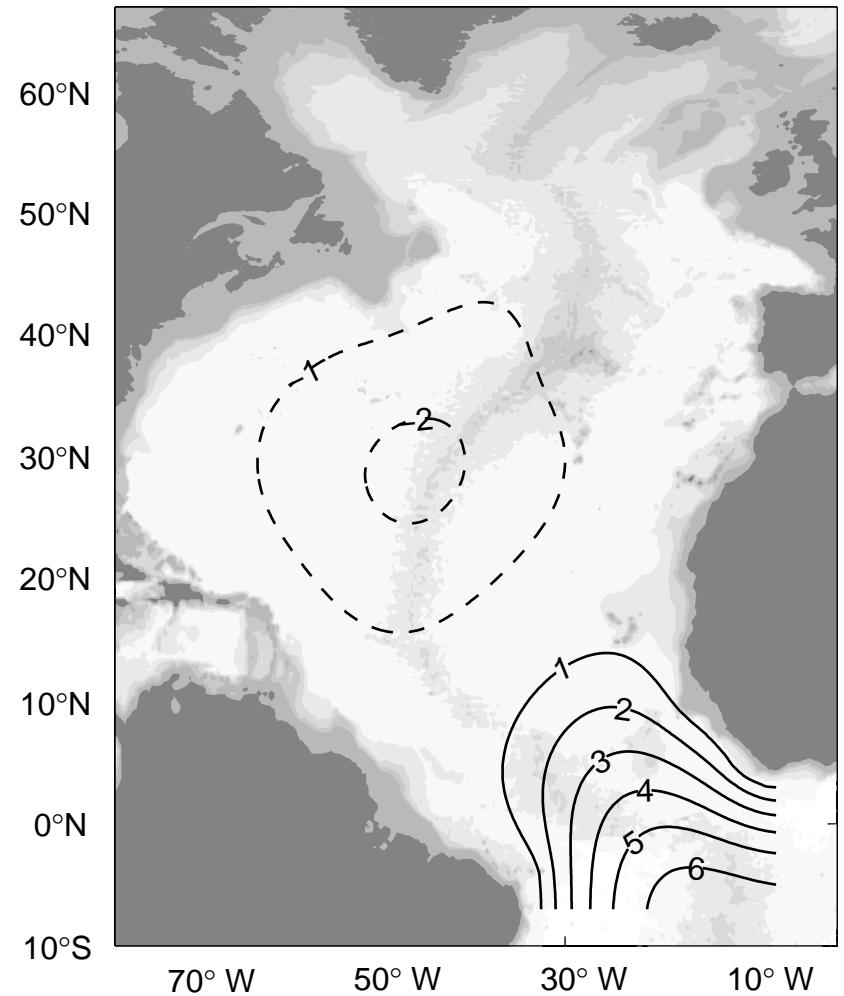
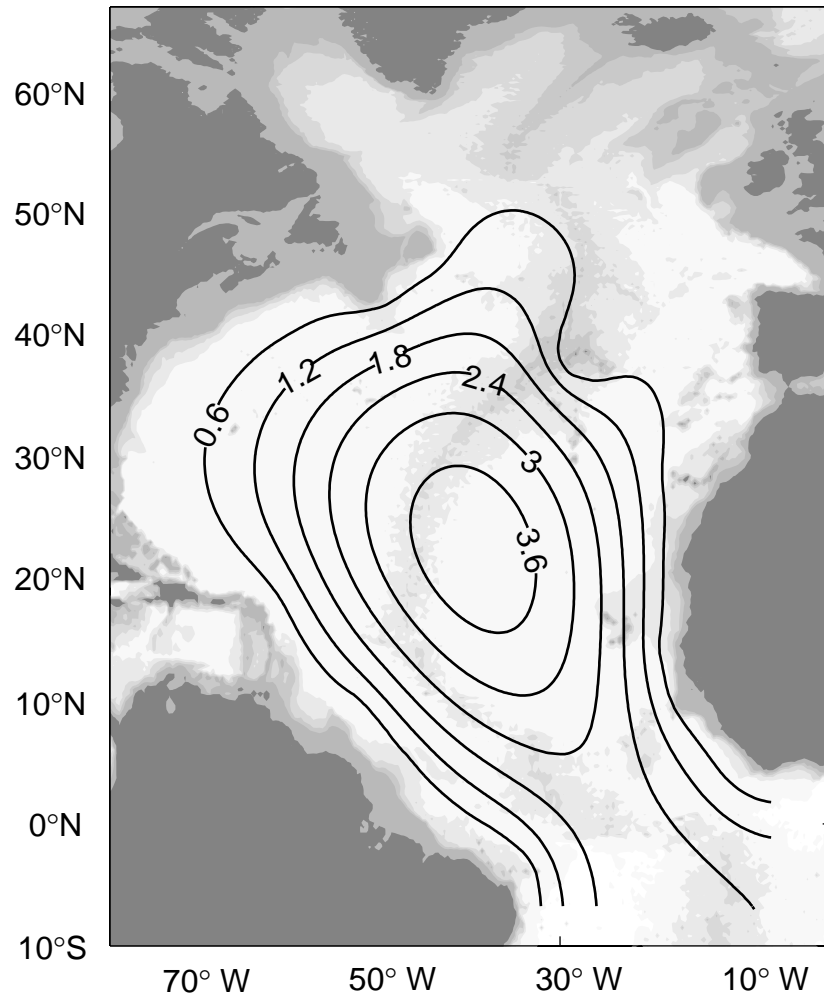
$$\Delta \Psi_k = -\lambda_k \Psi_k,$$

$$\Delta \Phi_m = -\mu_m \Phi_m,$$

$$\Psi_k|_{\Gamma} = 0, \quad \frac{\partial \Phi_m}{\partial n}|_{\Gamma} = 0,$$

$$\left[ \frac{\partial \Psi_k}{\partial n} + \kappa(\tau) \Psi_k \right] |_{\Gamma'_1} = 0, \quad \Phi_m|_{\Gamma'_1} = 0,$$

# Basis Functions for Streamfunction Mode-1 and Mode-2



# Spectral Decomposition

$$u_{KM} = \sum_{k=1}^K a_k(z, t^\circ) \frac{\partial \Psi_k(x, y, z, \kappa^\circ)}{\partial y} + \sum_{m=1}^M b_m(z, t^\circ) \frac{\partial \Phi_m(x, y, z)}{\partial x},$$
$$v_{KM} = - \sum_{k=1}^K a_k(z, t^\circ) \frac{\partial \Psi_k(x, y, z, \kappa^\circ)}{\partial x} + \sum_{m=1}^M b_m(z, t^\circ) \frac{\partial \Phi_m(x, y, z)}{\partial y}$$

# Optimal Mode Truncation

$$J(a_1, \dots, a_K, b_1, \dots, b_M, \kappa, P) = \frac{1}{2} \left( \|u_p^{obs} - u_{KM}\|_P^2 + \|v_p^{obs} - v_{KM}\|_P^2 \right) \rightarrow \min,$$

# Vapnik (1983) Cost Function

$$J_{emp} = J(a_1, \dots, a_K, b_1, \dots, b_M, \kappa, P).$$

$$\text{Prob} \left\{ \sup_{K, M, S} |\langle J(K, M, S) \rangle - J_{emp}(K, M, S)| \geq \mu \right\} \leq g(P, \mu)$$

$$\lim_{P \rightarrow \infty} g(P, \mu) = 0$$



# Optimal Truncation

- ARGO Data (Mid-Depth North Atlantic)

$K_{opt} = 38$ ,  $M_{opt} = 24$

# Determination of Spectral Coefficients (Ill-Posed Algebraic Equation)

$$\mathbf{A} \hat{\mathbf{a}} = \mathbf{QY},$$

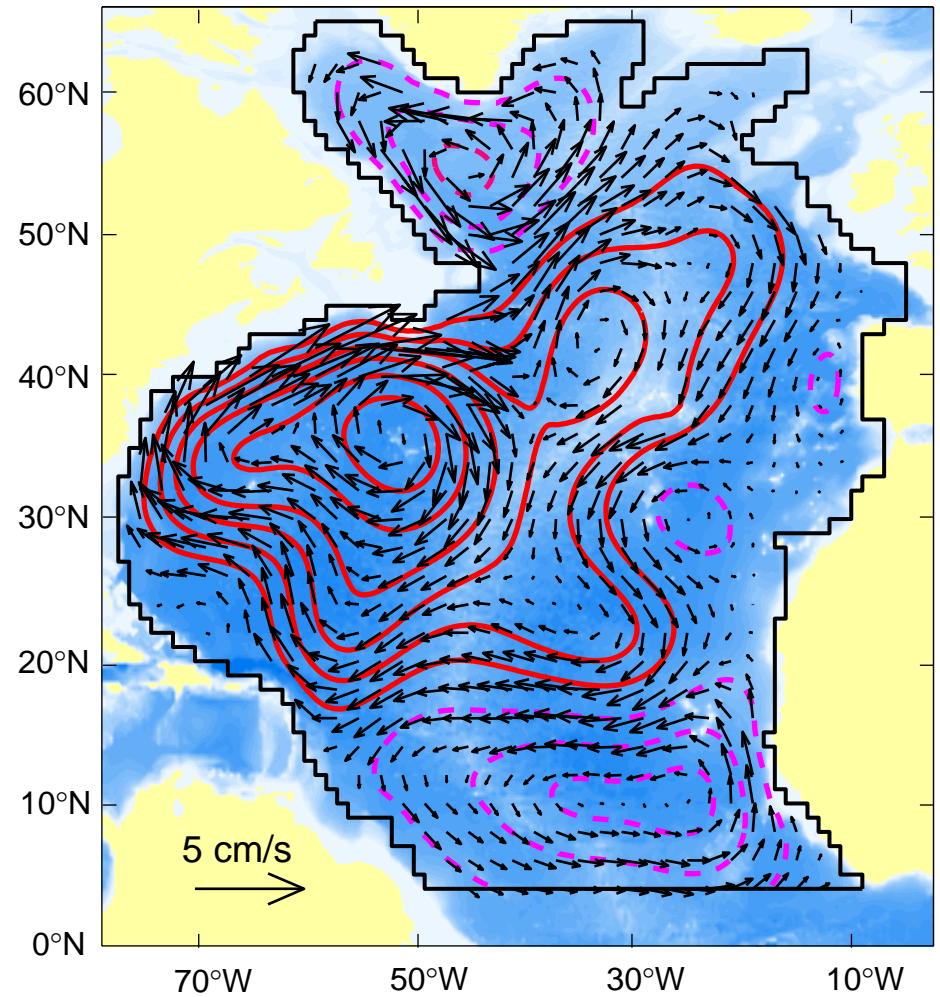
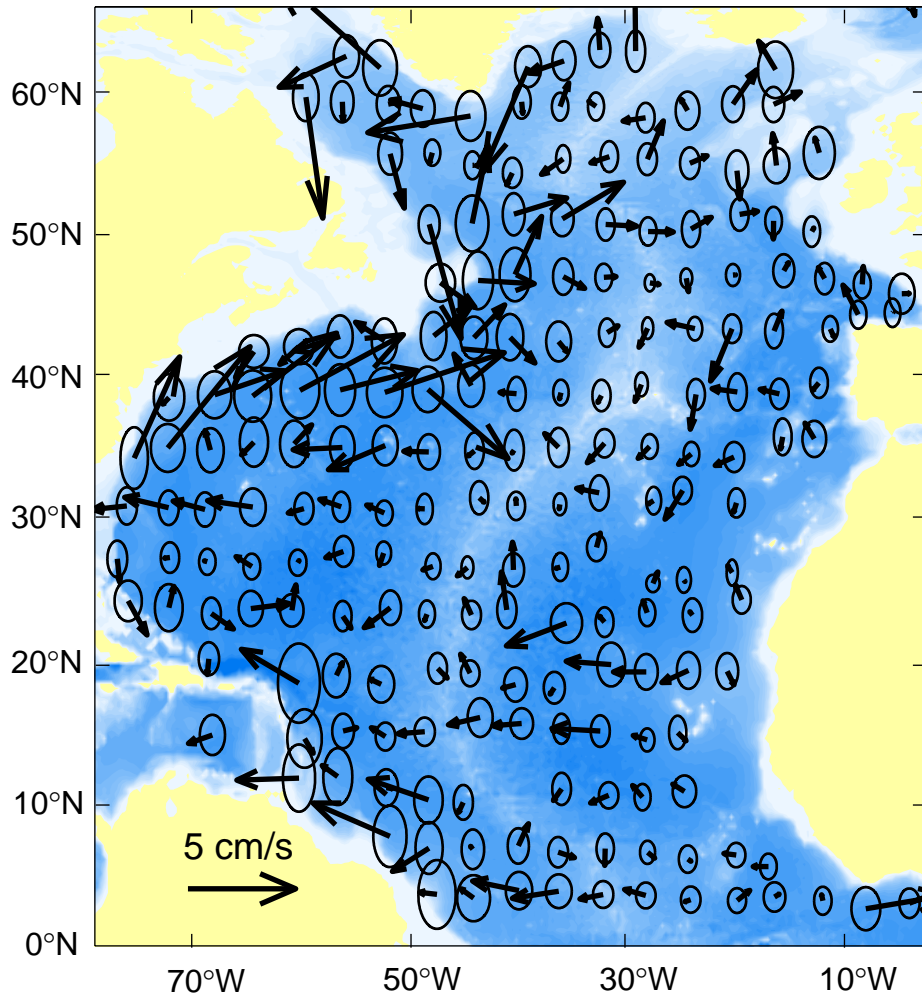
# Rotation Method for Solving Ill-Posed Algebraic Equation (Chu et al., 2004)

$$\mathbf{SA}\hat{\mathbf{a}} = \mathbf{SQY},$$

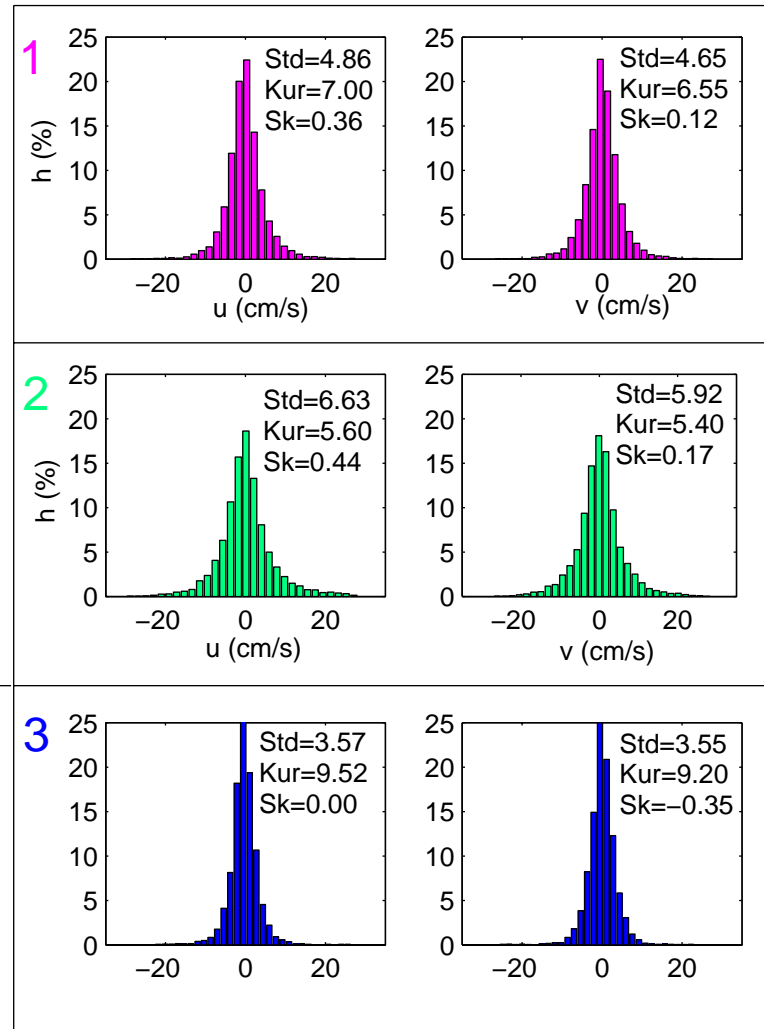
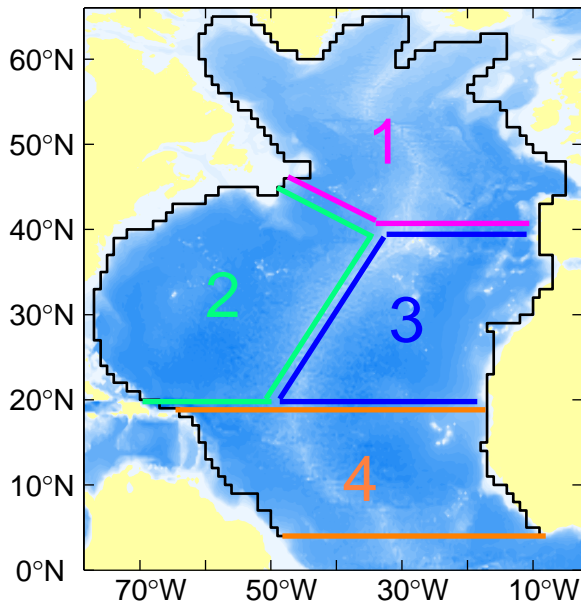
$$J_1 = \|\mathbf{A}\|^2 - \frac{\|\mathbf{SQY}\|^2}{\|\mathbf{a}\|^2} \rightarrow \max,$$

# Circulations at 1000 m (March 04 to May 05)

## Bin Method OSD



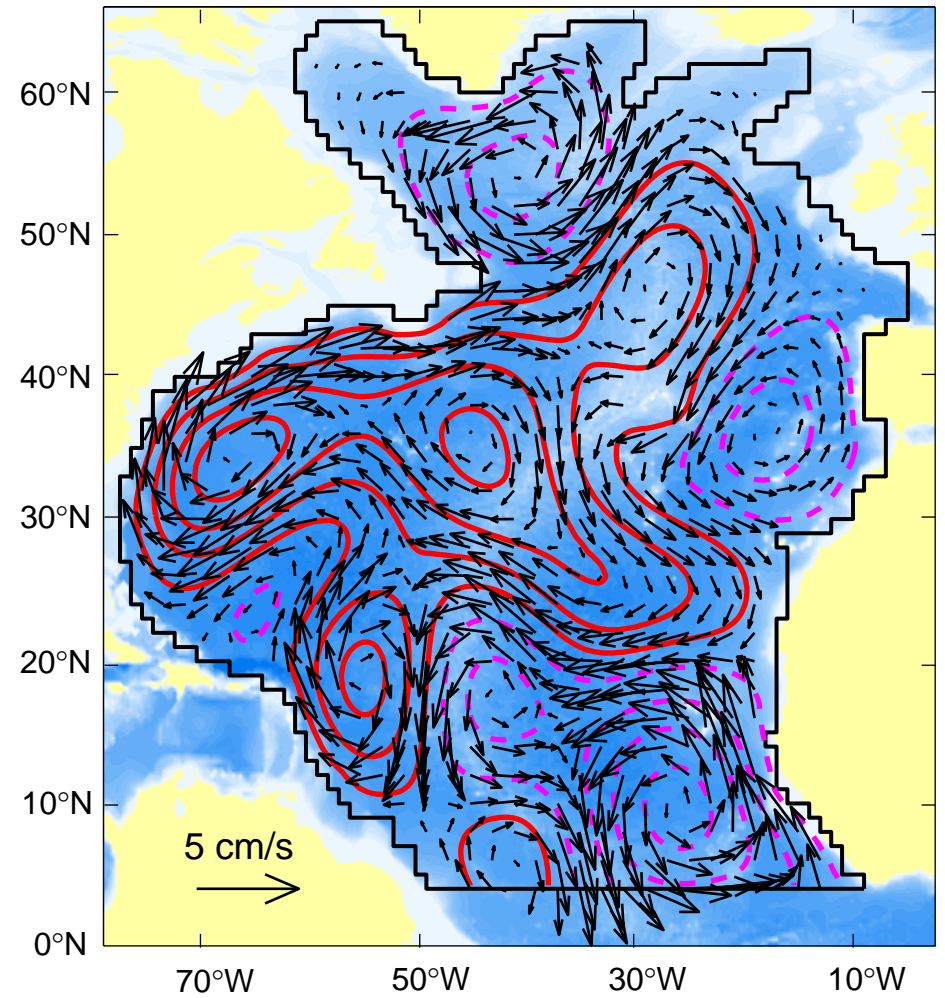
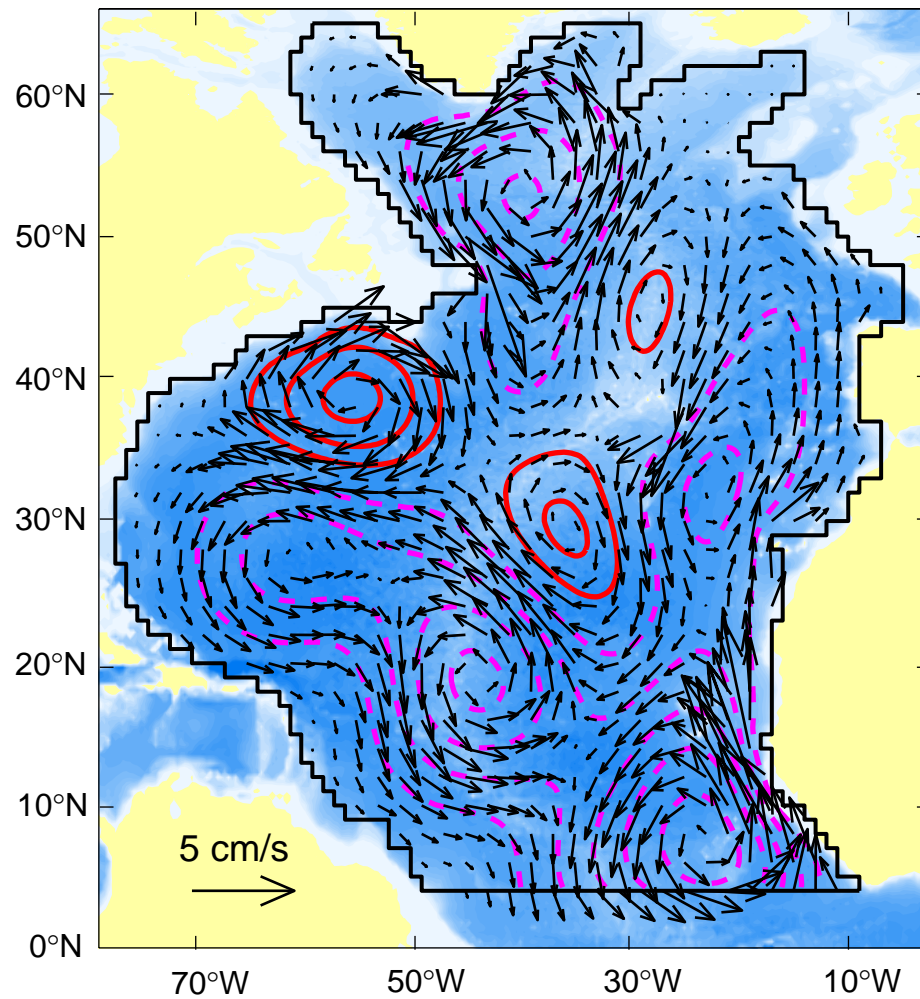
# Velocity Variability ( $V_{\text{obs}} - \langle V \rangle_{\text{rec}}$ )



# Mid-Depth Circulations (1000 m)

March-May 04

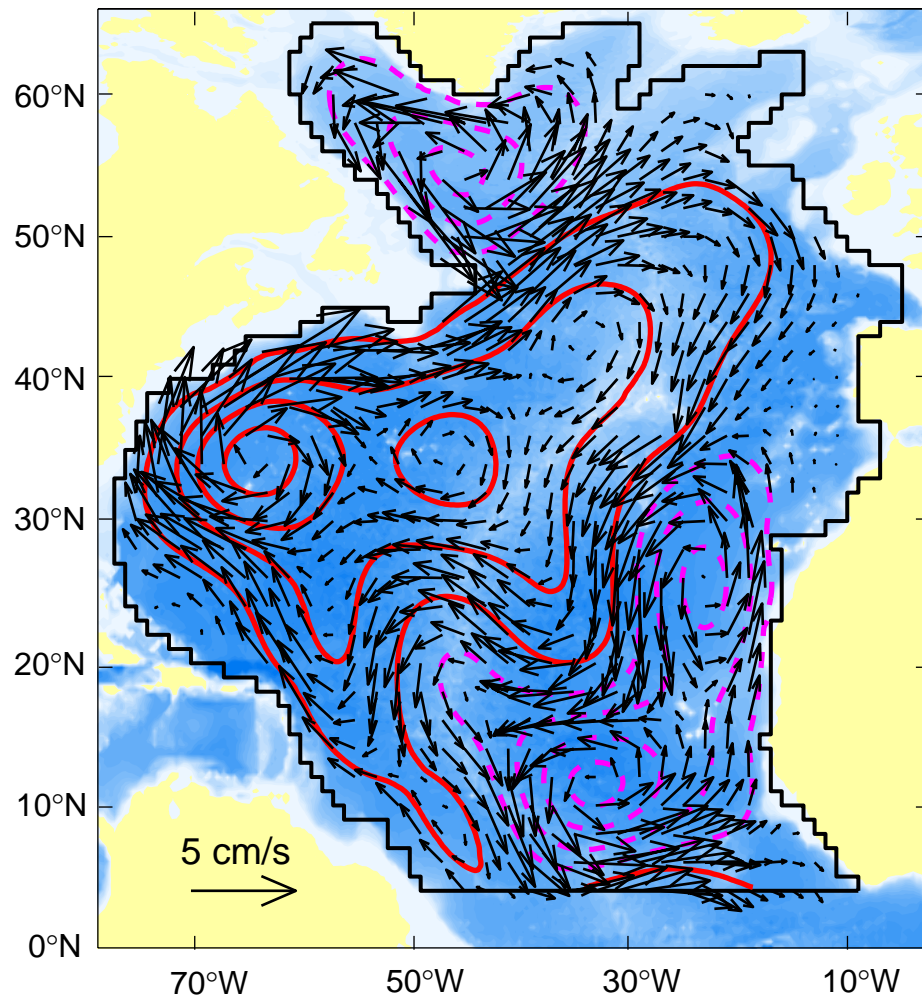
May-July 04



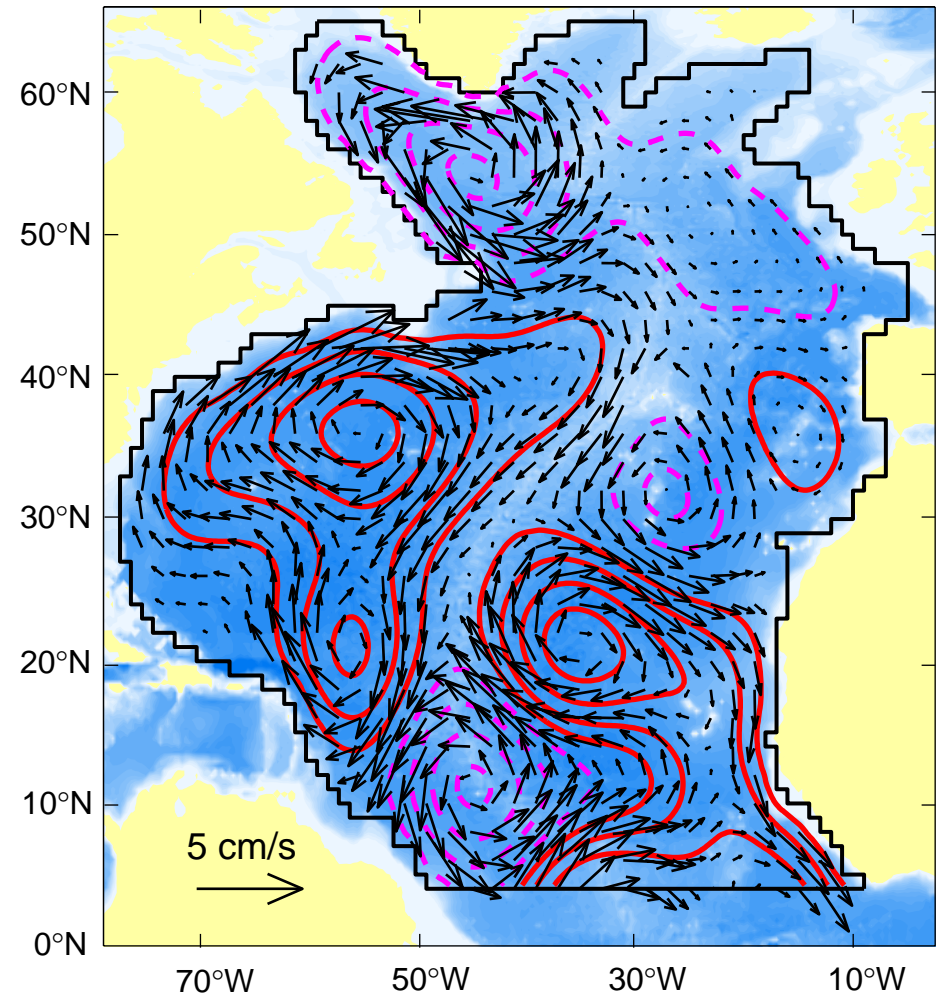


# Mid-Depth Circulations (1000 m)

July-Sept 04

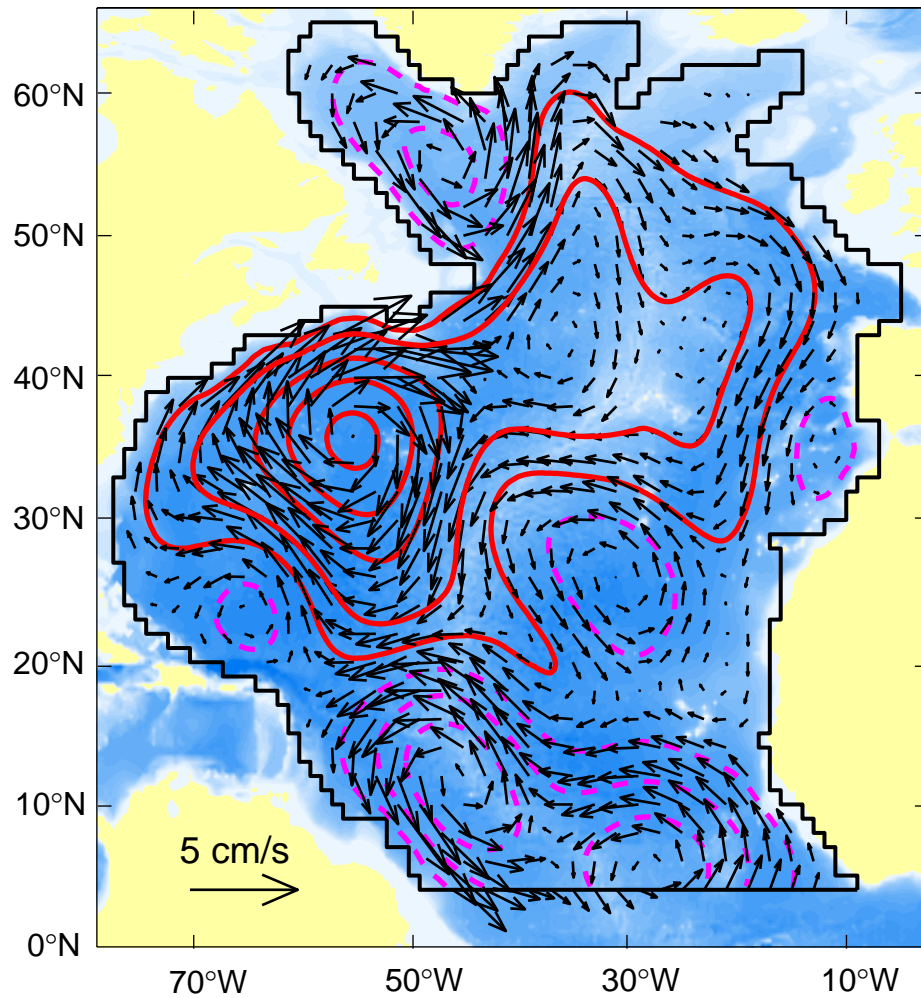


Sept-Nov 04

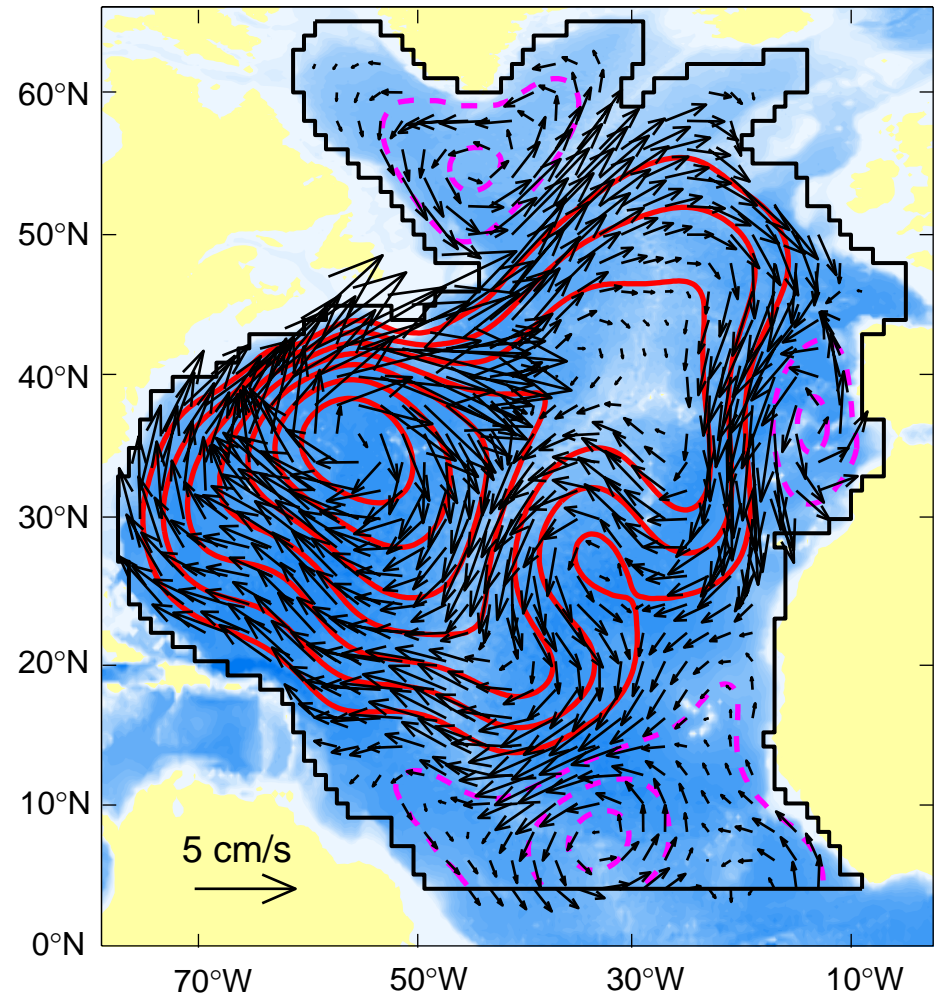


# Mid-Depth Circulations (1000 m)

Nov 04-Jan 05

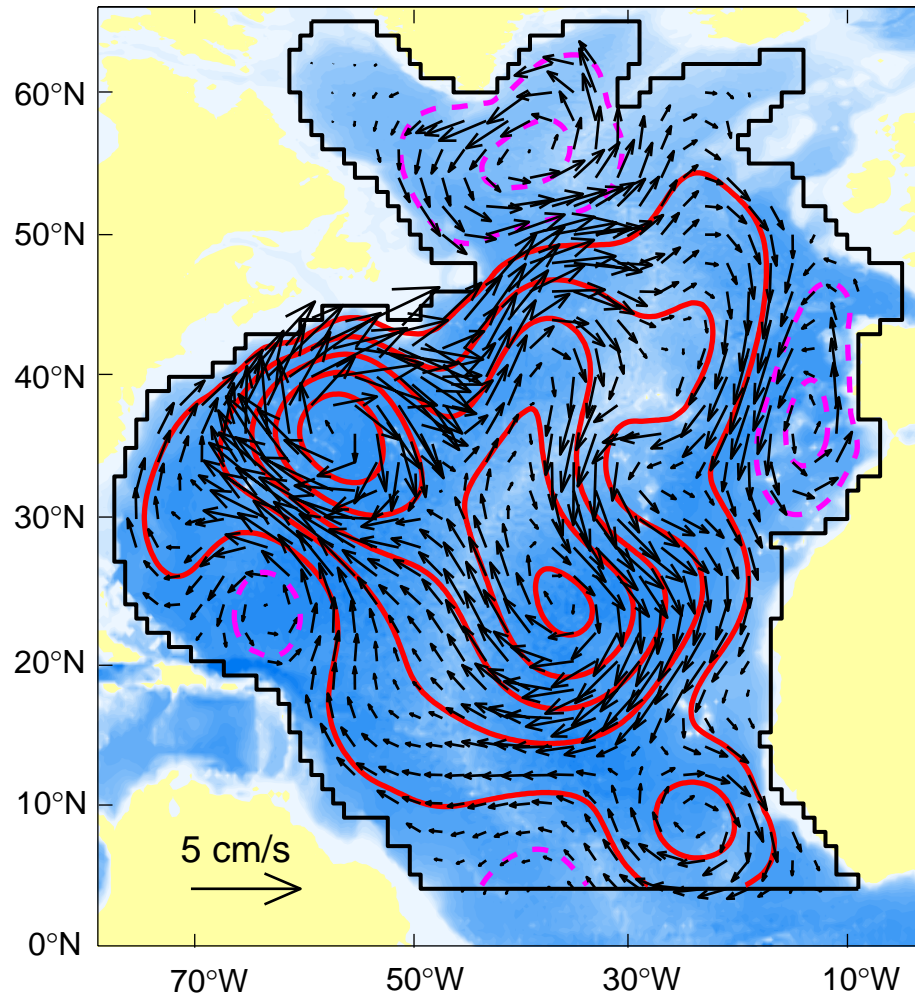


Jan-Mar 05



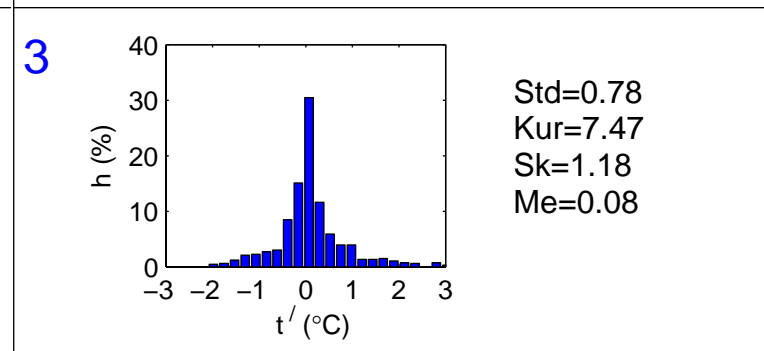
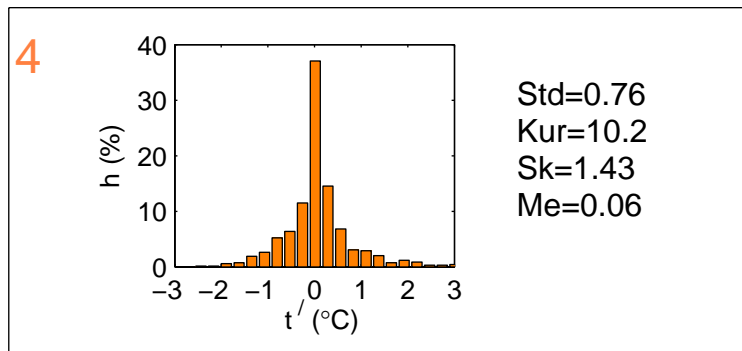
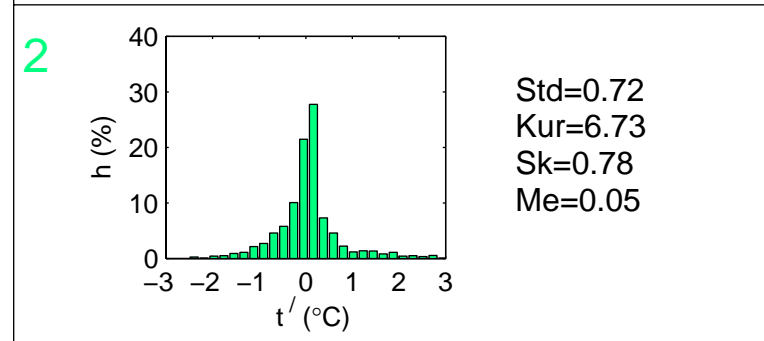
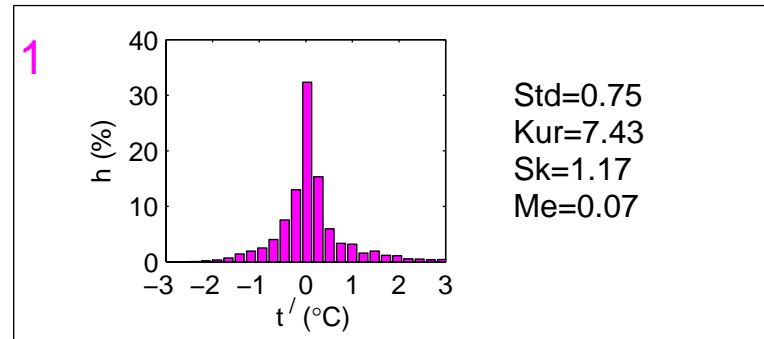
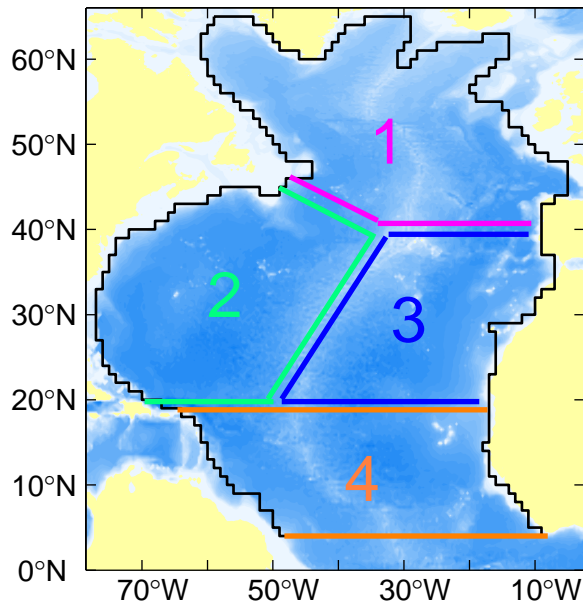


# Mid-Depth Circulations (1000 m) Mar-May 05





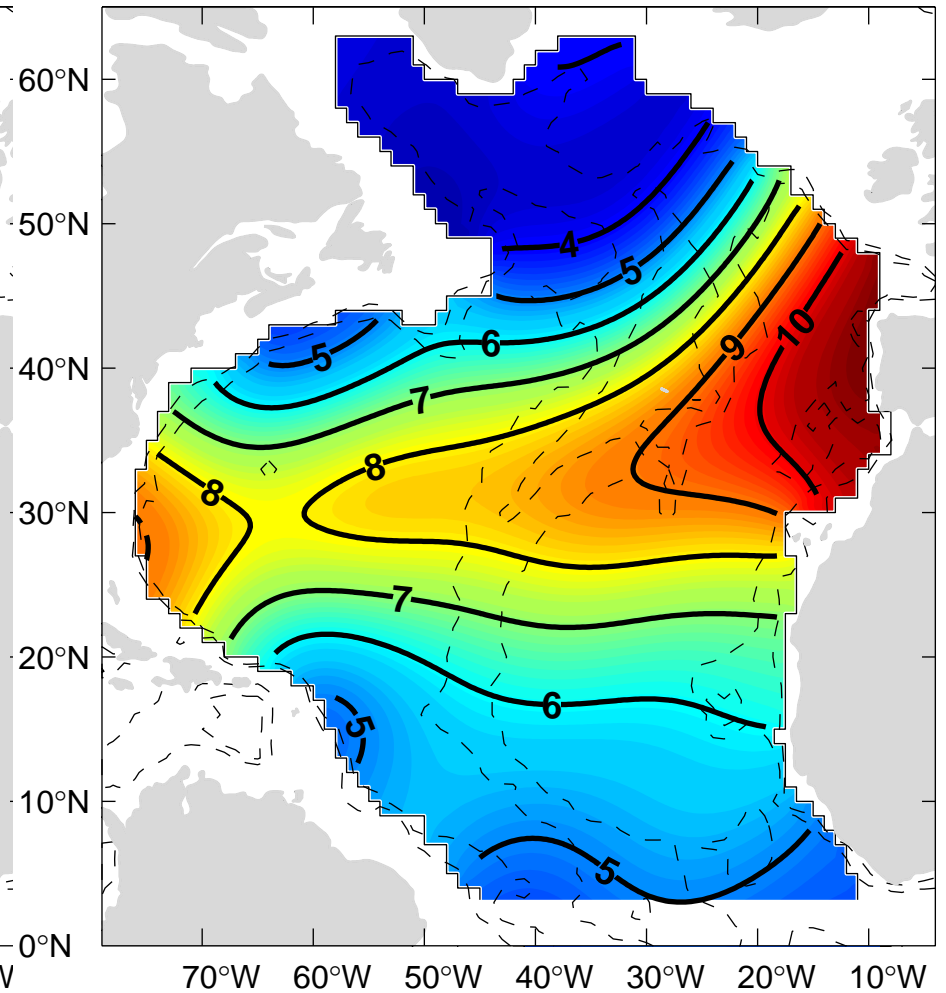
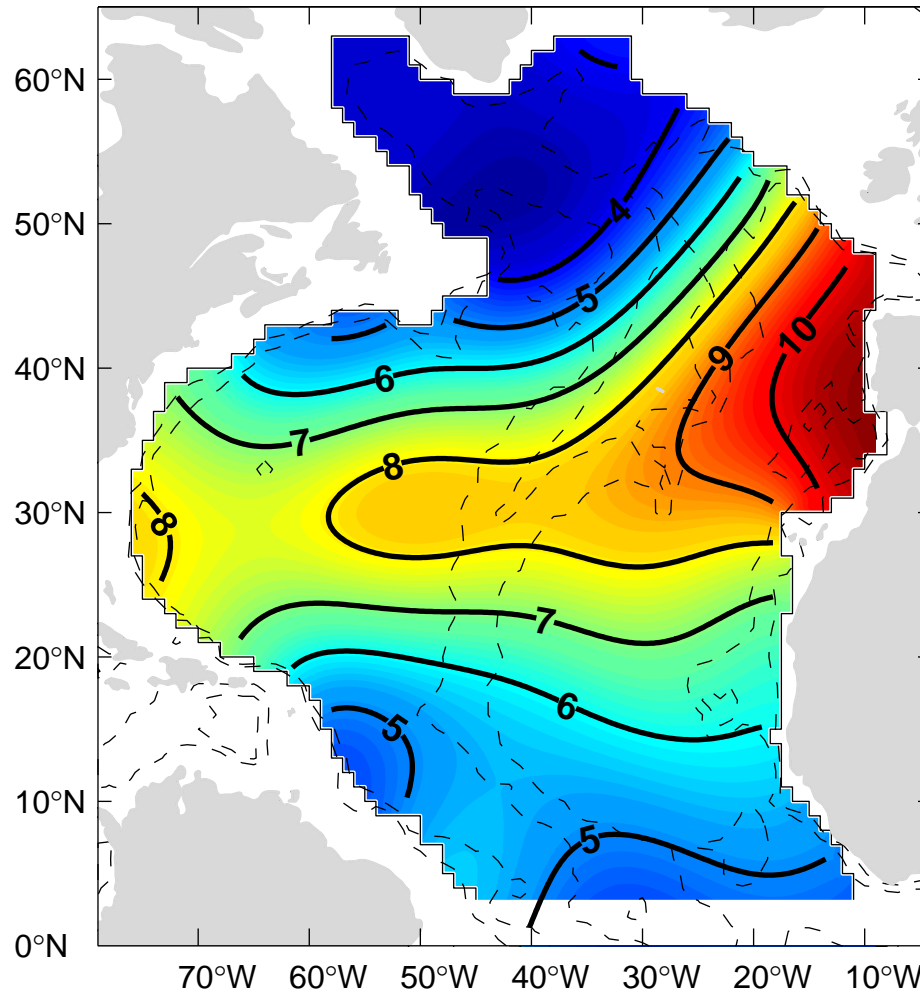
# Temperature ( $T_{\text{obs}} - \langle T \rangle_{\text{rec}}$ )



# Mid-Depth Temperature (950 m)

May 04

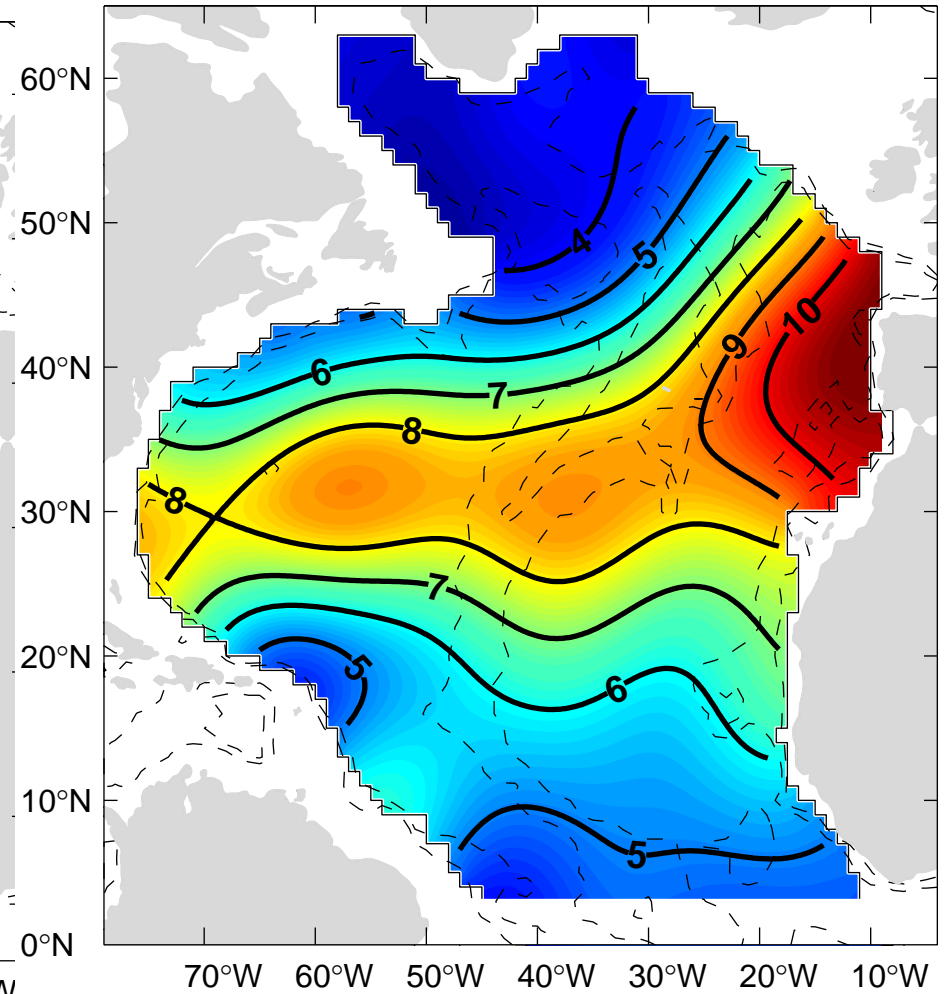
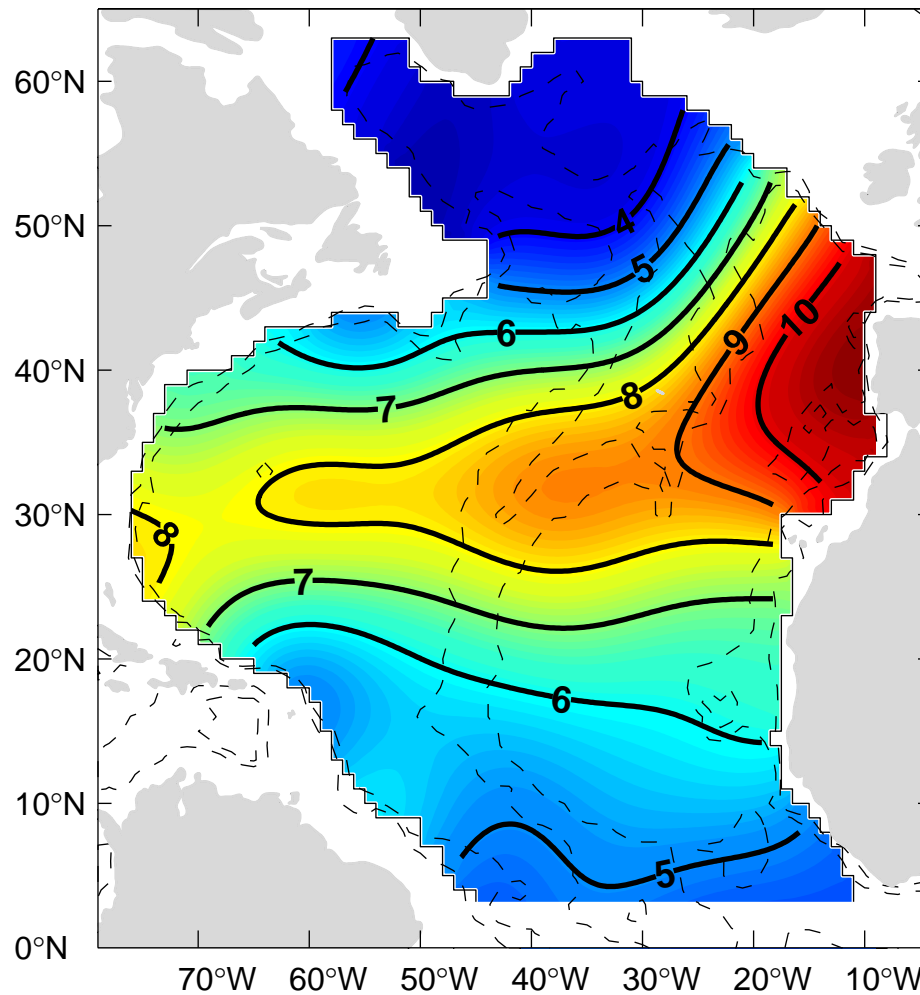
July 04



# Mid-Depth Temperature (950 m)

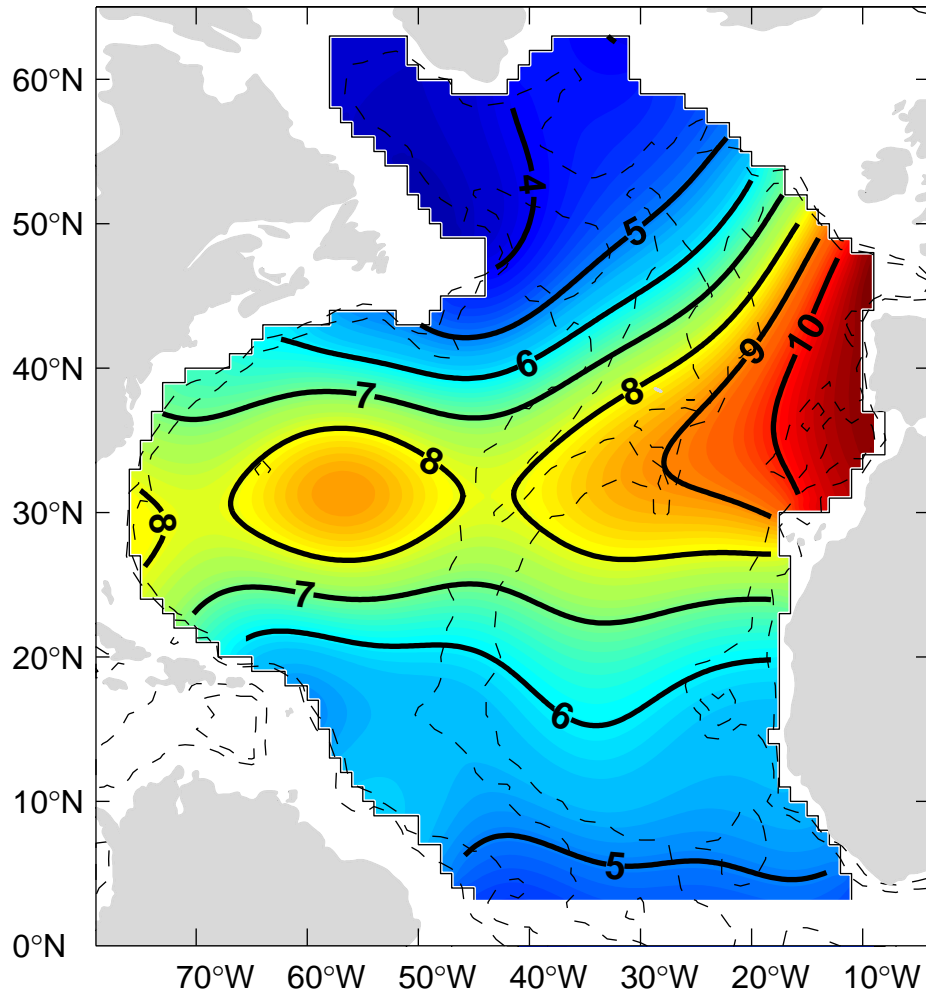
Sept 04

Nov 04

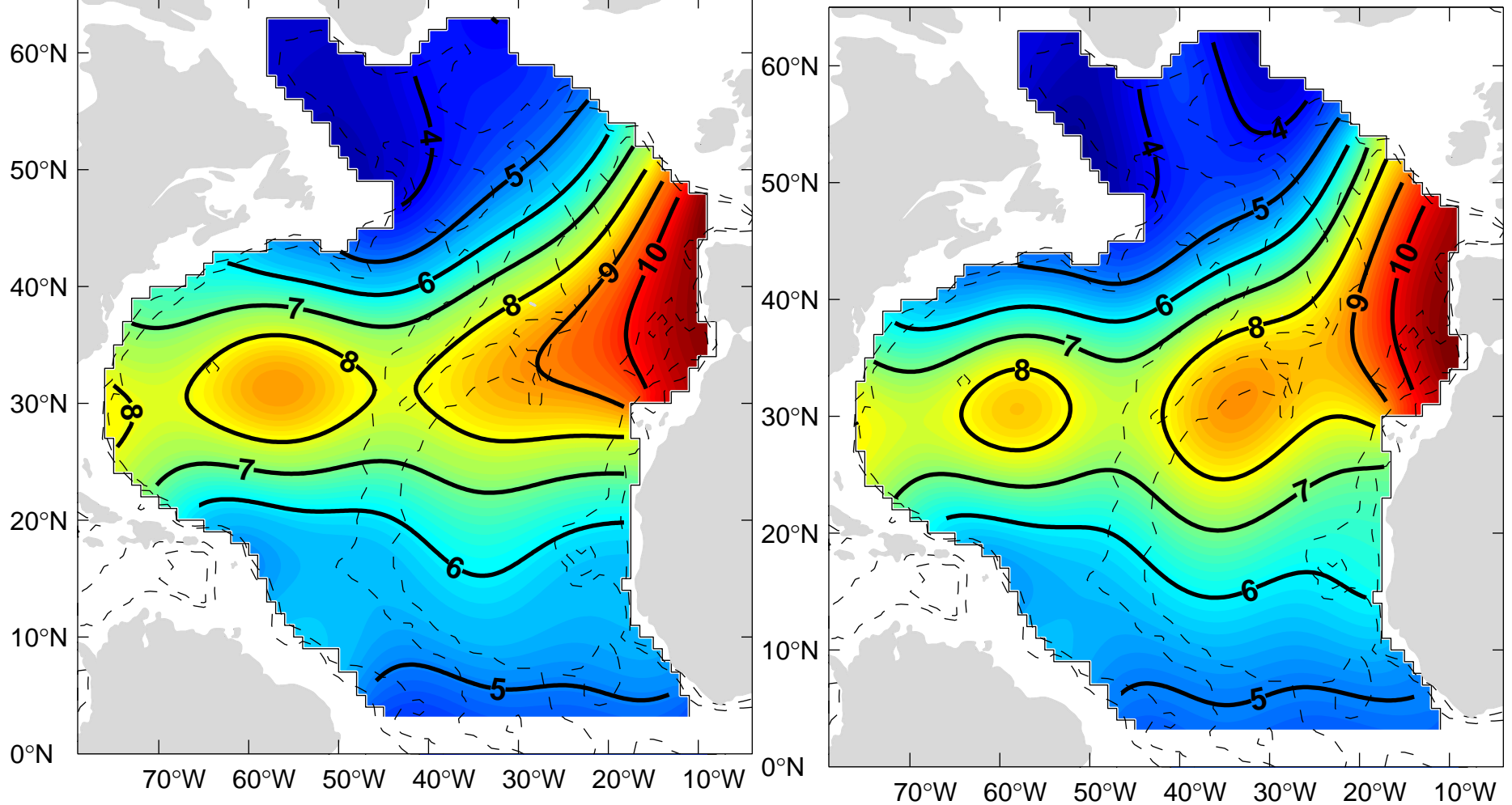


# Mid-Depth Temperature (950 m)

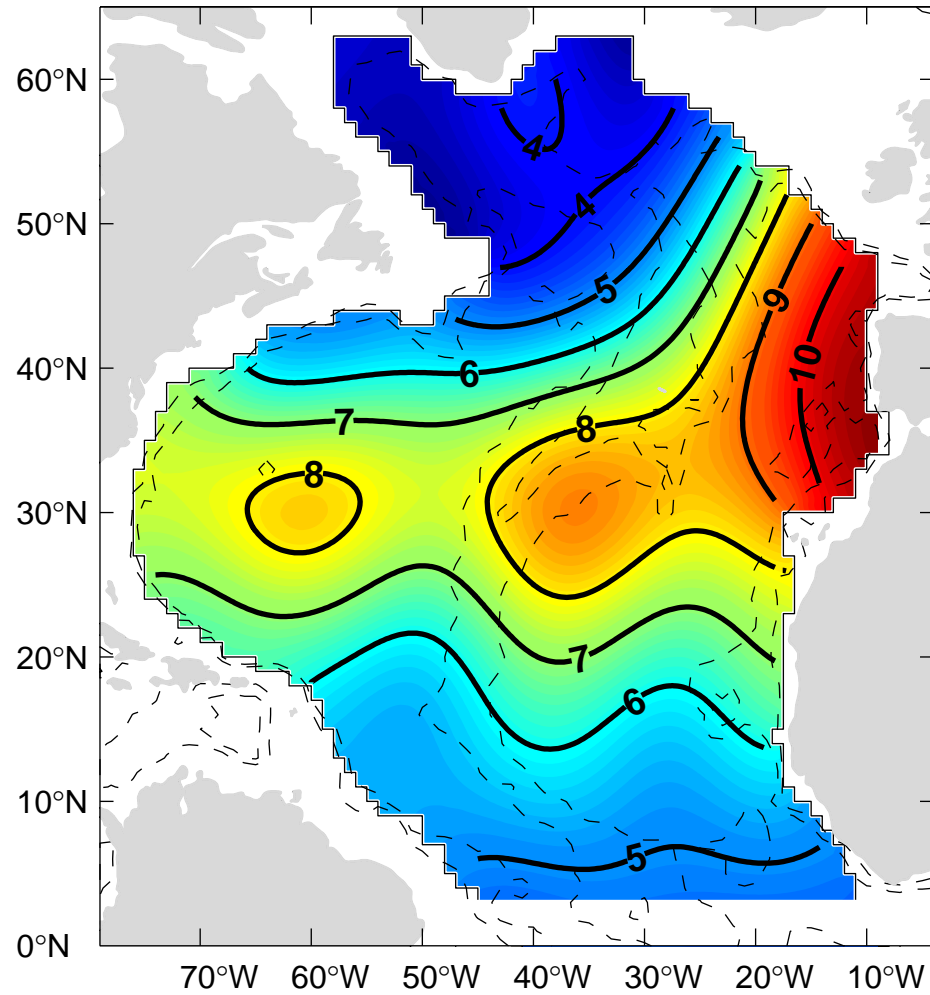
Jan 05



Mar 05



# Mid-Depth Temperature (950 m) May 05



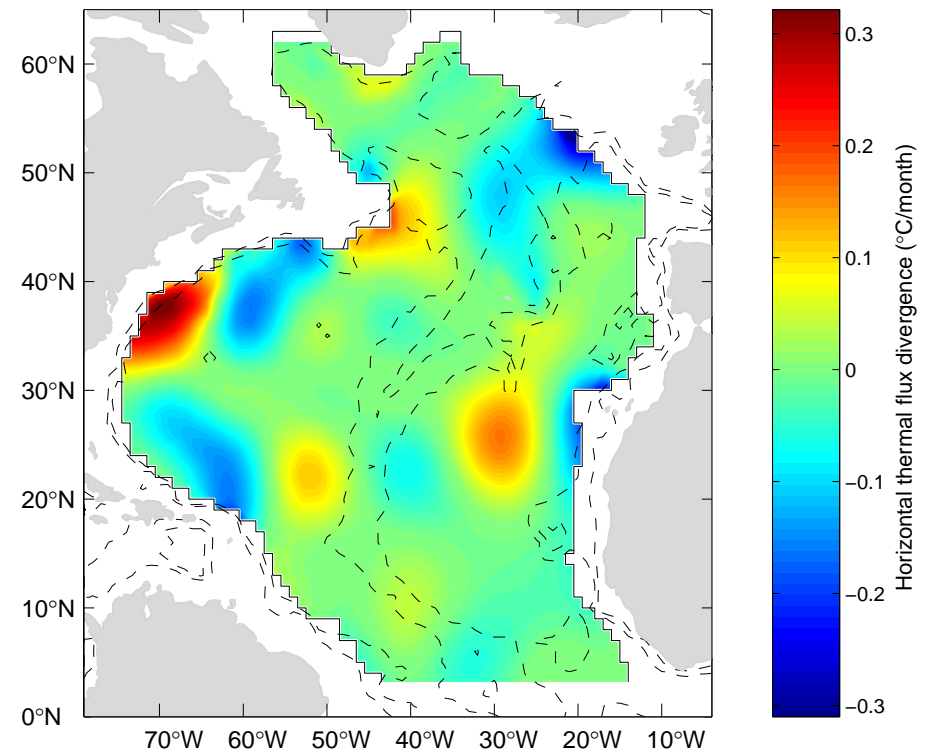
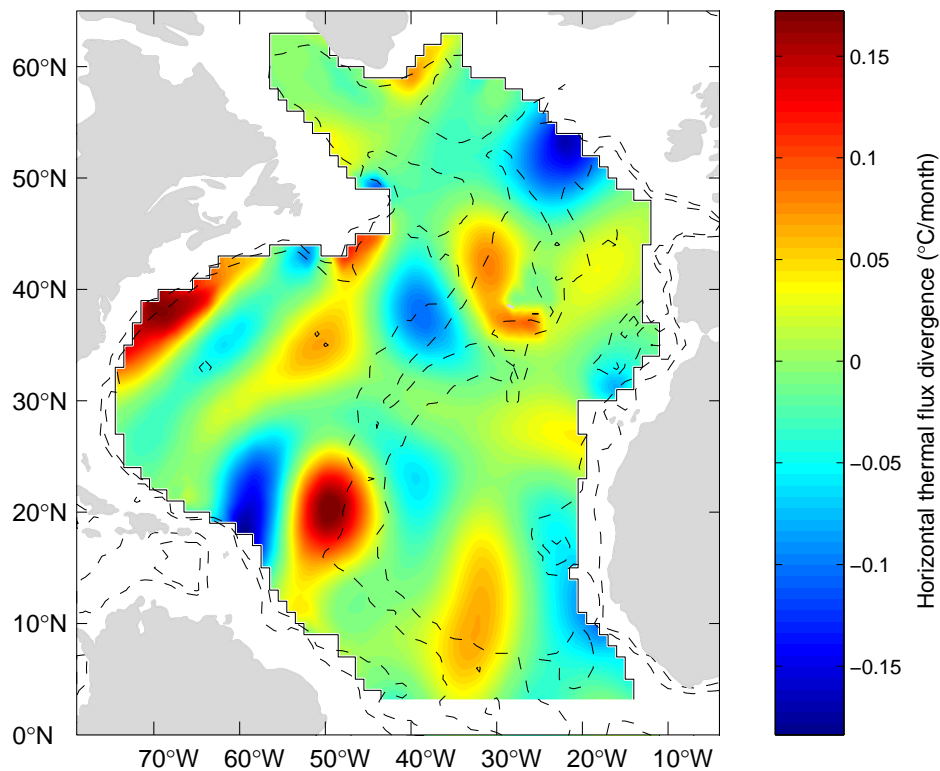


# Horizontal Heat Advection at 950 m

$$-u \frac{\partial T}{\partial x} - v \frac{\partial T}{\partial y}$$

June 04

Aug 04



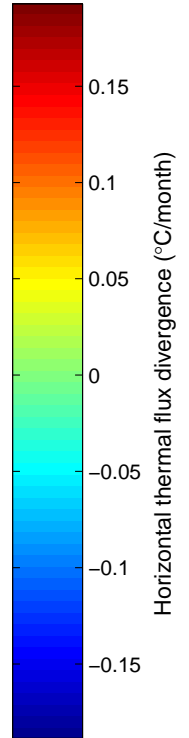
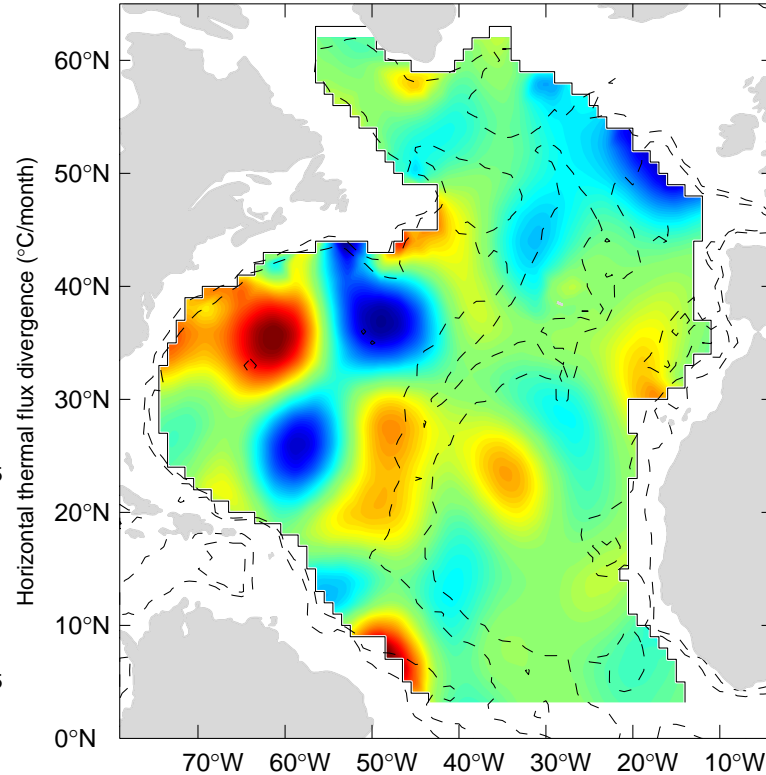
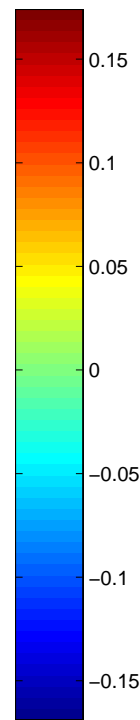
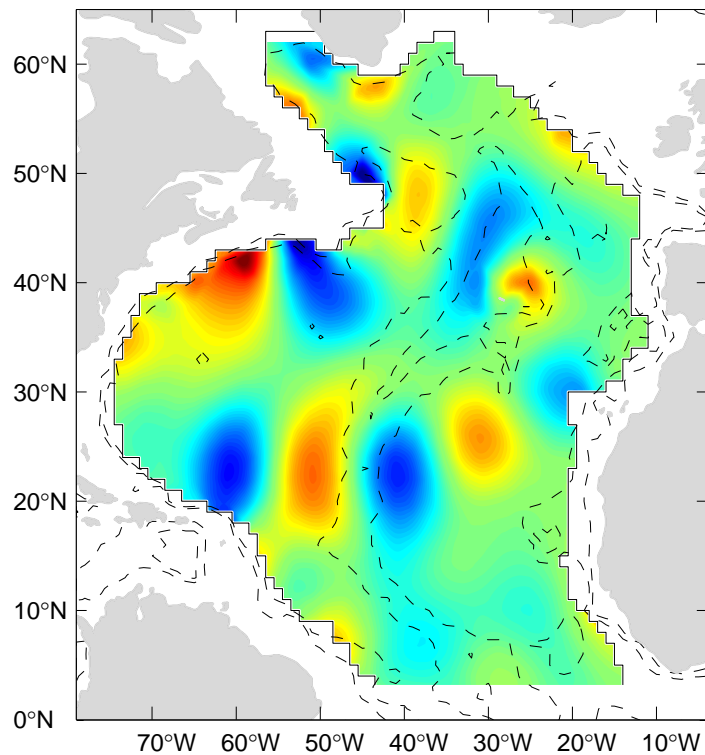


# Horizontal Heat Advection at 950 m

$$-u \frac{\partial T}{\partial x} - v \frac{\partial T}{\partial y}$$

Oct 04

Dec 04

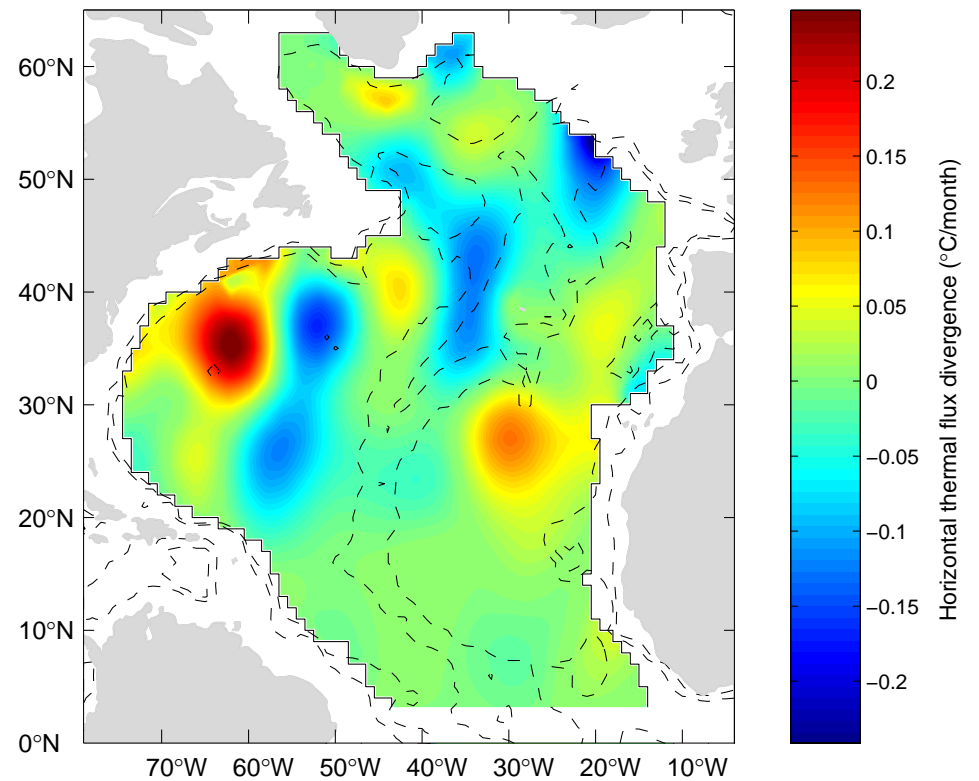
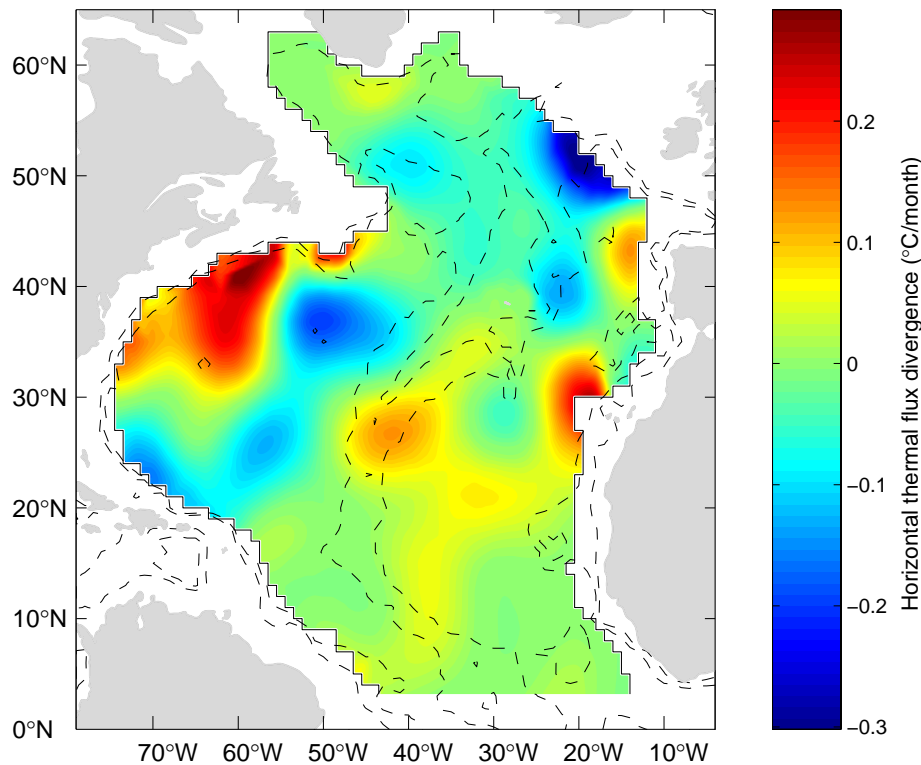


# Horizontal Heat Advection at 950 m

$$-u \frac{\partial T}{\partial x} - v \frac{\partial T}{\partial y}$$

Feb 05

Apr 05



# Conclusions

- Mid-depth North Atlantic Ocean circulation has rapid change (not steady!).
- The circulation variability is around 5 cm/s.
- The maximum horizontal temperature advection is around 0.25°/mon.
- The velocity and temperature perturbations are not normally distributed.
- OSD is a useful tool for processing real-time velocity data with short duration and limited-area sampling especially the ARGO data.