

# Predictability of Japan / East Sea (JES) System to Uncertain Initial / Lateral Boundary Conditions and Surface Winds

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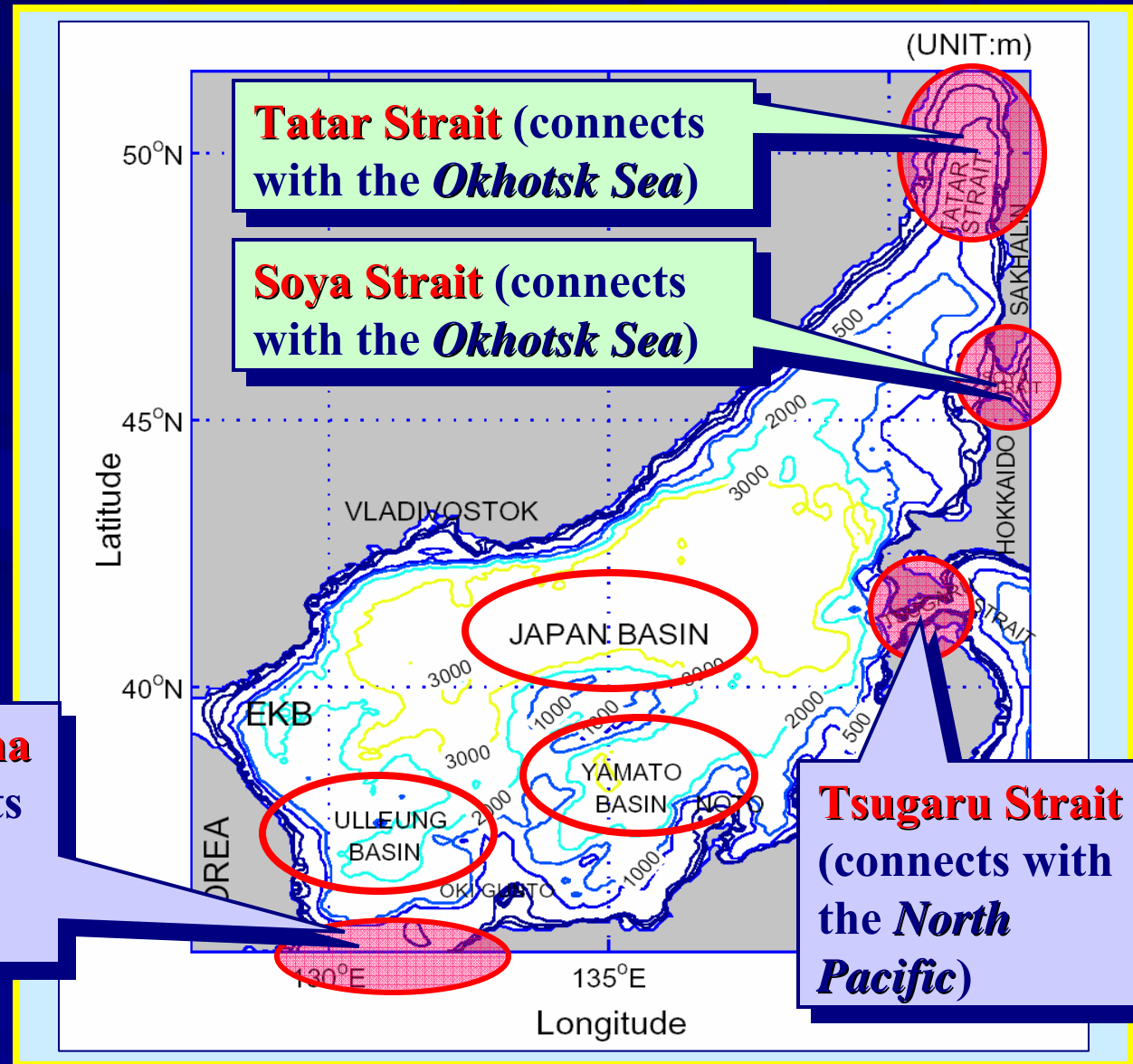
# Outline

- **Introduction**
- **Experimental design**
- **Statistical analysis methods**
- **Results**
- **Conclusions**

# Introduction

- Three Difficulties
- JES Geography & bottom topography
- Princeton Ocean Model

**Korea/Tsushima Strait** (connects with the *North Pacific*)



# Introduction

- **Three Difficulties**
- JES  
Geography &  
bottom  
topography
- Princeton  
Ocean Model

It is important for us to investigate **the response of a ocean model to these uncertainties.**

Uncertainty  
of the  
*initial  
velocity  
condition*

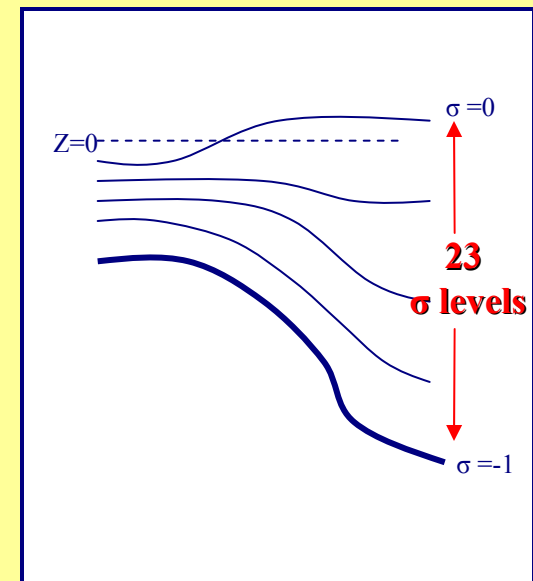
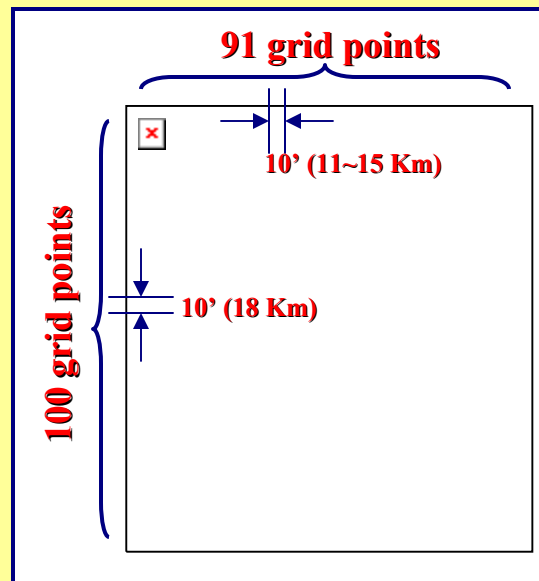
Uncertainty  
of the  
*open  
boundary  
condition*

Uncertainty  
of the  
*atmospheric  
forcing*

# Introduction

- Three Difficulties
- JES Geography & bottom topography
- Princeton Ocean Model
  - General information
  - Surface & lateral boundary forcing
  - Two step initialization

**POM : a time-dependent, primitive equation model rendered on a three-dimensional grid that includes realistic topography and a free surface.**



# Introduction

- Three Difficulties
- JES Geography & bottom topography
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  - General information
  - Surface & lateral boundary forcing
  - Two step initialization

- Wind stress at each time step is interpolated from monthly mean climatological wind stress from COADS (1945-1989).

- Volume transports at open boundaries are specified from historical data.

<i>Month</i>	<i>Feb</i>	<i>Apr</i>	<i>Jun.</i>	<i>Aug</i>	<i>Oct</i>	<i>Dec</i>
Tatar strait (inflow)	0.05	0.05	0.05	0.05	0.05	0.05
Soya strait (outflow)	-0.1	-0.1	-0.4	-0.6	-0.7	-0.4
Tsugaru strait (outflow)	-0.25	-0.35	-0.85	-1.45	-1.55	-1.05
Tsushima strait (inflow)	0.3	0.4	1.2	2.0	2.2	1.4

Unit: Sv, 1 Sv =  $10^6 \text{ m}^3\text{s}^{-1}$

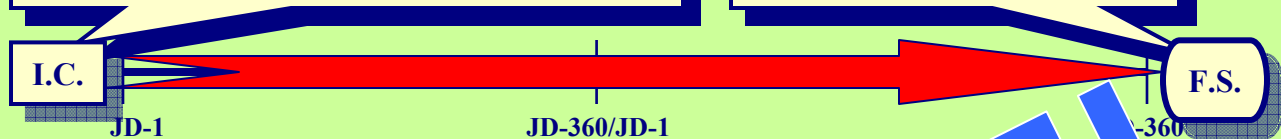
# Introduction

- Three Difficulties
- JES Geography & bottom topography
- Princeton Ocean Model
  - General information
  - Surface & lateral boundary forcing
  - Two step initialization

## *The first step: Diagnostic Run*

- From **zero velocity** and  $T_c$  and  $S_c$  fields (Levitus).
- **Wind stress** from COADS data & without flux forcing.

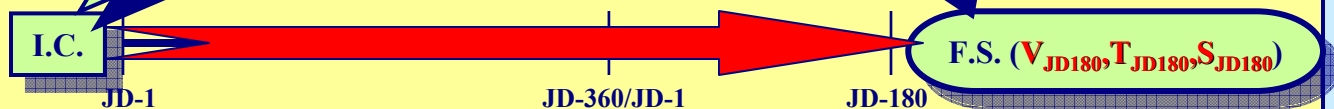
The final states are taken as **initial conditions** for the second step



## *The second step: Prognostic Run*

- From **the final states** of the first step.
- **Wind stress** from COADS data & with flux forcing.

The final states are taken as **standard initial conditions** ( $V_0, T_0, S_0$ ) for the experiments.



# Temporal Variation of the Kinetic Energy During the First Stage

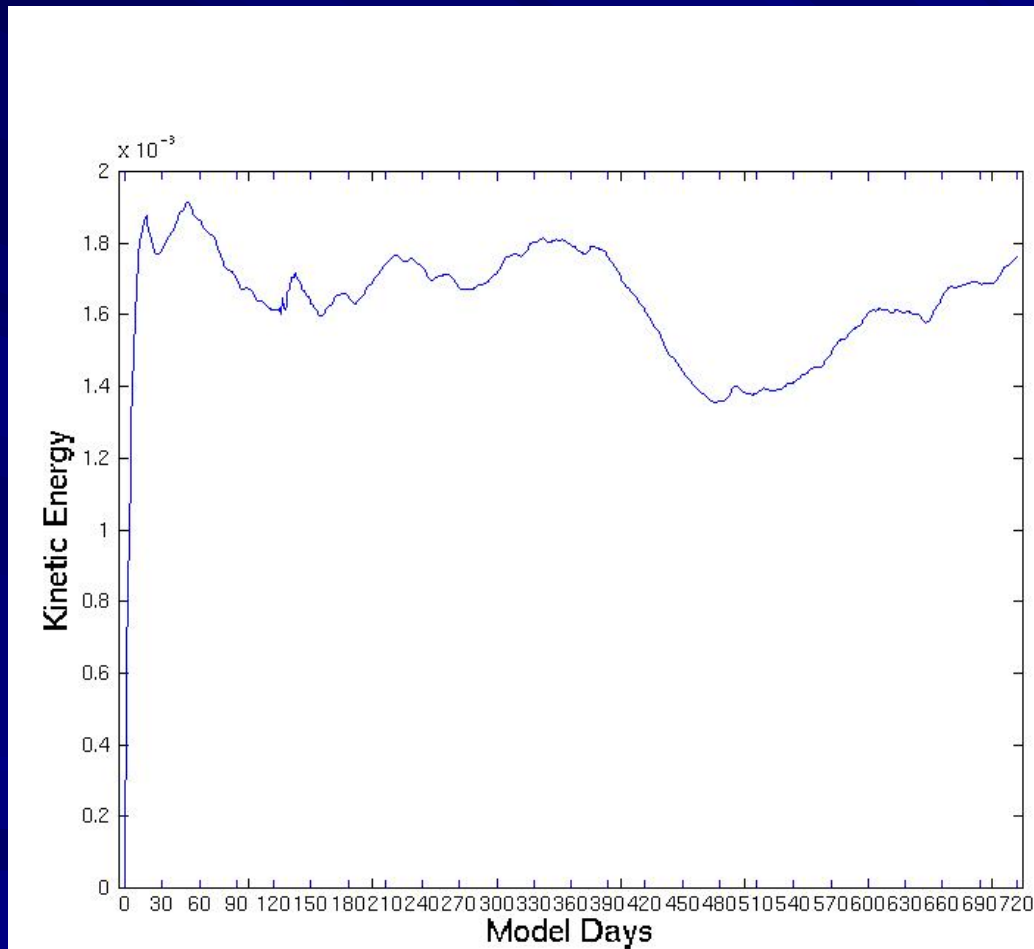


fig8



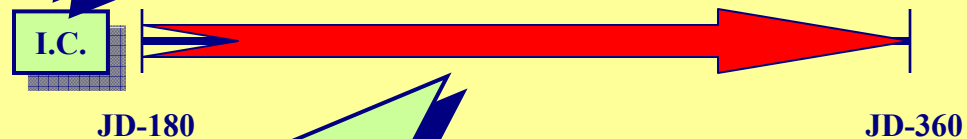
# Experimental Design

<i>Experimen t</i>	<i>Property</i>
0	<u>Control run</u>
1	Uncertain <u>velocity initialization processes</u>
2	
3	
4	
5	Uncertain <u>wind stress</u>
6	
7	Uncertain <u>lateral boundary transport</u>
8	
9	<u>Combination of uncertainty</u>
10	
11	

# Experimental Design

- Control Run
- Uncertain Initial Conditions
- Uncertain Wind Forcing
- Uncertain Lateral Transport
- Combined Uncertainty

- From the standard initial conditions  $(V_0 = V_{JD180}, T_0 = T_{JD180}, S_0 = S_{JD180})$ .
- Lateral transport from historical data and Wind stress from COADS data & with flux forcing.



The simulated **temperature** and **salinity** fields and **circulation pattern** are **consistent with observational studies** (*Chu et al. 2003*).

# Experimental Design

- Control Run
- Uncertain Initial Conditions
- Uncertain Wind Forcing
- Uncertain Lateral Transport
- Combined Uncertainty

<i>Experiment</i>	<i>Initial Conditions</i>	<i>Wind Forcing</i>	<i>Lateral Boundary Conditions</i>
1	$V_0 = 0$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Same as Run-0	Same as Run-0
2	$V_0 = V_{30D}^{(Diag)}$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Same as Run-0	Same as Run-0
3	$V_0 = V_{60D}^{(Diag)}$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Same as Run-0	Same as Run-0
4	$V_0 = V_{90D}^{(Diag)}$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Same as Run-0	Same as Run-0

# Experimental Design

- Control Run
- Uncertain Initial Conditions
- **Uncertain Wind Forcing**
- Uncertain Lateral Transport
- Combined Uncertainty

<i>Experiment</i>	<i>Initial Conditions</i>	<i>Wind Forcing</i>	<i>Lateral Boundary Conditions</i>
5	Same as Run-0	Adding Gaussian random noise with zero mean and <b>0.5 m/s</b> noise intensity	Same as Run-0
6	Same as Run-0	Adding Gaussian random noise with zero mean and <b>1.0 m/s</b> noise intensity	Same as Run-0

# Experimental Design

- Control Run
- Uncertain Initial Conditions
- Uncertain Wind Forcing
- Uncertain Lateral Transport
- Combined Uncertainty

<i>Experiment</i>	<i>Initial Conditions</i>	<i>Wind Forcing</i>	<i>Lateral Boundary Conditions</i>
7	Same as Run-0	Same as Run-0	Adding Gaussian random noise with the zero mean and noise intensity being <b>5%</b> of the transport (control run)
8	Same as Run-0	Same as Run-0	Adding Gaussian random noise with the zero mean and noise intensity being <b>10%</b> of the transport (control run)

# Experimental Design

- Control Run
- Uncertain Initial Conditions
- Uncertain Wind Forcing
- Uncertain Lateral Transport
- Combined Uncertainty

<i>Experiment</i>	<i>Initial conditions</i>	<i>Wind forcing</i>	<i>Lateral Boundary Conditions</i>
9	$V_0 = V_{30D}^{(Diag)}$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Adding Gaussian random noise with <b>1.0 m/s</b> noise intensity	Same as Run-0
10	$V_0 = V_{30D}^{(Diag)}$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Same as Run-0	Adding Gaussian random noise with noise intensity being <b>10%</b> of the transport (control run)
11	$V_0 = V_{30D}^{(Diag)}$ , $T_0 = T_{JD180}$ , $S_0 = S_{JD180}$	Adding Gaussian random noise with <b>1.0 m/s</b> noise intensity	Adding Gaussian random noise with noise intensity being <b>10%</b> of the transport (control run)

# Statistical Analysis Methods

**Model Error :**

$$\Delta\psi(x, y, z, t) = \psi_c(x, y, z, t) - \psi_e(x, y, z, t)$$

**Root Mean  
Square Error  
(RMSE) :**

$$RMSE(z, t) = \sqrt{\frac{1}{M_y \times M_x} \sum_{j=1}^{M_y} \sum_{i=1}^{M_x} [\Delta\psi_u(x_i, y_j, z, t)^2 + \Delta\psi_v(x_i, y_j, z, t)^2]}$$

**Relative Root  
Mean Square  
Error (RRMSE) :**

$$RRMSE(z, t) = \frac{\sqrt{\sum_{j=1}^{M_y} \sum_{i=1}^{M_x} [\Delta\psi_u(x_i, y_j, z, t)^2 + \Delta\psi_v(x_i, y_j, z, t)^2]}}{\sqrt{\sum_{j=1}^{M_y} \sum_{i=1}^{M_x} [\psi_{c_u}(x_i, y_j, z, t)^2 + \psi_{c_v}(x_i, y_j, z, t)^2]}}$$

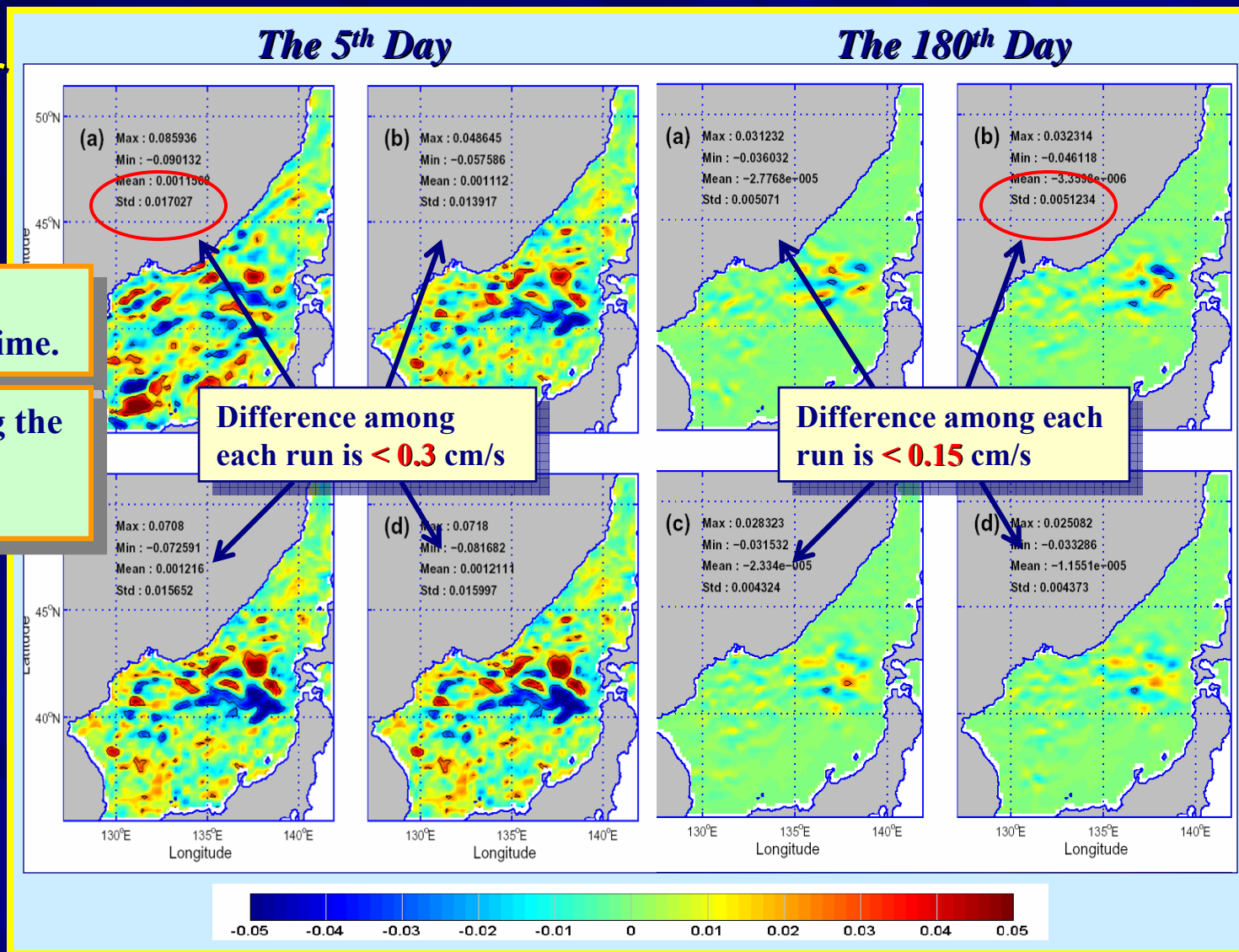
# Model Errors Due To Initial Conditions

- Model Error Distribution
  - Horizontal distributio

Model error is decreasing with time.

Difference among the four runs is not significant.

1	$V_0 = 0$ $T_0 = T_{JD180}$ $S_0 = S_{JD180}$
2	$V_0 = V_{30D}^{(Diag)}$ $T_0 = T_{JD180}$ $S_0 = S_{JD180}$
3	$V_0 = V_{60D}^{(Diag)}$ $T_0 = T_{JD180}$ $S_0 = S_{JD180}$
4	$V_0 = V_{90D}^{(Diag)}$ $T_0 = T_{JD180}$ $S_0 = S_{JD180}$





# Model Errors Due To Initial Conditions

## Model Error Distribution

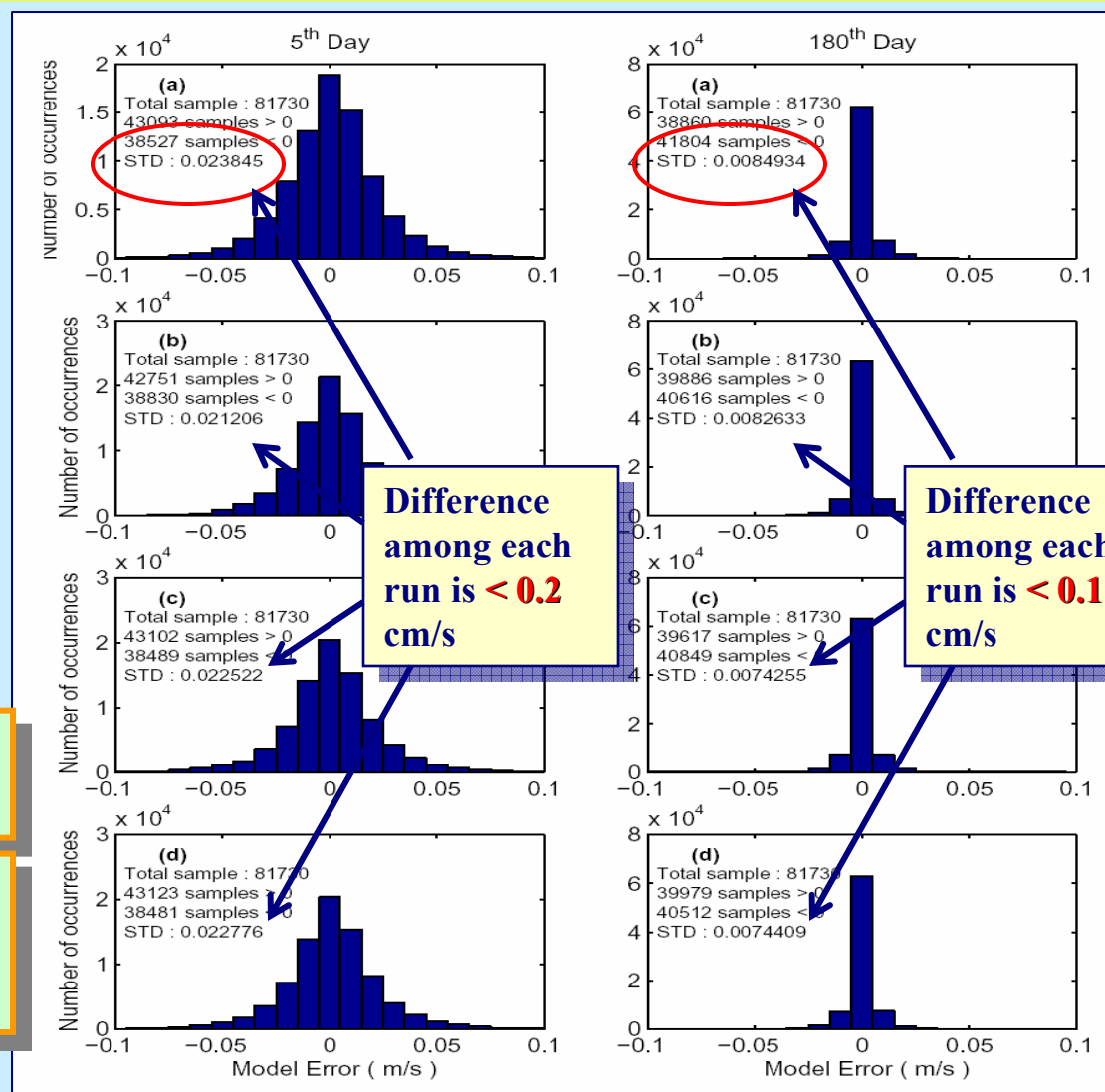
- Horizontal distribution

- Histogram

## Relative Root Mean Square Error

Model error is decreasing with time.

Difference among the four runs is not significant.

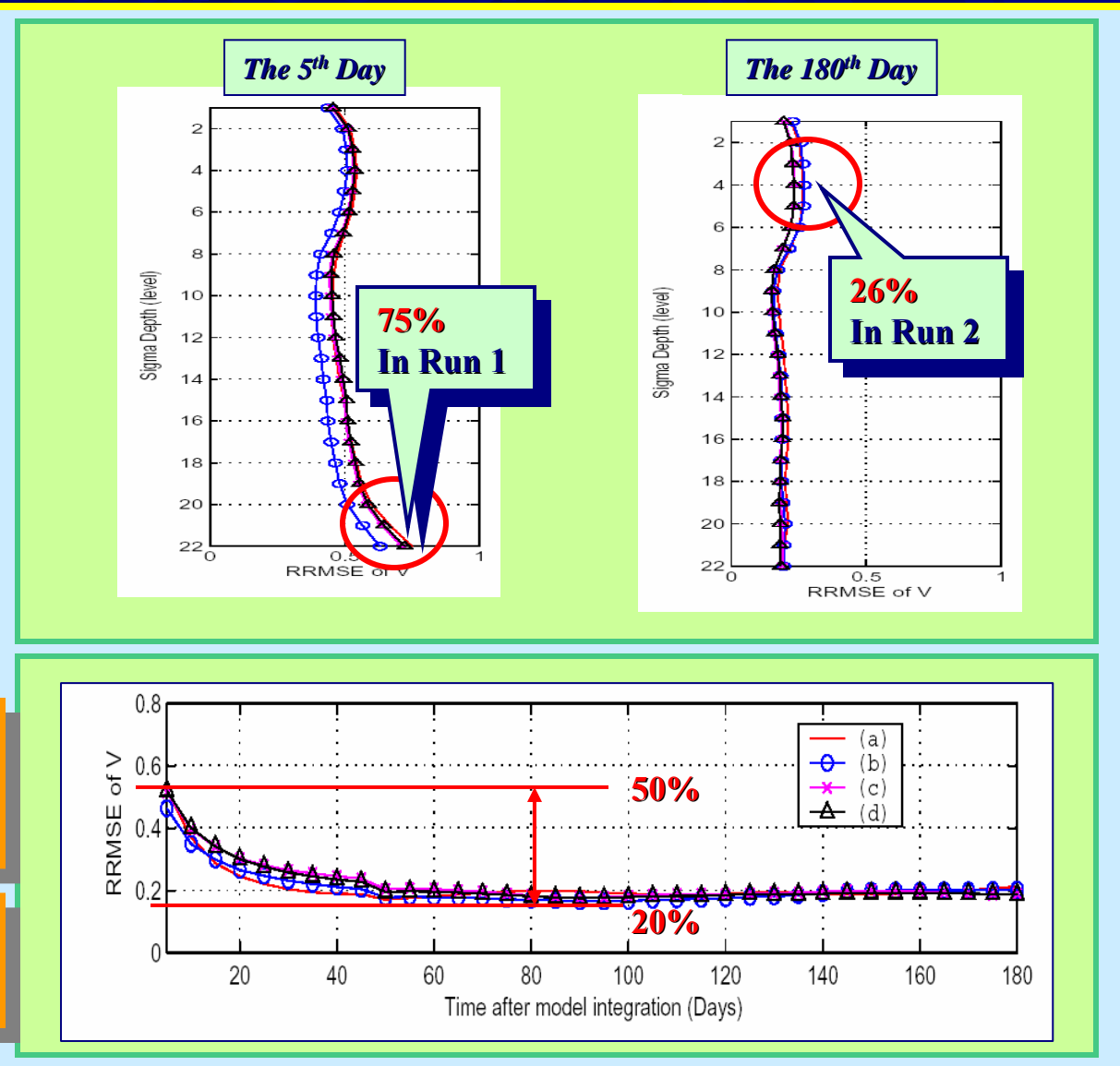


# Model Errors Due To Initial Conditions

- Model Error Distribution
- Relative Root Mean Square Error (RRMSE)
  - Vertical Variation
  - Temporal

Effects to the horizontal velocity prediction are quite significant.

No obvious difference among these four runs.



# Model Errors Due To Wind Forcing

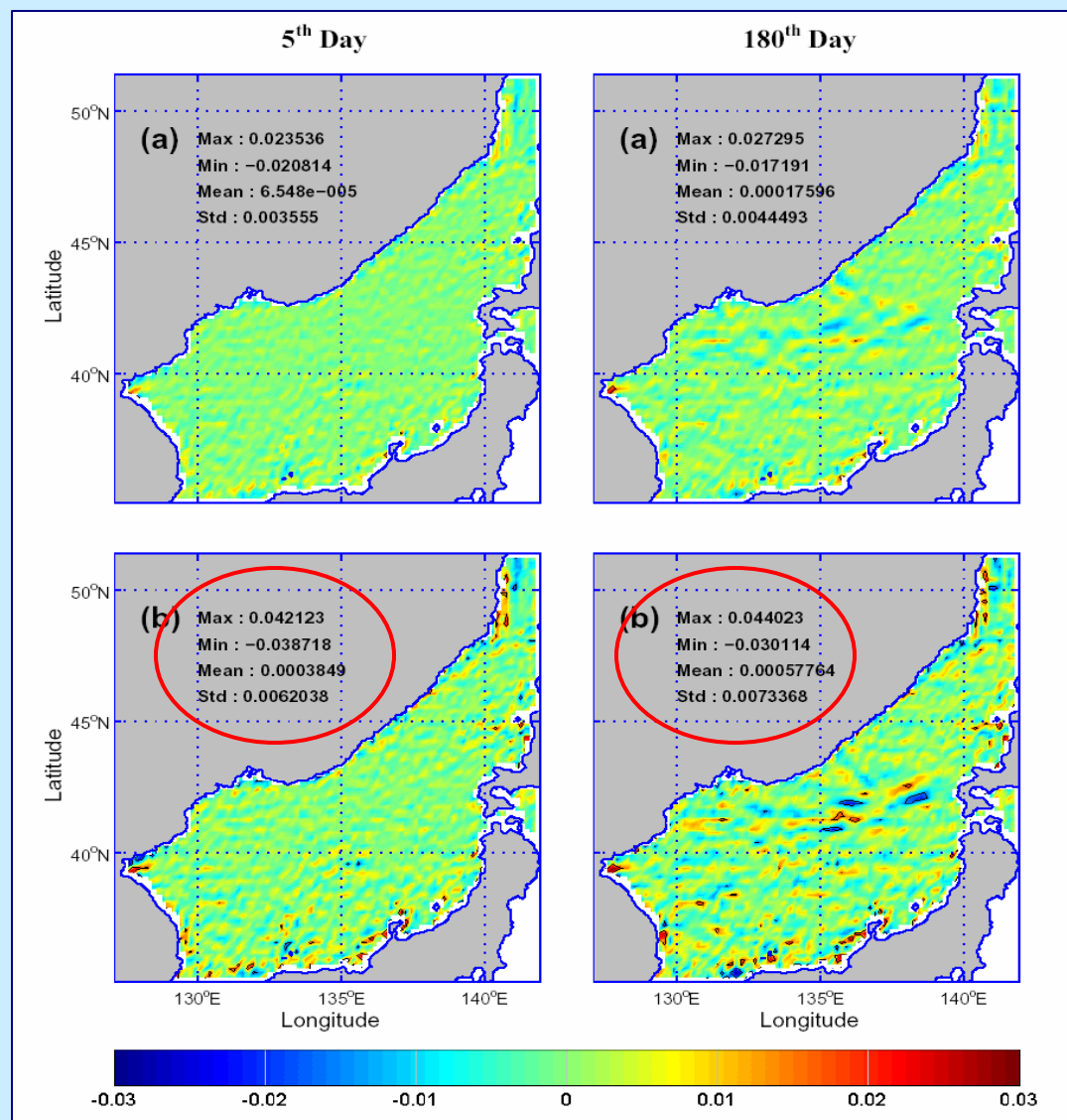
## Model Error Distribution

- Horizontal distributio

Larger model error in Run 6.

Model error is increasing with time.

Experiment	Wind Forcing
5	Adding Gaussian random noise with zero mean and <b>0.5 m/s</b> noise intensity
6	Adding Gaussian random noise with zero mean and <b>1.0 m/s</b> noise intensity



# Model Errors Due To Wind Forcing

## Model Error Distribution

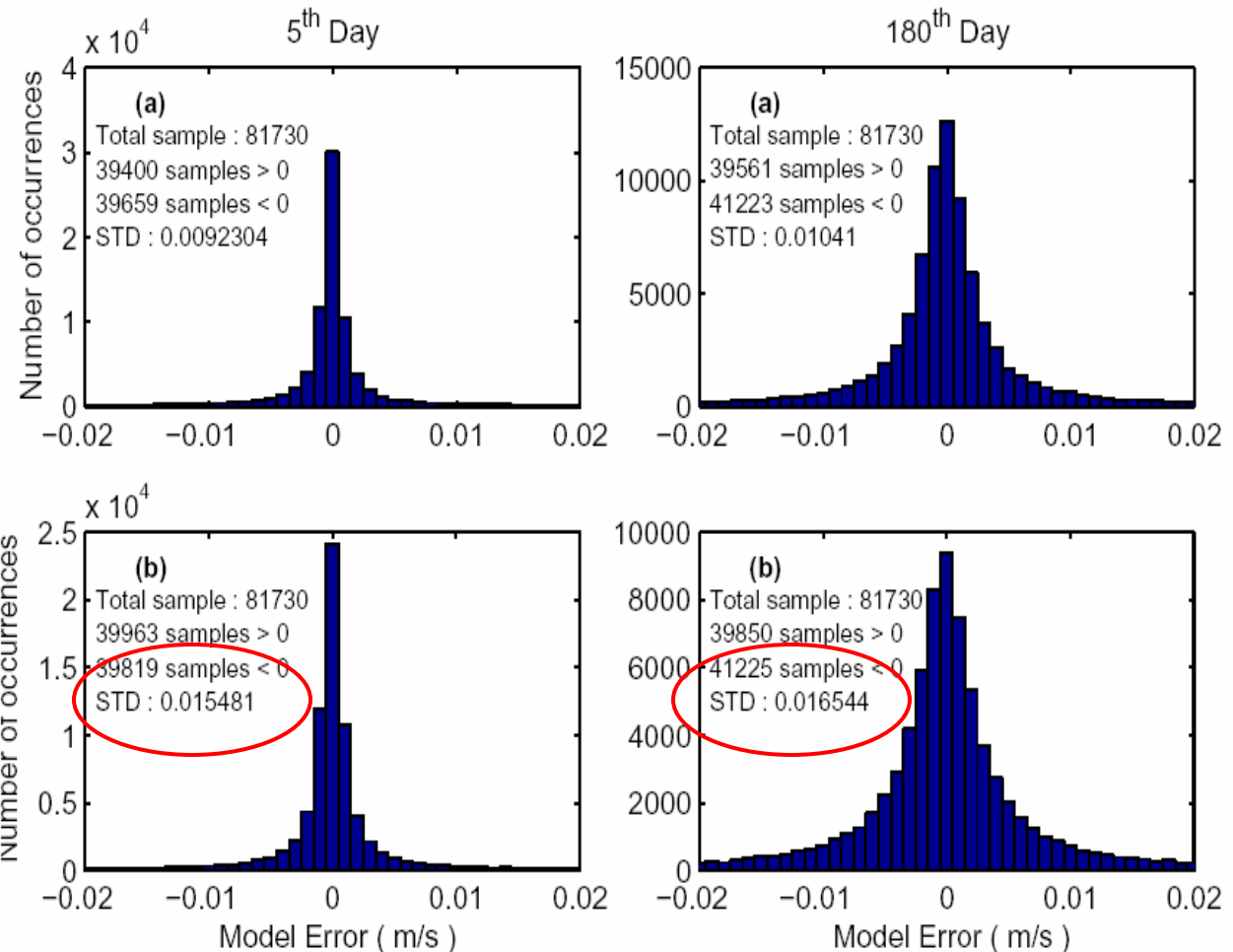
- Horizontal distribution

– Histogram

## Relative Root Mean Square Error

Larger model error in Run 6.

Model error is increasing with time.

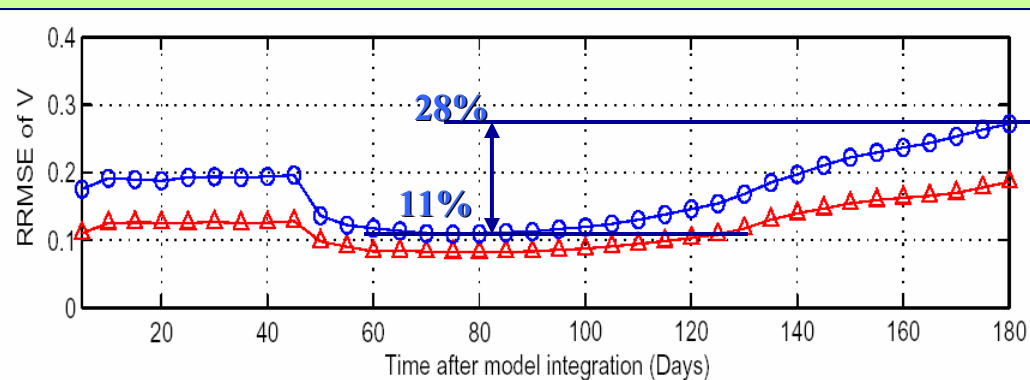
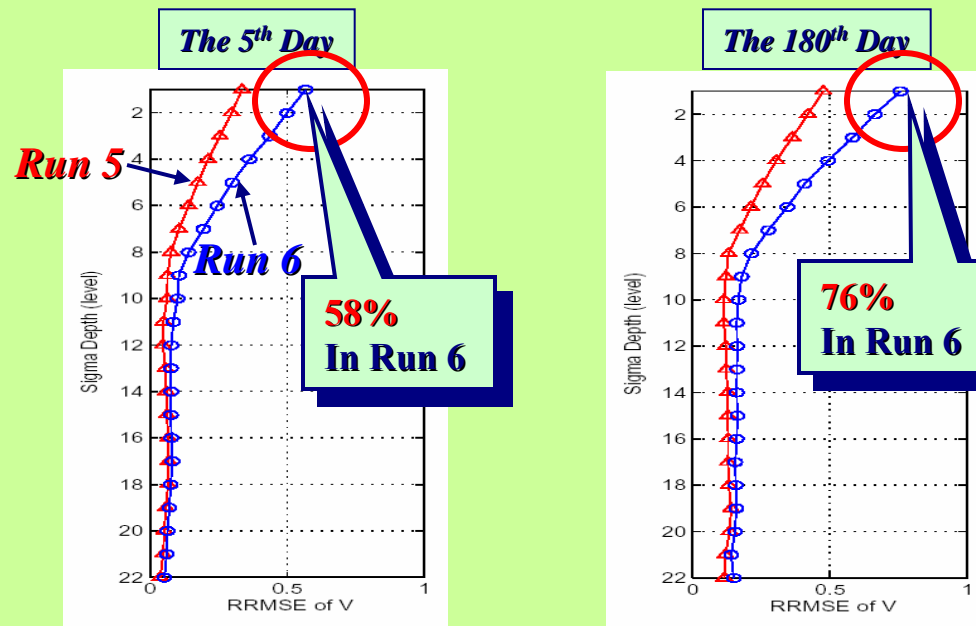


# Model Errors Due To Wind Forcing

- Model Error Distribution
- Relative Root Mean Square Error (RRMSE)
  - Vertical Variation
  - Temporal

Larger model error in Run 6.

Effects to the horizontal velocity prediction are quite significant.



# Model Errors Due To Open Boundary Conditions

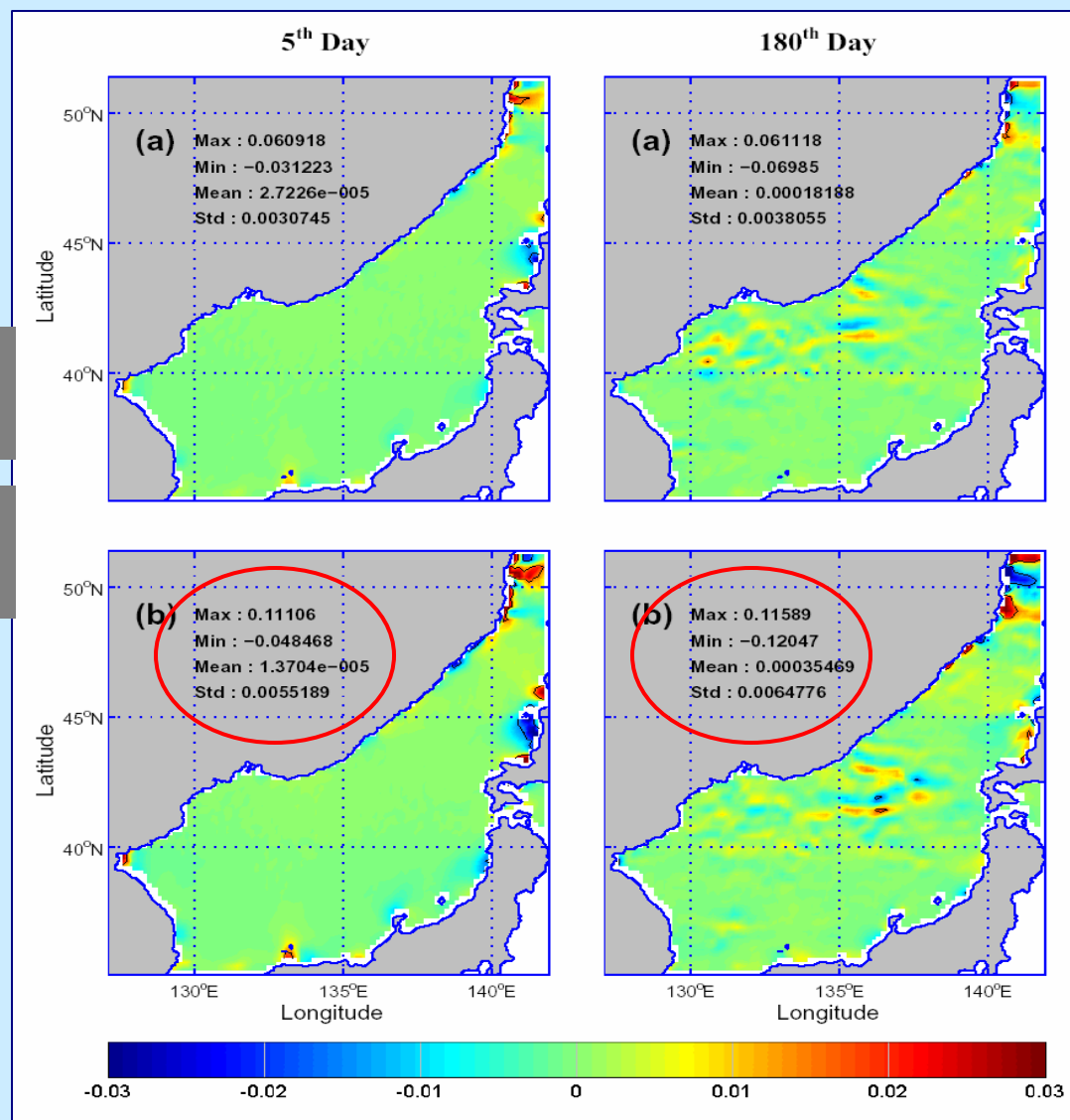
## Model Error Distribution

- Horizontal distributio

Larger model error in Run 8.

Model error is increasing with time.

Experiment	Lateral Boundary Conditions
7	Adding Gaussian random noise with the zero mean and noise intensity being <b>5%</b> of the transport (control run)
8	Adding Gaussian random noise with the zero mean and noise intensity being <b>10%</b> of the transport (control



# Model Errors Due To Open Boundary Conditions

## ■ Model Error Distribution

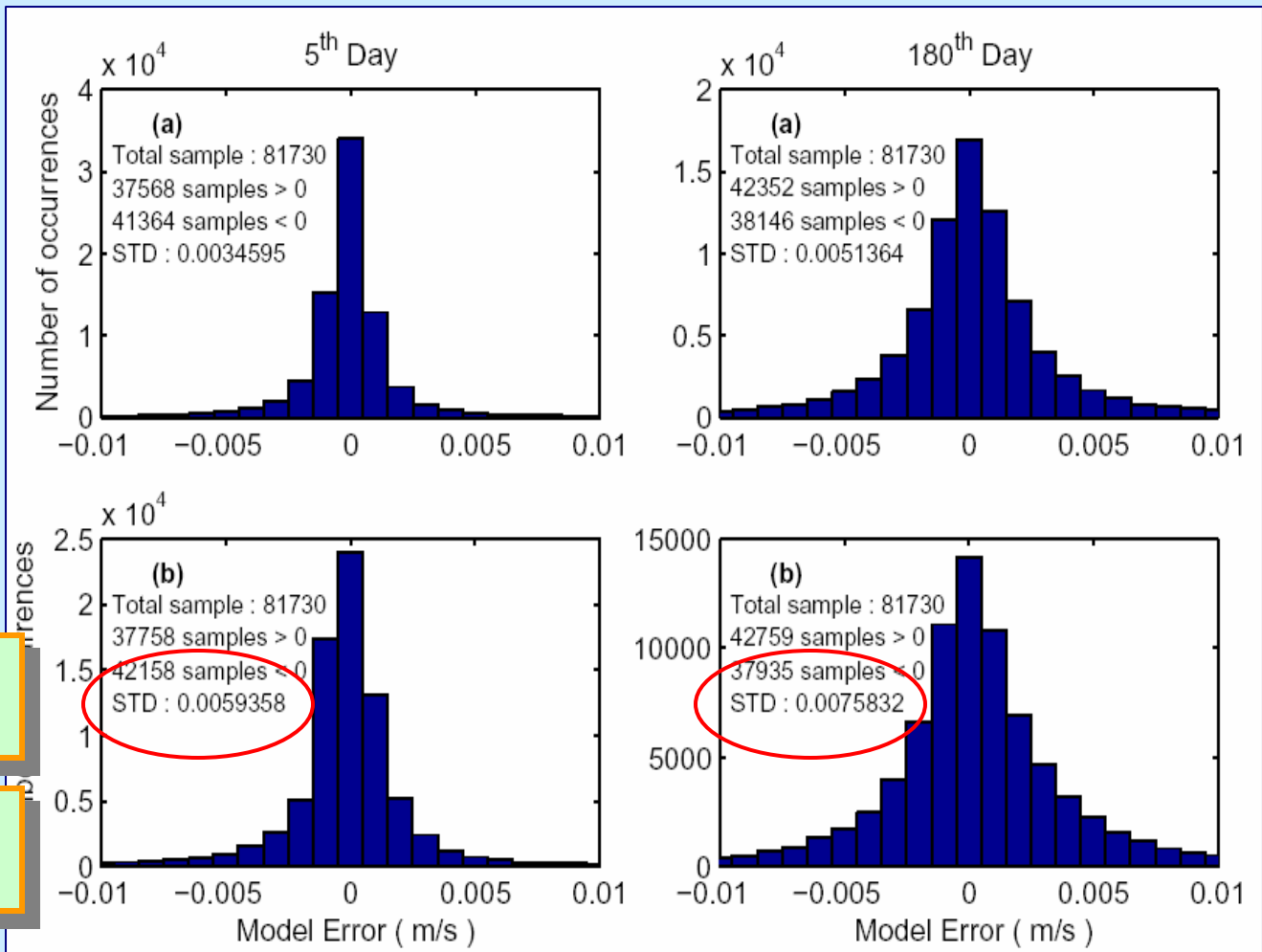
- Horizontal distribution

– Histogram

## ■ Relative Root Mean Square Error

Larger model error in Run 8.

Model error is increasing with time.

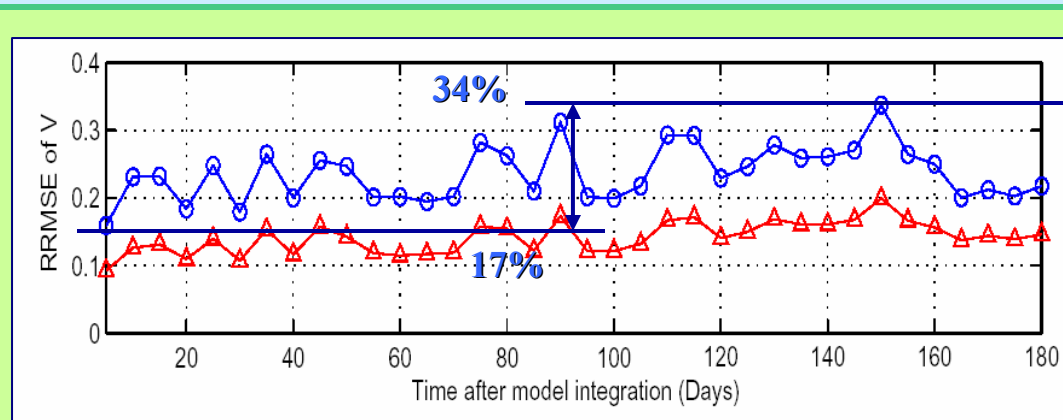
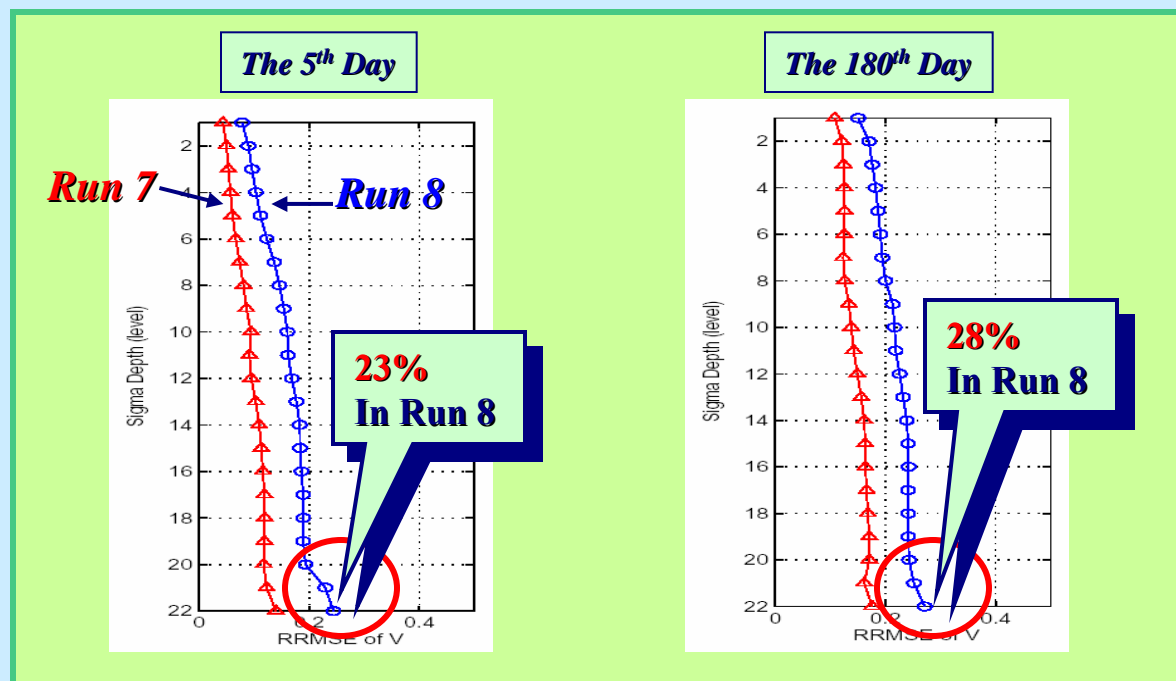


# Model Errors Due To Open Boundary Conditions

- Model Error Distribution
- Relative Root Mean Square Error (RRMSE)
  - Vertical Variation
  - Temporal

Larger model error in Run 8.

Effects to the horizontal velocity prediction are quite significant.





# Model Errors Due To Combined Uncertainty

## Model Error Distribution

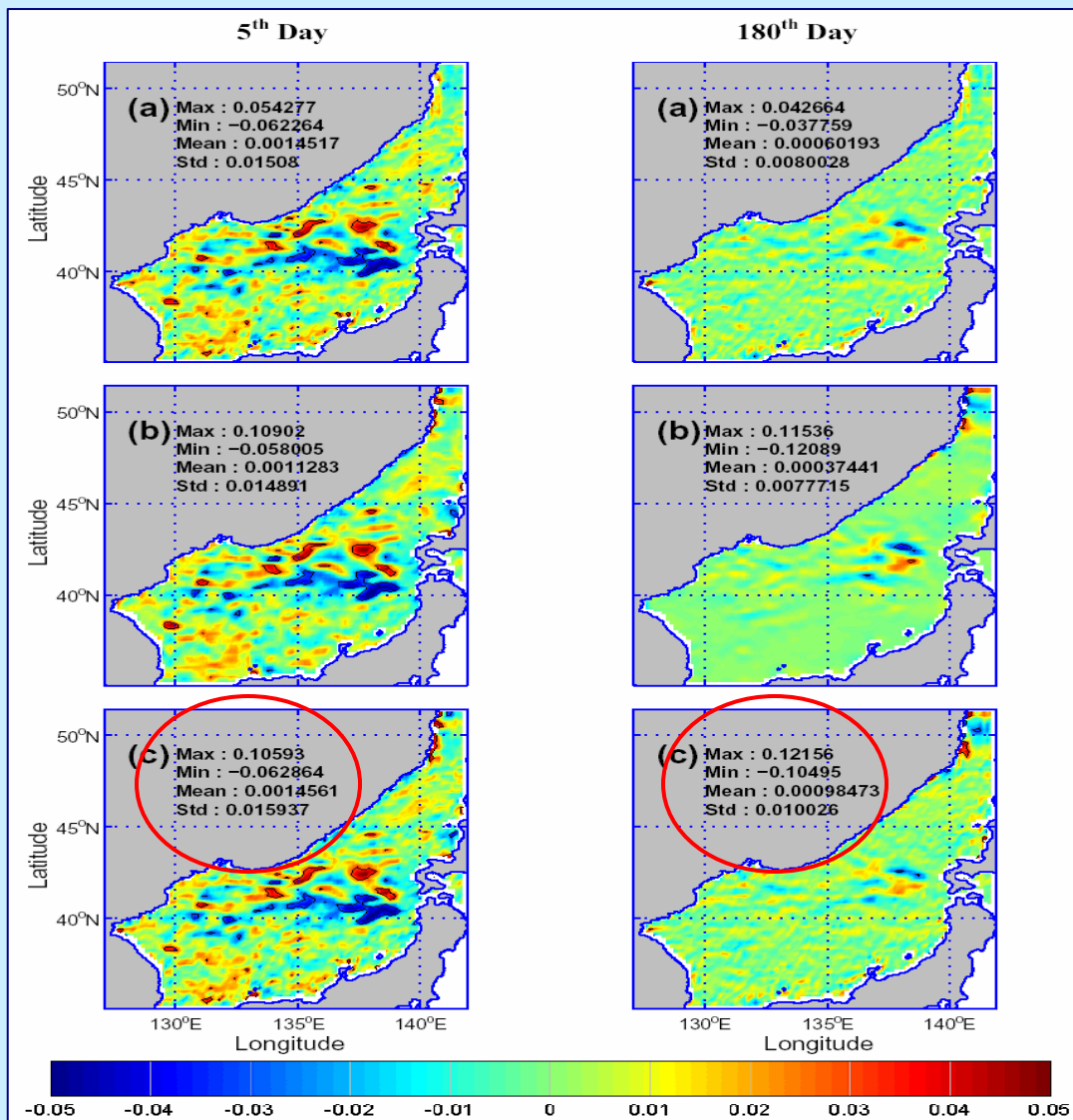
- Horizontal distribution

Larger model error in Run 11.

## Relationship

Model error is decreasing with time.

Experiment	Initial conditions	forcing	Conditions
9	$V_0 = V_{30D}^{(Diag)}$ $T_0 = T_{JD180}$ $S_0 = S_{JD180}$	with <b>1.0 m/s</b> noise intensity	Same as Run-0
10	$V_0 = V_{30D}^{(Diag)}$ $T_0 = T_{JD180}$ $S_0 = S_{JD180}$	Same as Run-0	with noise intensity being <b>10%</b> of the transport
11	$T_0 = T_{JD180}$ $S_0 = S_{JD180}$	with <b>1.0 m/s</b> noise intensity	with noise intensity being <b>10%</b> of the



# Model Errors Due To Combined Uncertainty

## Model Error Distribution

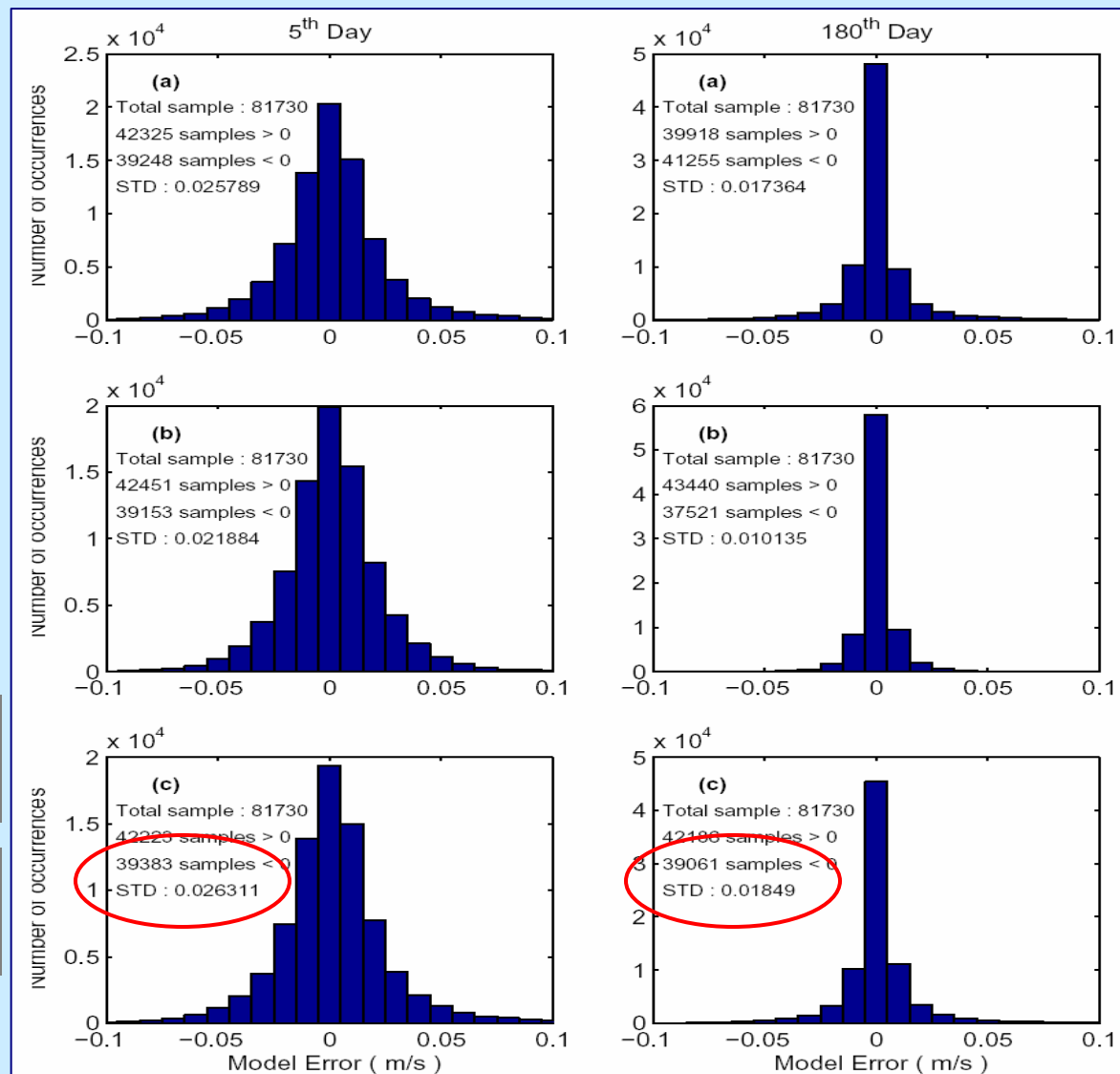
- Horizontal distribution

- Histogram

## Relative Root Mean Square Error

Larger model error in Run 11.

Model error is decreasing with time.

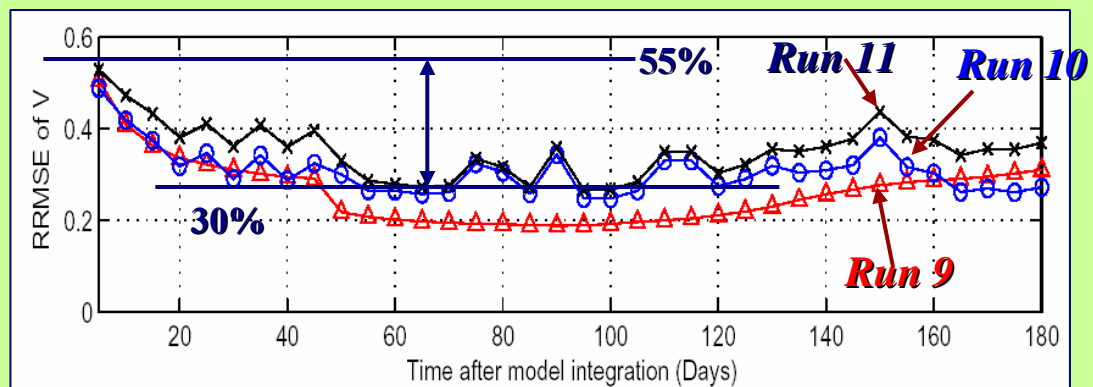
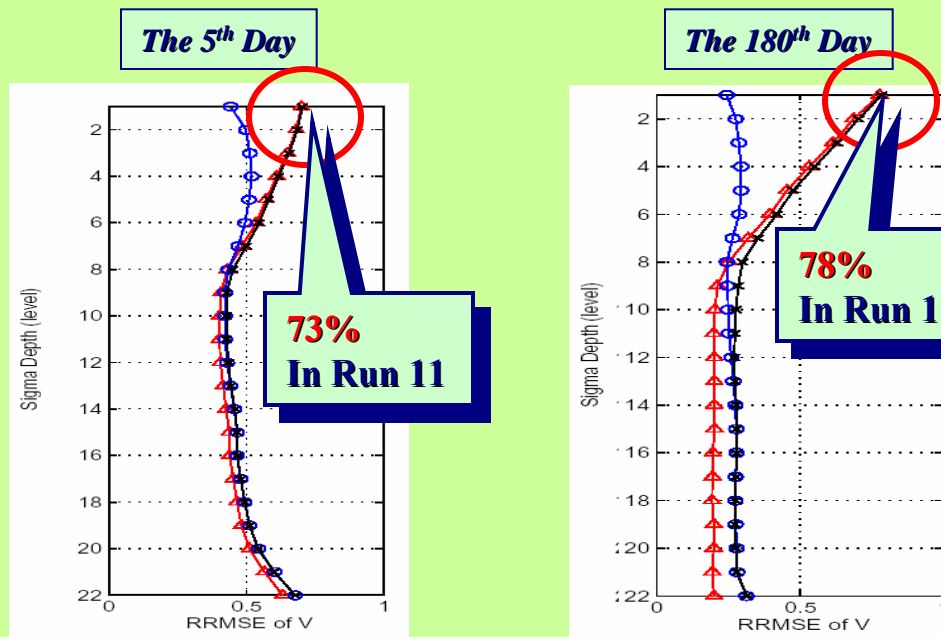


# Model Errors Due To Combined Uncertainty

- Model Error Distribution
- Relative Root Mean Square Error (RRMSE)
  - Vertical Variation
  - Temporal

Larger model error in Run 11.

Effects to the horizontal velocity prediction are quite significant.



# Conclusions

For uncertain velocity initial conditions :

- The model errors **decreases** with time.
- The model errors with and without ***diagnostic initialization*** are quite comparable and significant.
- The magnitude of model errors is less dependent on the ***diagnostic initialization period*** no matter it is 30 day, 60 day or 90 day.

Experiment	Vertically averaged RRMSE		Max. RRMSE	
	Min.	Max.	5 <sup>th</sup> Day	180 <sup>th</sup> Day
For uncertain <u>velocity initial conditions</u>	<u>20%</u>	<u>50%</u>	<u>70%</u> near the <u>surface</u>	<u>25%</u> near the <u>surface</u>

# Conclusions

For uncertain wind forcing :

- The model error increases with time and noise intensity.

Experiment	Vertically averaged RRMSE		Max. RRMSE	
	Min.	Max.	5 <sup>th</sup> Day	180 <sup>th</sup> Day
For <b>0.5 m/s</b> noise intensity	<b><u>8%</u></b>	<b><u>19%</u></b>	<b><u>35%</u></b> near the <u>surface</u>	<b><u>50%</u></b> near the <u>surface</u>
For <b>1.0 m/s</b> noise intensity	<b><u>11%</u></b>	<b><u>28%</u></b>	<b><u>60%</u></b> near the <u>surface</u>	<b><u>80%</u></b> near the <u>surface</u>

# Conclusions

For uncertain lateral boundary transport :

- The model error increases with time and noise intensity.

Experiment	Vertically averaged RRMSE		Max. RRMSE	
	Min.	Max.	5 <sup>th</sup> Day	180 <sup>th</sup> Day
For noise intensity as 5% of transport	<u>9%</u>	<u>20%</u>	<u>14% near the bottom</u>	<u>18% near the bottom</u>
For noise intensity as 10% of transport	<u>17%</u>	<u>34%</u>	<u>24% near the bottom</u>	<u>28% near the bottom</u>

# Conclusions

For combined uncertainty :

Experiment	Vertically averaged RRMSE		Max. RRMSE	
	Min.	Max.	5 <sup>th</sup> Day	180 <sup>th</sup> Day
For uncertain <u>initial condition</u> and <u>wind forcing</u>	<u>20%</u>	<u>52%</u>	<u>70%</u> near the <u>surface</u>	<u>77%</u> near the <u>surface</u>
For uncertain <u>initial condition</u> and <u>lateral boundary transport</u>	<u>27%</u>	<u>50%</u>	<u>65%</u> near the <u>bottom</u>	<u>35%</u> near the <u>bottom</u>
For uncertain <u>initial condition</u> , <u>wind forcing</u> and <u>lateral boundary transport</u>	<u>30%</u>	<u>55%</u>	<u>73%</u> near the <u>surface</u>	<u>78%</u> near the <u>surface</u>