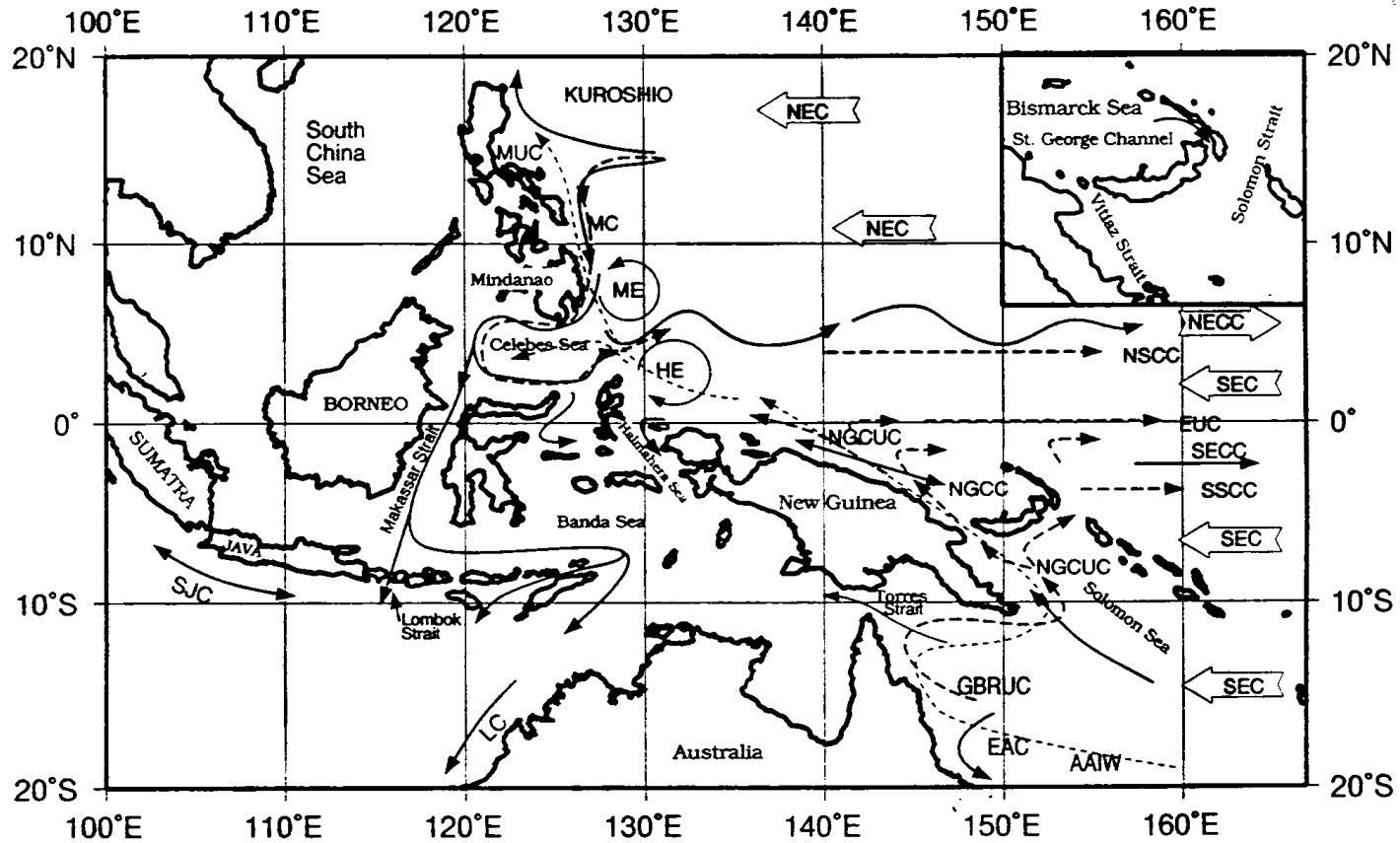


# Isopycnal Surface Circulation in Water Mass Crossroads

Peter C Chu, R. Li, and C.W. Fan

Naval Postgraduate School,  
Monterey, California

# Water Mass Crossroads (Fines et al. 1994)

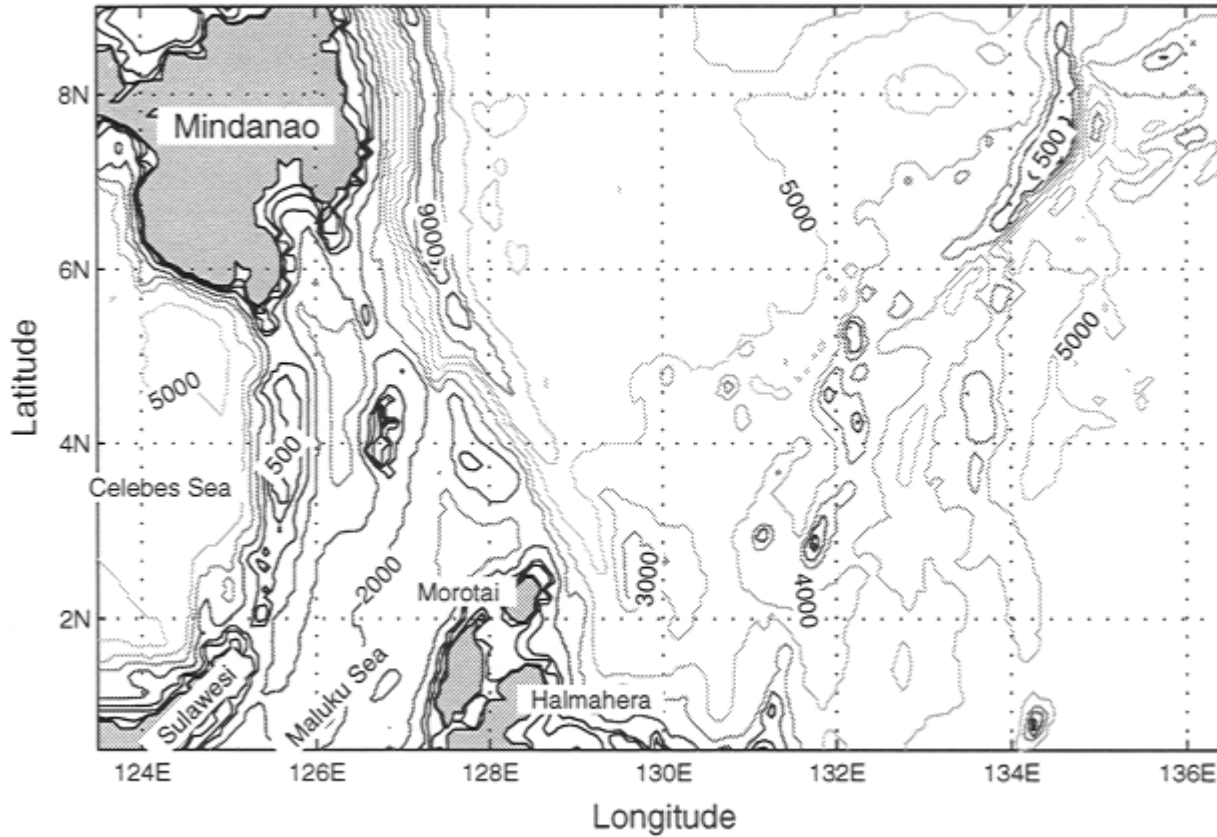


# Literature

- Lukas (1988, JGR)
- Lukas et al. (1991, 1996)
- Godfrey (1996)
- Fine et al. (1994)
- Qiu and Lukas (1999)
- Qiu et al. (1998)
- Qu (1998, 1999)
- Wajsowicz (1993, 1999a, b)

Can we get seasonal  
variability of current  
structure from T, S data?

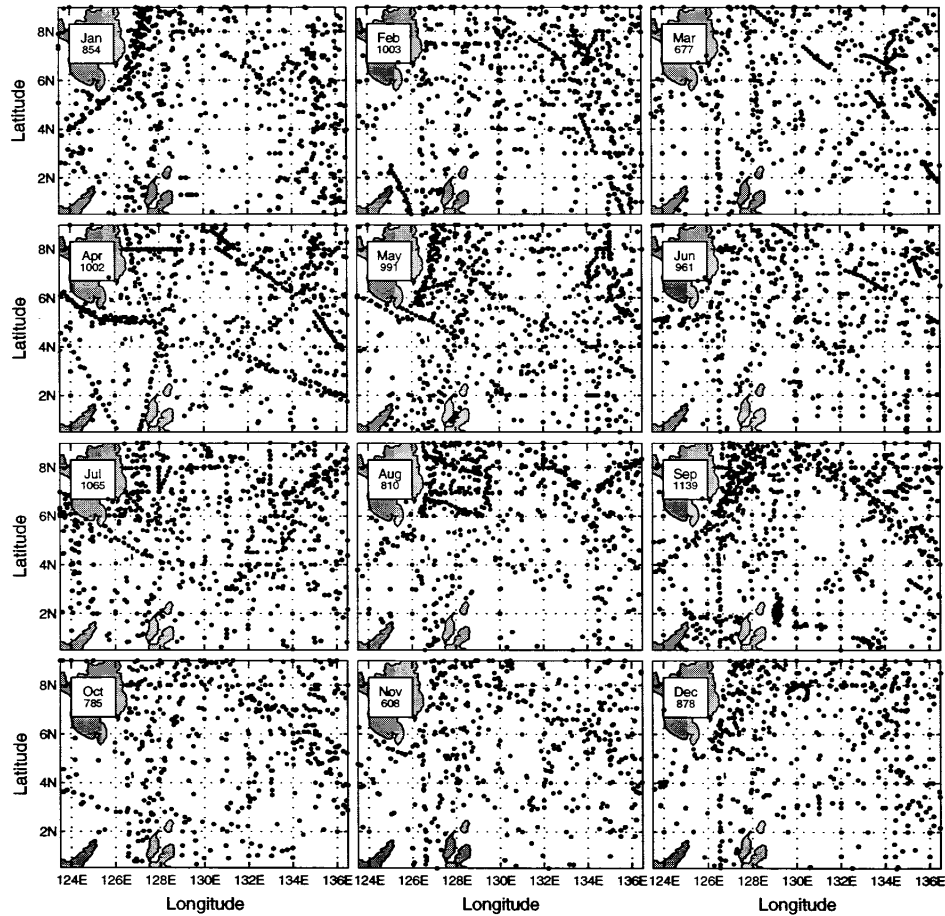
# Geography and Topography



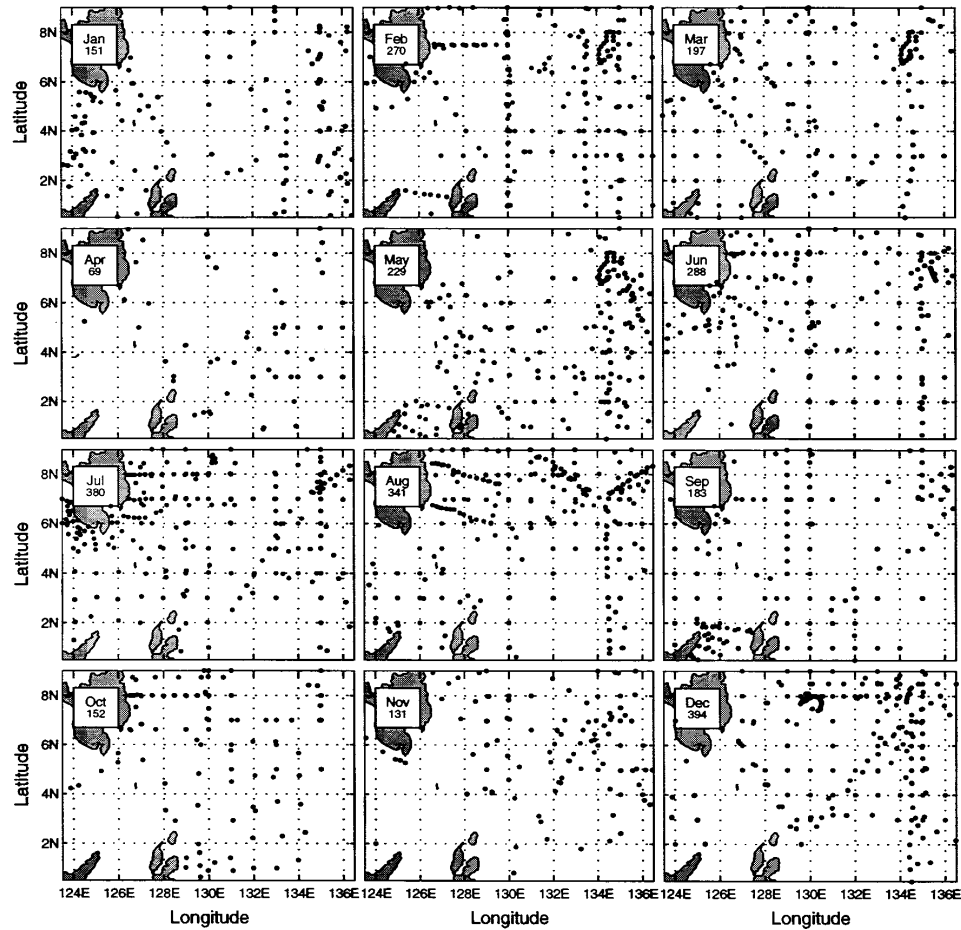
# Navy's GDEM Climatology

- Monthly mean temperature and salinity
- 0.5° Horizontal resolution
- 59 Vertical levels
- Built-up from The Navy's Master Oceanographic Observational Data Set (MOODS)

# Navy's MODDS (Temperature)

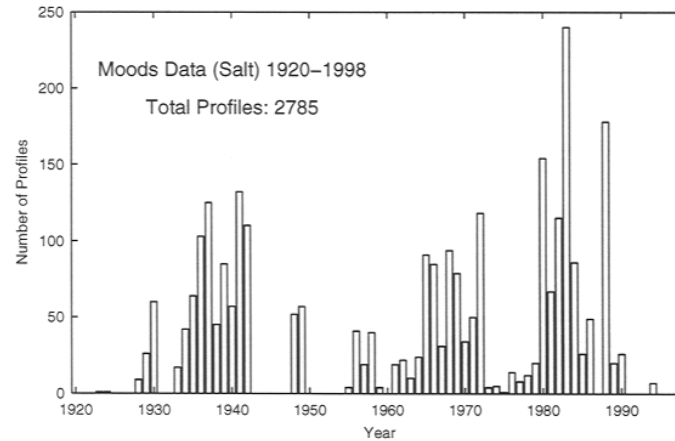
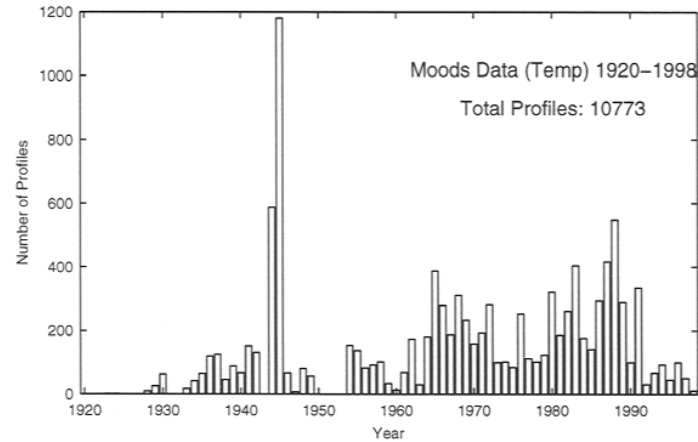


# MOODS Data (Salinity)

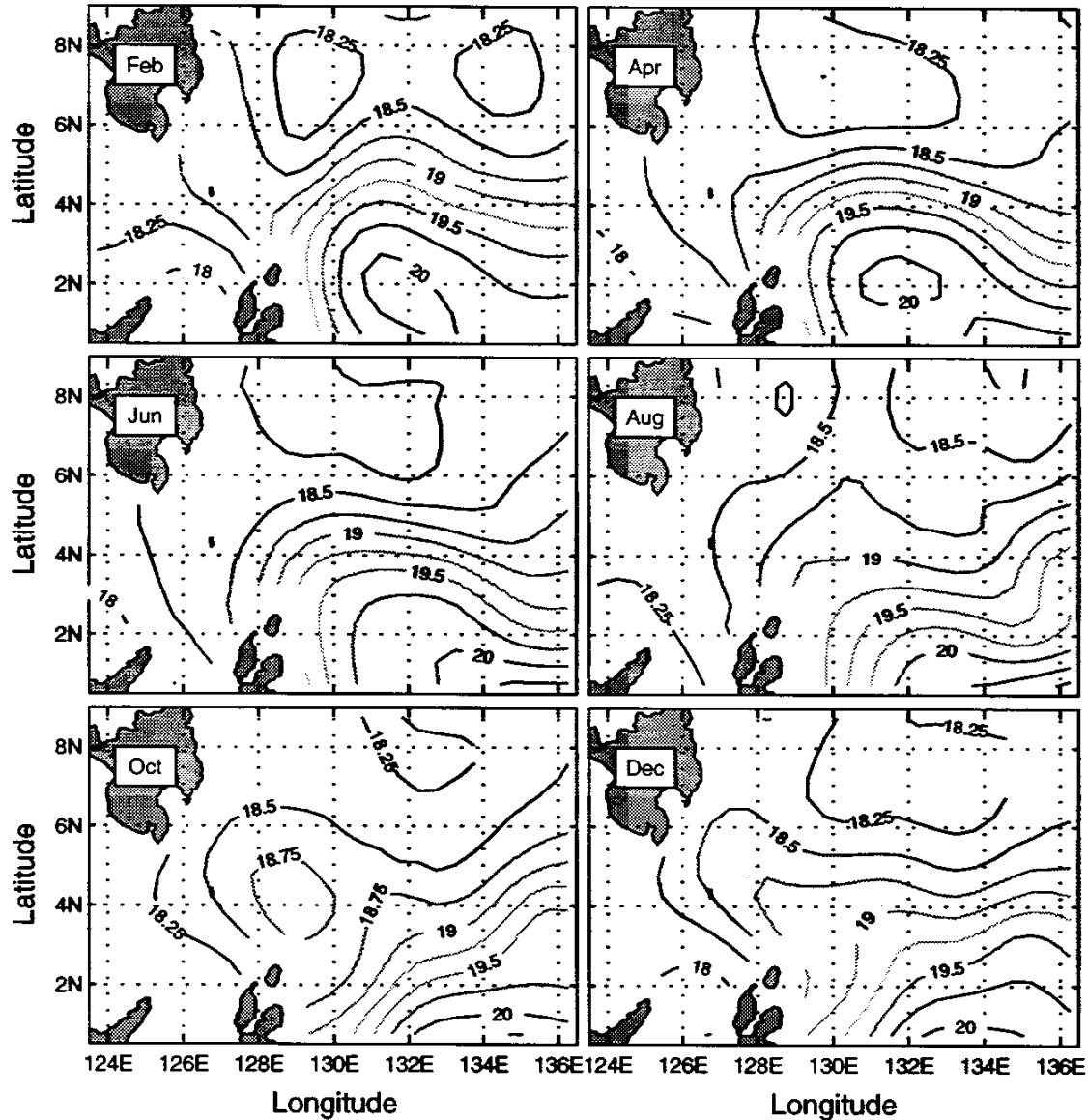




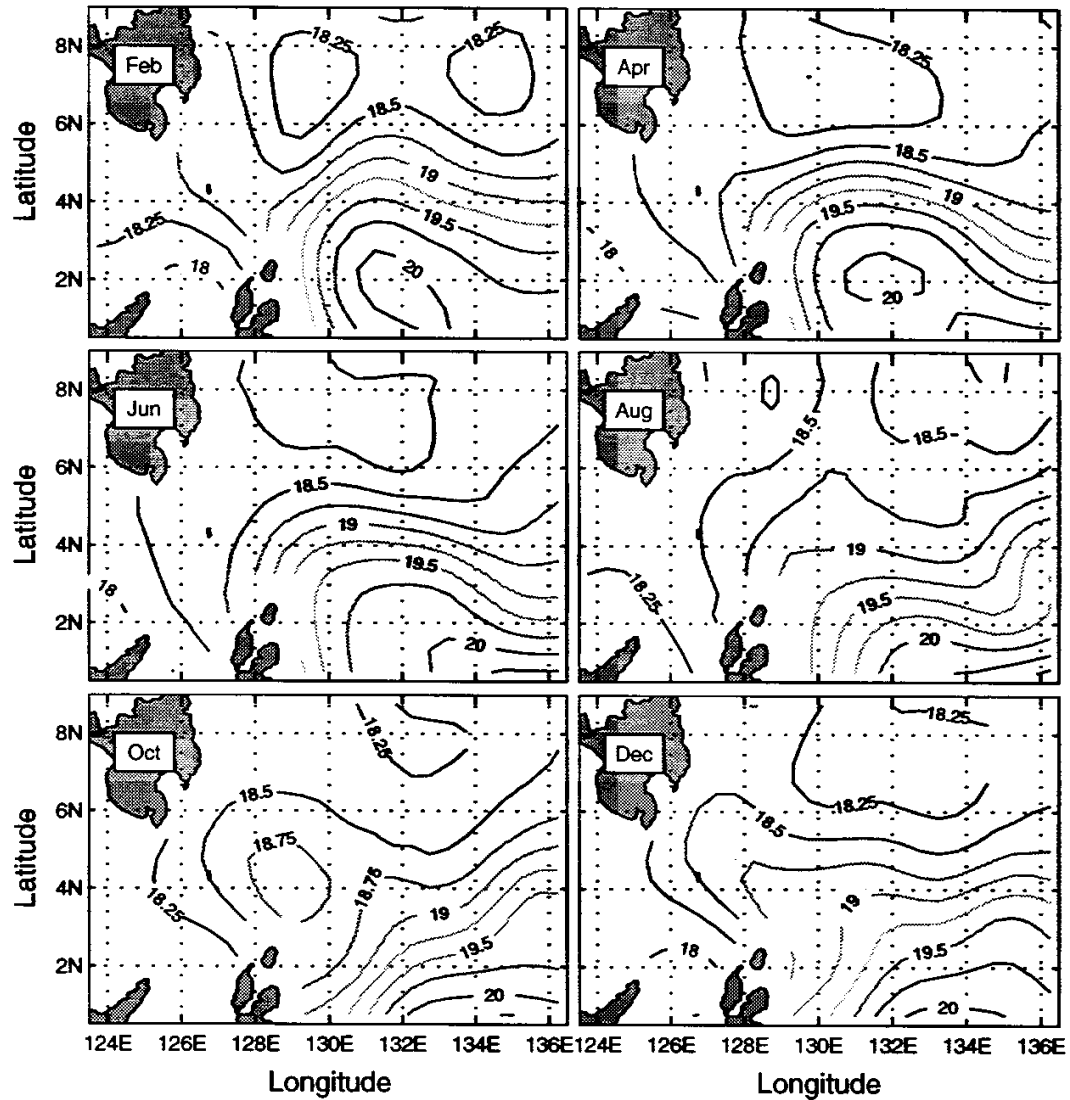
# Temporal Distributions of MOODS Stations



# Temperature (GDEM)



# Salinity (GDEM)

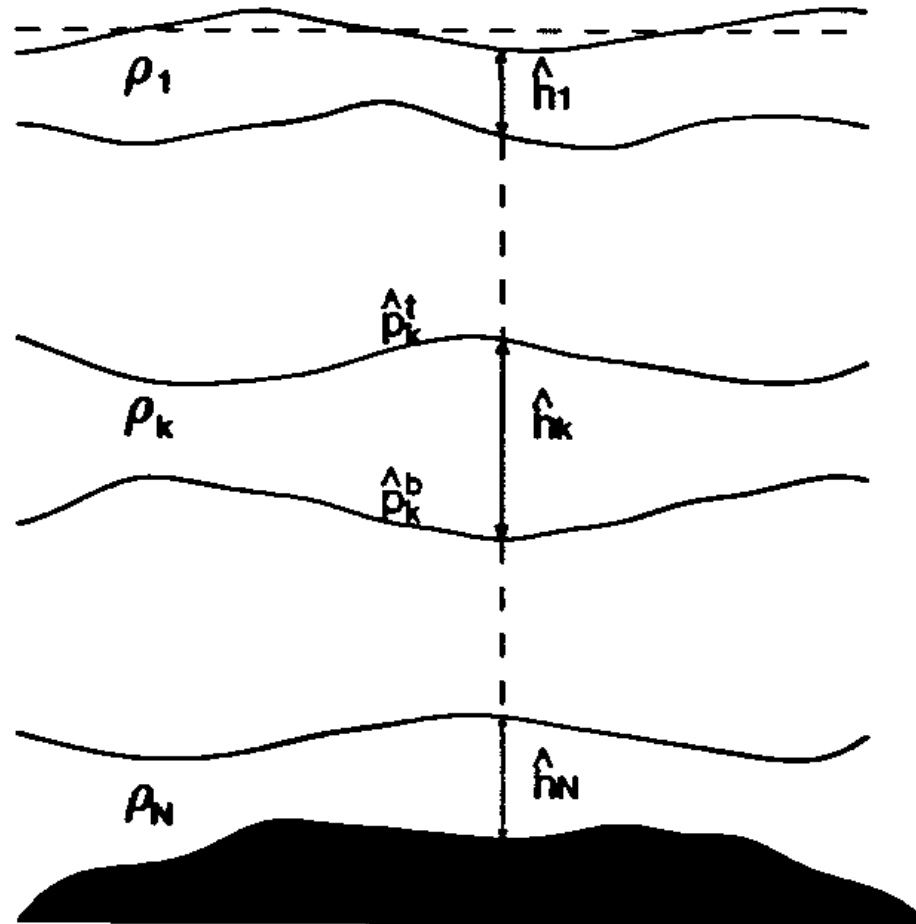


# Absolute Velocity

$$\mathbf{V} = \mathbf{V}_0 + \frac{1}{f} \mathbf{k} \times \int_{z_0}^z \nabla \left[ \frac{\partial}{\partial z} \left( \frac{p}{\rho} \right) \right] dz',$$

$$\mathbf{V}' = \frac{1}{f} \mathbf{k} \times \int_{z_0}^z \nabla \left[ \frac{\partial}{\partial z} \left( \frac{p}{\rho} \right) \right] dz' = -\frac{g}{f\rho_0} \mathbf{k} \times \int_{z_0}^z \nabla \rho dz'.$$

# Isopycnal Surface



# Isopycnal Surface

- Potential Density Surfaces ( $\sigma_\theta$ ) with the Depth  $z^{(\sigma)}$

$$z^{(\sigma)} = R(x, y, \sigma).$$

- Vertical Distance Between two  $\sigma$ -Levels

$$h^{(\sigma)} = \frac{\partial z^{(\sigma)}}{\partial \sigma} \Delta \sigma.$$

# Pseudo-Potential Vorticity Conservation on Isopycnal Surface (McDogall 1988)

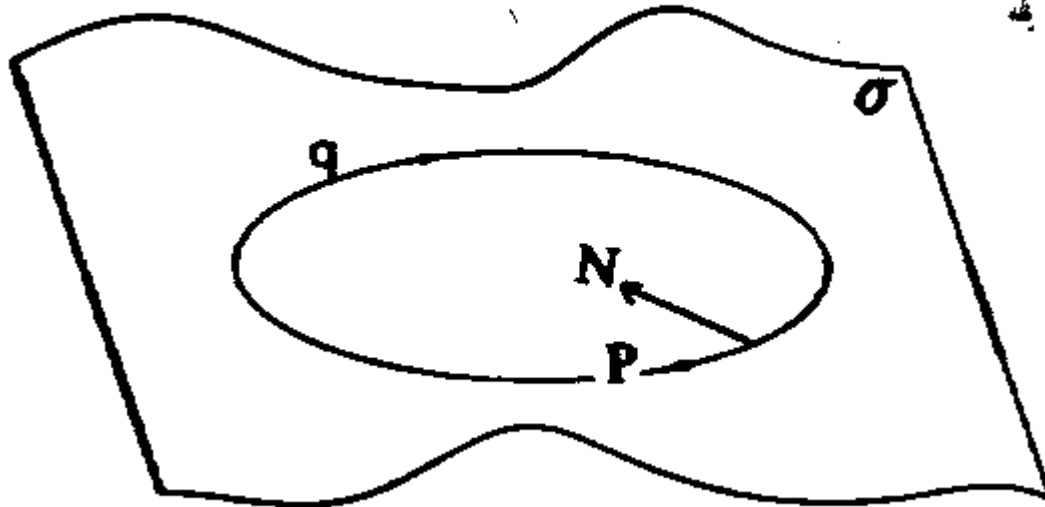
- Pseudo Potential Vorticity

$$q^{(\sigma)} = \ln[Q^{(\sigma)}], \quad Q^{(\sigma)} = \frac{f}{h^{(\sigma)}}$$

- Conservation of Pseudo Potential Vorticity on Isopycnal Surface

$$\mathbf{V}^{(\sigma)} \cdot \nabla_{\sigma} [q^{(\sigma)}] = \frac{\partial w^{(\sigma)}}{\partial z},$$

# Two Unit Vectors on Isopycnal Surface





# Two Unit Vectors on Isopycnal Surface

- P – Vector

$$\mathbf{P} = \frac{1}{|\nabla q^{(\sigma)}|} \left( \frac{\partial q^{(\sigma)}}{\partial y} \mathbf{i} - \frac{\partial q^{(\sigma)}}{\partial x} \mathbf{j} \right),$$

- N - Vector

$$\mathbf{N} = \frac{\nabla_{\sigma} (q^{(\sigma)})}{|\nabla_{\sigma} (q^{(\sigma)})|}$$

# P-Vector Components

$$P_x = \left( \frac{\beta}{f} - \frac{\partial \ln h^{(\sigma)}}{\partial y} \right) / \left[ \left( \frac{\beta}{f} - \frac{\partial \ln h^{(\sigma)}}{\partial y} \right)^2 + \left( \frac{\partial \ln h^{(\sigma)}}{\partial x} \right)^2 \right]^{1/2} .$$

$$P_y = \frac{\partial \ln h^{(\sigma)}}{\partial x} / \left[ \left( \frac{\beta}{f} - \frac{\partial \ln h^{(\sigma)}}{\partial y} \right)^2 + \left( \frac{\partial \ln h^{(\sigma)}}{\partial x} \right)^2 \right]^{1/2} .$$

# Absolute Velocity on Isopycnal Surface

- With Diapycnal Velocity

$$V^{(\sigma)} = \gamma P + \frac{\partial w^{(\sigma)} / \partial z}{|\nabla_{\sigma}(q^{(\sigma)})|} N$$

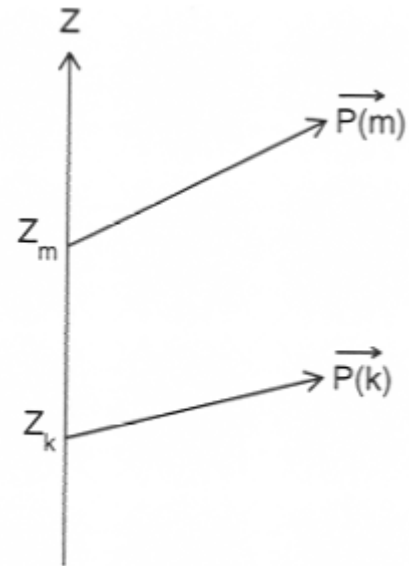
- Without Diapycnal Velocity

$$V^{(\sigma)} = \gamma P$$

# P-Vector Inverse Method

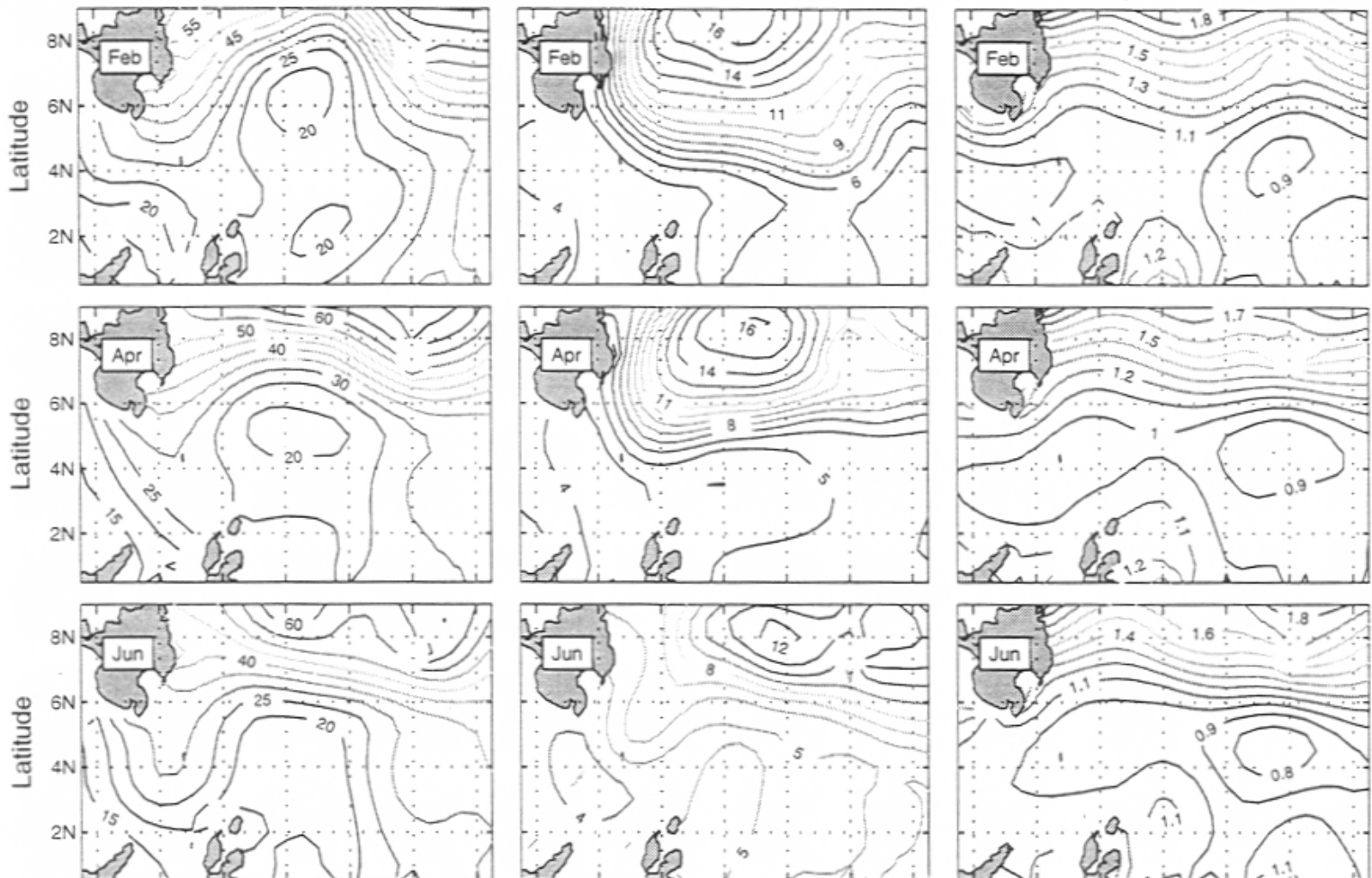
$$\gamma^{(k)} P_x^{(k)} - \gamma^{(m)} P_x^{(m)} = \Delta u_{km} =$$

$$\gamma^{(k)} P_y^{(k)} - \gamma^{(m)} P_y^{(m)} = \Delta v_{km} =$$



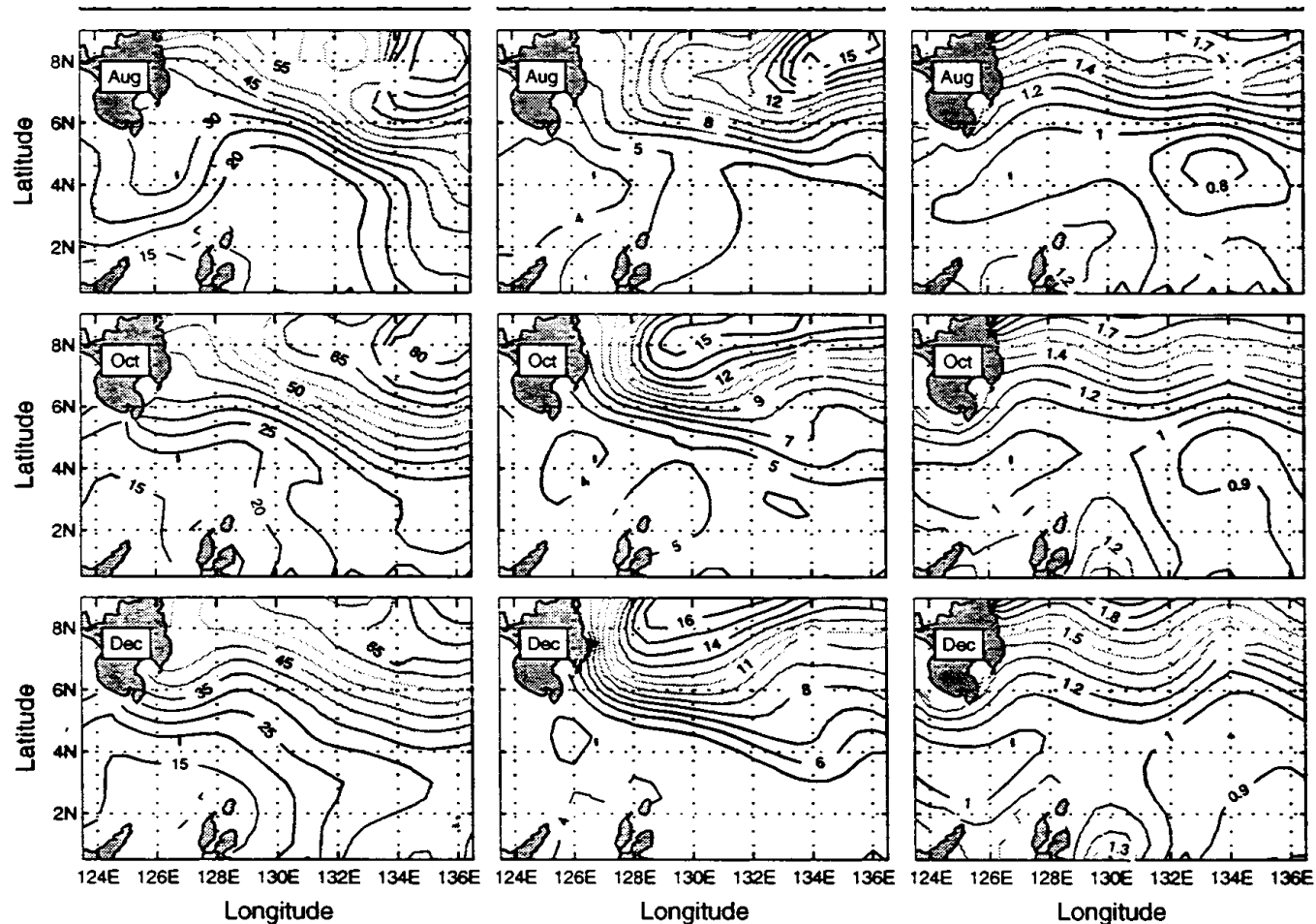
# Potential Vorticity on Isopycnal Surfaces

- Isopycnal:  $\sigma_{\theta}=25$        $\sigma_{\theta}=26.5$        $\sigma_{\theta}=27.2$



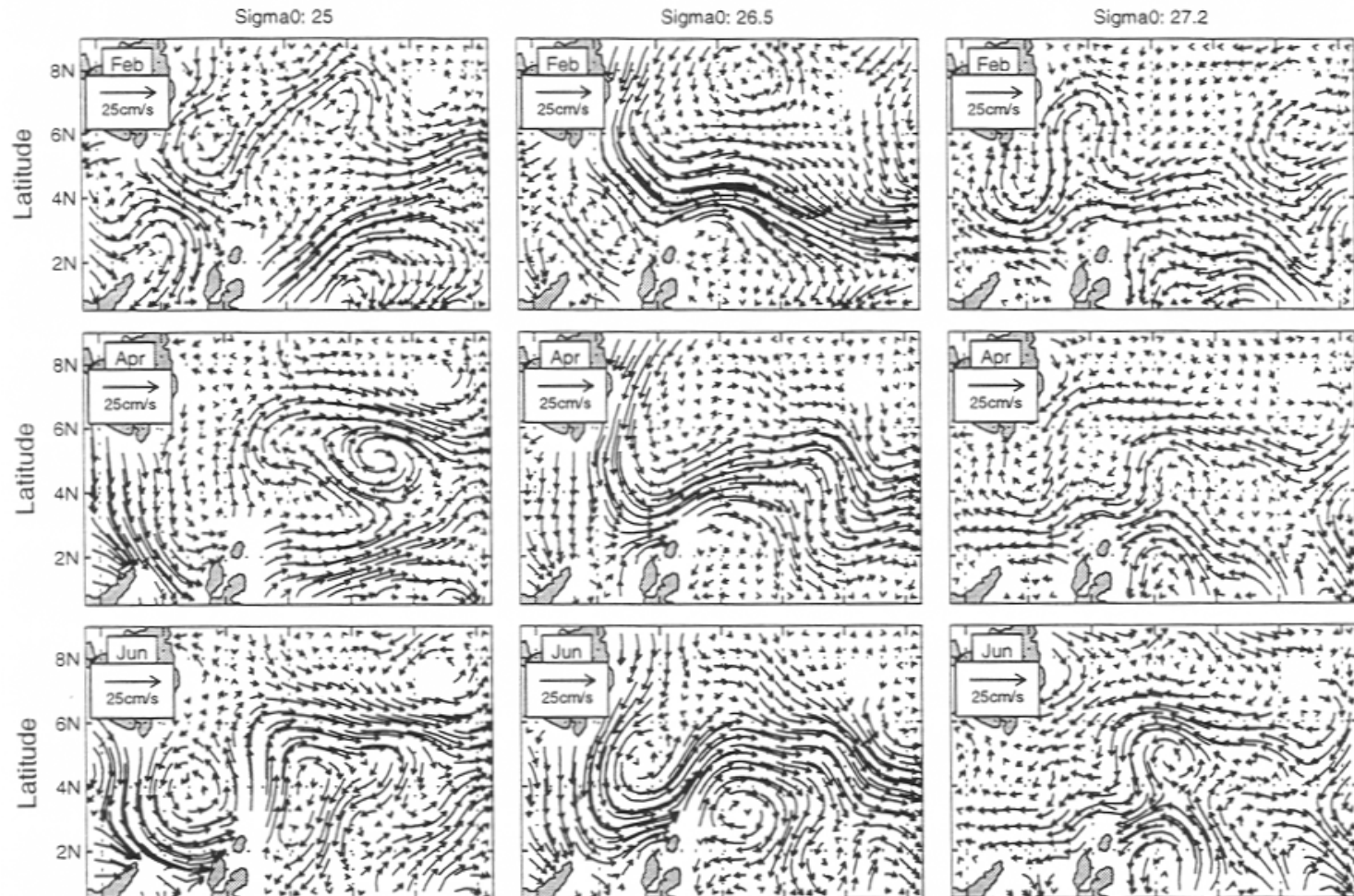
# Potential Vorticity on Isopycnal Surfaces

- Isopycnal:  $\sigma_{\theta}=25$        $\sigma_{\theta}=26.5$        $\sigma_{\theta}=27.2$



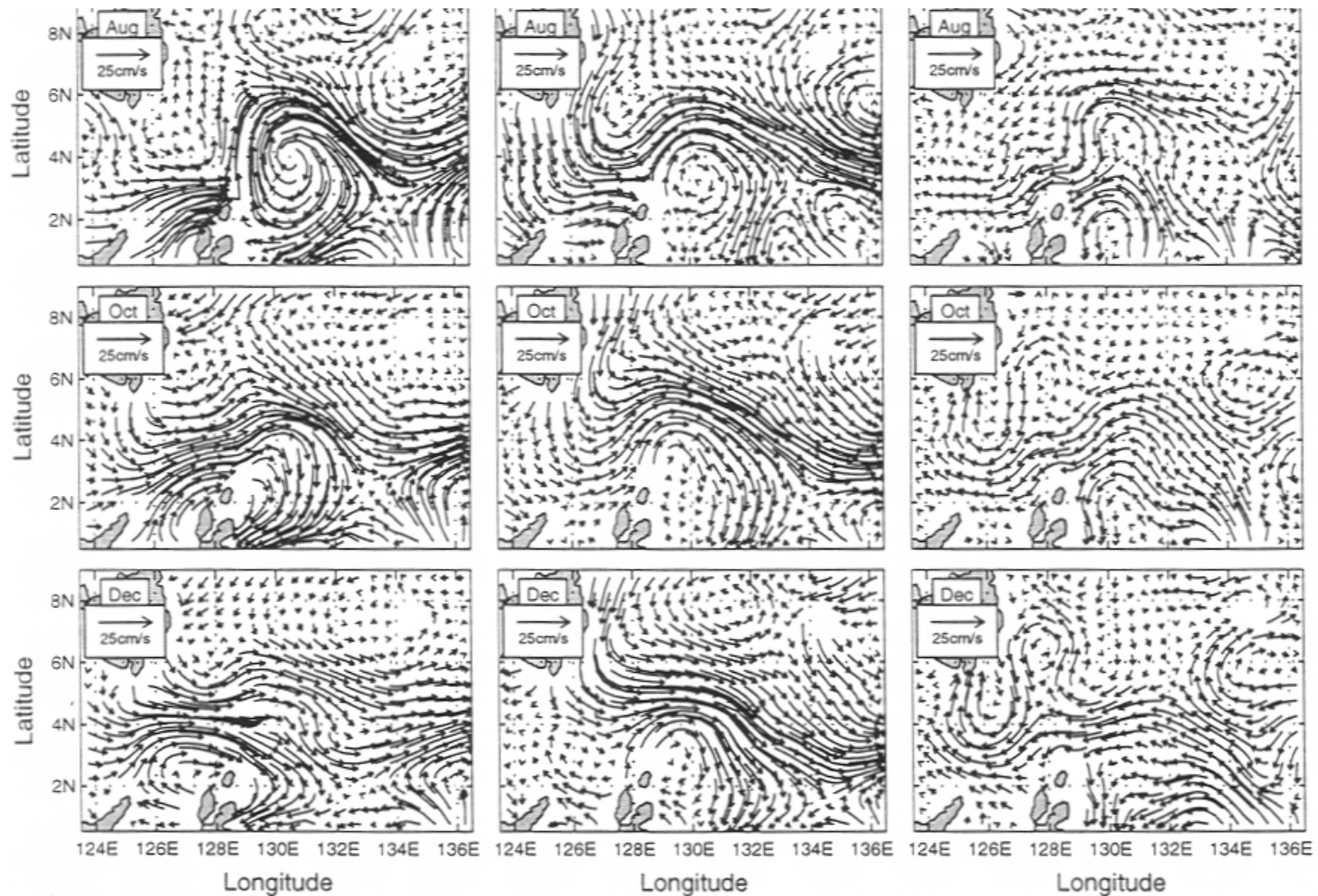
# Circulation on Isopycnal Surface

- Isopycnal:  $\sigma_\theta=25$        $\sigma_\theta=26.5$        $\sigma_\theta=27.2$



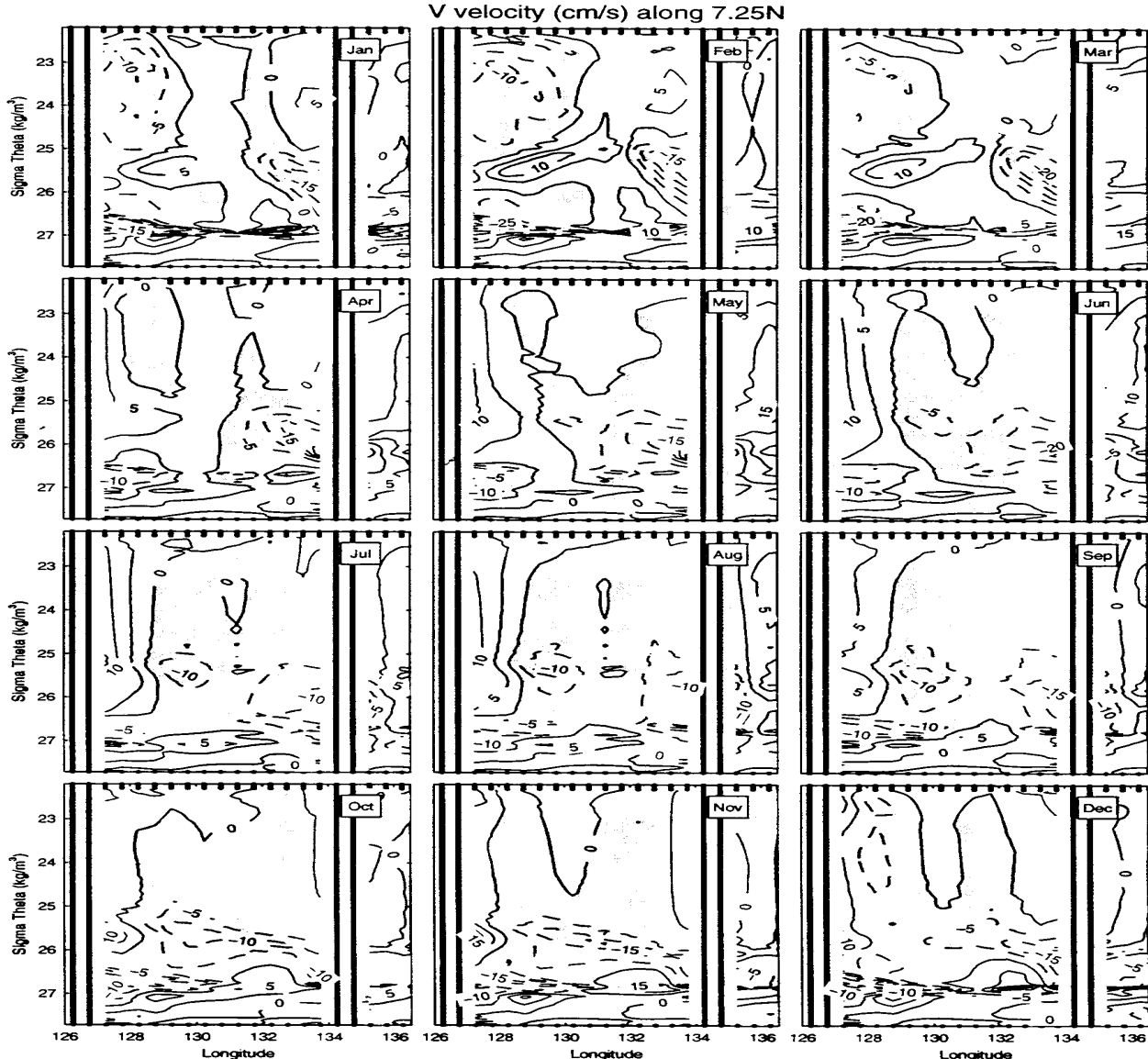
# Circulation on Isopycnal Surface

- Isopycnal:  $\sigma_\theta=25$        $\sigma_\theta=26.5$        $\sigma_\theta=27.2$

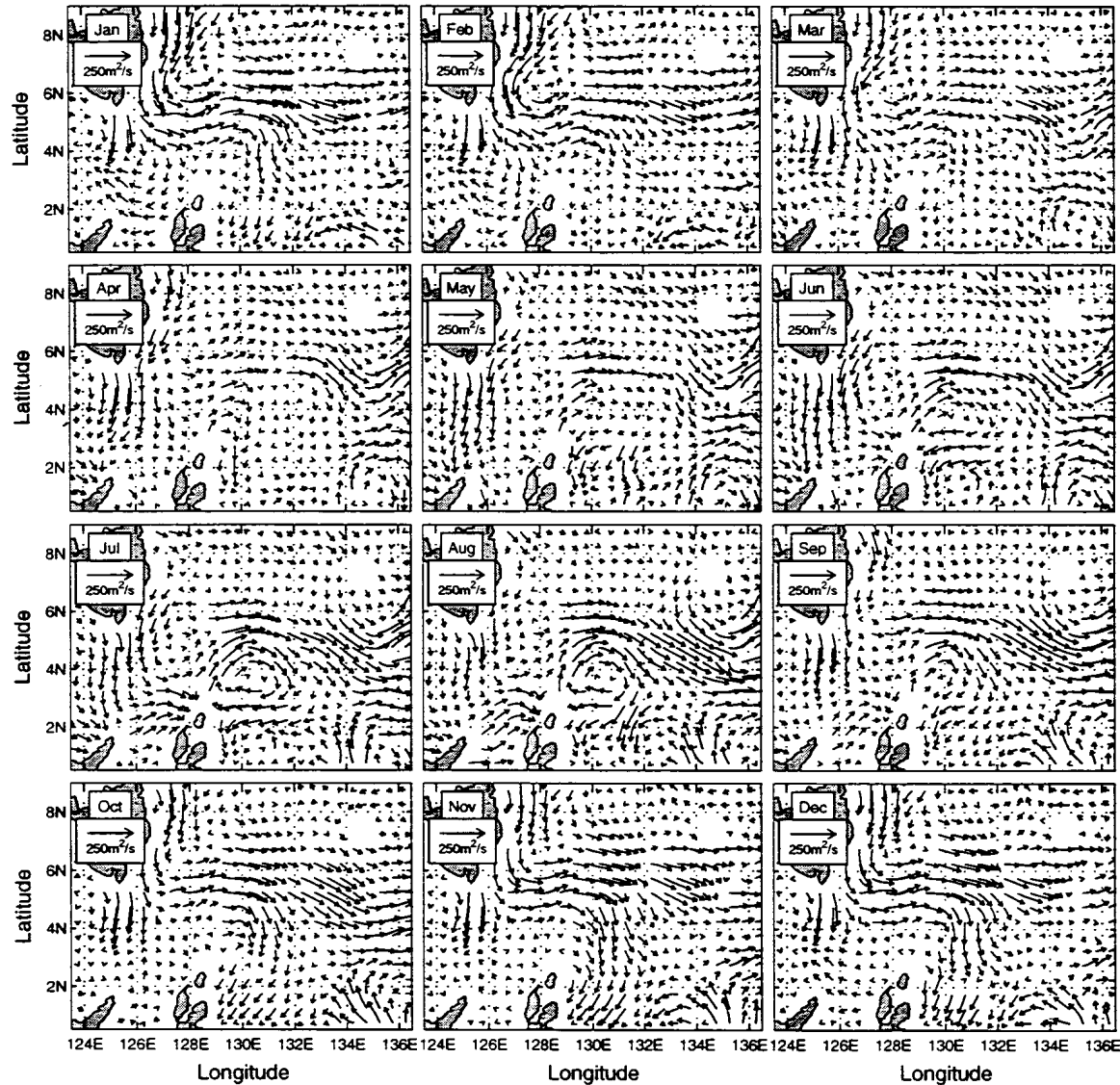




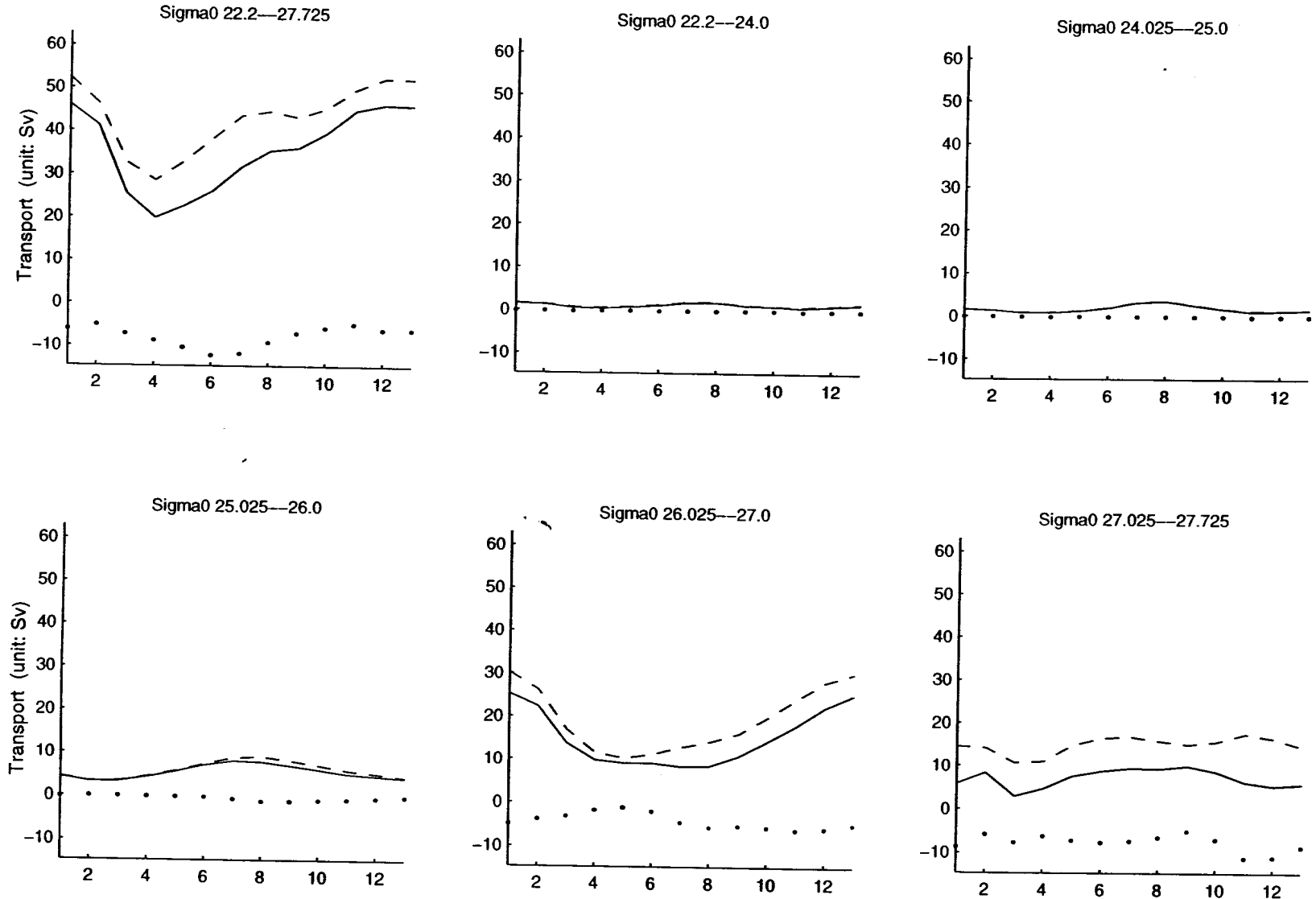
# V-Velocity (cm/s) along 7.25° N



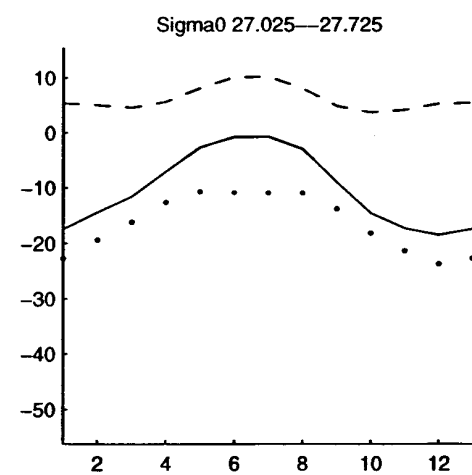
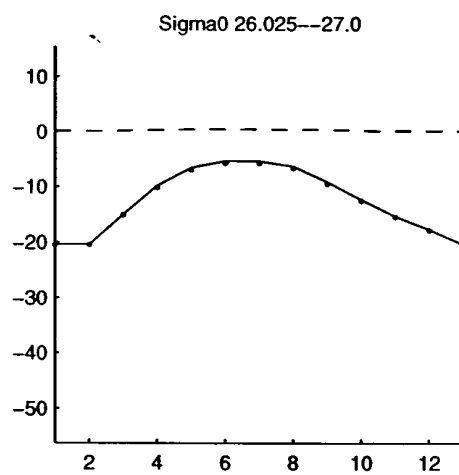
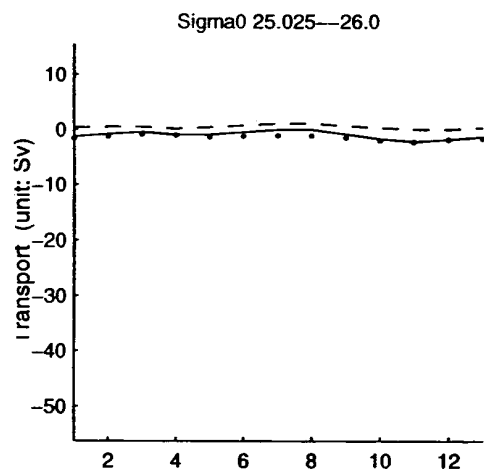
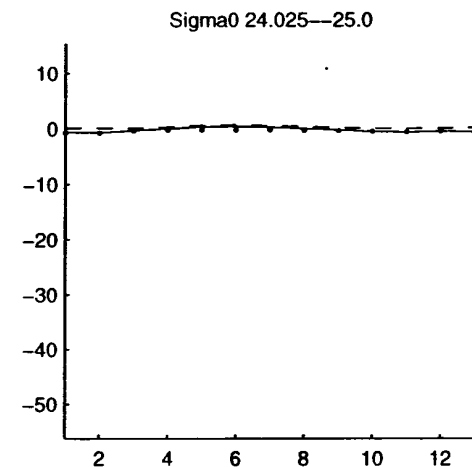
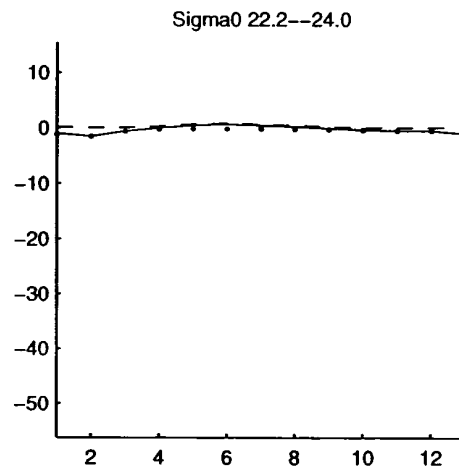
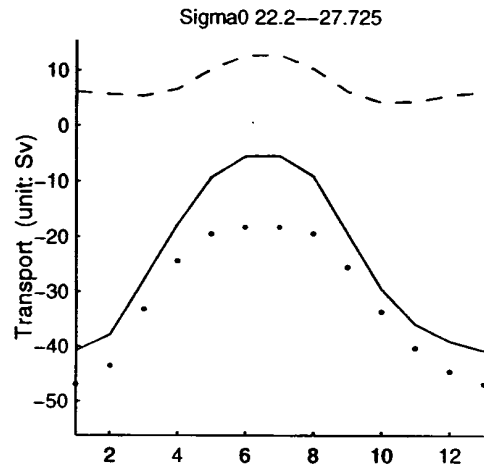
# Vertically integrated velocity vectors ( $250 \text{ m}^2 / \text{s}$ )



# Volume Transport (Sv) of North Pacific Equatorial Counter Current (0.75 to 8.25° N) along 130.25° E



# Volume Transport (Sv) of Midanao Current (126.75 to 130.75° E) along 8.25° N



# Conclusions

- **Seasonal Variability of Four Major Currents**

Mindanao Current, Mindanao Counter Current, New Guinea Coastal Undercurrent, and North Equatorial Counter Current

## Two Eddies

Mindanao Eddy and Halmahera Eddy