

Operational Resilience Analysis and Capacity Building in the US Virgin Islands



David L. Alderson, PhD

Associate Professor, Operations Research Department

Director, Center for Infrastructure Defense

Naval Postgraduate School

Workshop: Fundamentals of Microgrid Analysis and Design
Sandia National Laboratories & University of the Virgin Islands
St. Croix Campus (24 Oct 2018) & St. Thomas Campus (26 Oct 2018)

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Naval Postgraduate School (NPS)

America's national security research university

History Highlights

1909 Founded at U.S. Naval Academy

1951 Moved to Monterey, CA
Operations Research Curriculum

- Facilities of a graduate research university
- Faculty who work for the U.S. Navy, with clearances
- Students with fresh operational experience

FY2017:

- 65 M.S. and 15 Ph.D. programs
- 612 faculty
- 1432 resident students includes (166 international / 47 countries)
- 909 distributed learning students



Operations Research at NPS

- Operations Research (OR) is the science of helping people and organizations make better decisions using
 - mathematical models, statistical analyses, simulations
 - analytical reasoning and common senseto the understanding and improvement of real-world operations.
- OR originated during World War II. The military uses OR at the strategic, operational, and tactical levels.
- Biggest users of OR: modern corporations
 - Supply chain logistics
 - Manufacturing and production planning
 - Scheduling
- NPS has the oldest OR instructional program in the U.S.

NPS Center for Infrastructure Defense (CID)

Operations Research Department



David Alderson
Associate Professor, OR
Director, NPS Center for
Infrastructure Defense
Ph.D., Stanford University,
2003



Gerald Brown
Distinguished Emeritus
Professor, OR
Member, National Academy
of Engineering
Ph.D., U.C.L.A., 1974



W. Matthew Carlyle
Professor & Chair, OR
Ph.D., Stanford University,
1997



Robert Dell
Professor, OR
Ph.D., S.U.N.Y. Buffalo,
1990



Daniel Eisenberg
Research Assistant
Professor, OR
Ph.D., Arizona State
University, 2018

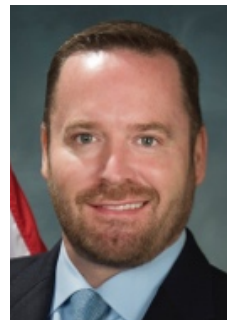


Javier Salmerón
Associate Professor, OR
Ph.D., Universidad
Politécnica (Spain), 1998

NPS Energy Academic Group (EAG)



Dan Nussbaum
Visiting Professor, OR
Chair, NPS Energy
Academic Group
Ph.D., Michigan State
Univ., 1971



Alan Howard
Deputy Director, NPS
Energy Academic Group
MBA/MIM in International
Management, 2000



Jack Templeton
Program Manager, NPS
Energy Academic Group
MSM Defense Systems
Analysis, NPS, 2013

What is Critical Infrastructure?

- **Critical Infrastructure (CI):** “systems and assets, whether physical or virtual, so vital to the United States that the incapacity or destruction of such systems and assets would have a debilitating impact on security, national economic security, national public health or safety, or any combination of those matters” --**Section 1016(e) of the USA PATRIOT Act of 2001**





Critical Infrastructure Systems:

NPS has a unique perspective and capability

- We have been studying critical infrastructure for decades.
- We look at our own domestic infrastructure through the eyes of intelligent adversaries.
- We have conducted over 150 “red team analyses” to plan attacks on our own infrastructure (and determine how to mount effective hardening and defensive efforts)



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Goals For This Session

- **10 key ideas** for how to assess and improve operational resilience of critical infrastructures
- Ongoing work in applying these ideas to the USVI

Idea #1: **Start by focusing on delivery of services,**
not mitigation of hazards/threats

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**What we need to do
(operation)**

- Electricity
- Fuels
- Transportation
- Communications
- Water & Wastewater
- Emergency response

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**What can go wrong
(interdiction)**

- Extreme Weather
 - Coastal Flooding
 - Rainfall Flooding
 - Wind
 - Drought
- Human accident
- Technological failure
- Deliberate attack

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Idea #2: Avoid getting stuck on predefined threat scenarios.

- Surprise Happens. Things we have not imagined.
- Tunnel vision (on the last disaster). Need to be proactive, not reactive.

A policy shift toward “operational resilience”

U.S. National Strategy for Homeland Security (2007)

“We will not be able to deter all terrorist threats, and it is impossible to deter or prevent natural catastrophes. We can, however, mitigate the Nation’s vulnerability to acts of terrorism, other man-made threats, and natural disasters by **ensuring the structural and operational resilience** of our critical infrastructure and key resources” (p. 27)

“We must now focus on the **resilience of the system as a whole** – an approach that centers on investments that make the system better able to absorb the impact of an event without losing the capacity to function” (p.28)

Most recently: U.S. Presidential Policy Directive (PPD)-21: Critical Infrastructure Security and Resilience, 2013.

“system as a whole” and “capacity to function”

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How to Think About Critical Infrastructure (CI)

- A list of assets
- An interconnected (network) system that works to achieve a particular function

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Idea #3: We need to think in terms of **systems.**

We want to make our operations
(public and private) resilient to disruptive events.

We need our infrastructure systems to continue to
function even when “bad things” happen.

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A shift toward “operational resilience”

- DOD Directive 3020.40: Mission Assurance (2016)

DOD has recently reorganized its efforts to protect defense-related critical infrastructure under a broader program of *mission assurance*

- Key recognition

- Assets work together as systems to provide function
- Function enables capability
- Capability supports mission

- Focus needs to remain on the relationship between the infrastructure asset and the missions it supports

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Idea #4: **Resilience is not about what you have,
its about what you do!** This is a common misperception.
(Think of safety as another concept with this feature...)

Idea #5: Take an “operational” perspective

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- Demographics
- Geography
- Population density
- Special needs

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Move goods/services from areas of supply to demands:

- Must include infrastructure owners and operators
- Both public and private!

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Idea #6: Often represented as **flows** through **networks**.

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Idea #7: Measure **performance**.
Define **mission success**.

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BUT... Systems Are Complicated, Sometimes Complex

- Interactions often non-additive and non-intuitive.
- An event in one location can often affect things that are far away, and it can be hard to predict how this happens.
- The contribution/importance of a single component to system function may depend on interactions with other components.

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- When determining how best to protect systems, a natural question is, “*What components are most critical?*”
- Better yet: *Which components, if lost, would be most disruptive to system function?*

Definition: A component is *critical* if losing it would significantly reduce system function (relative to the reduction from losing other components).

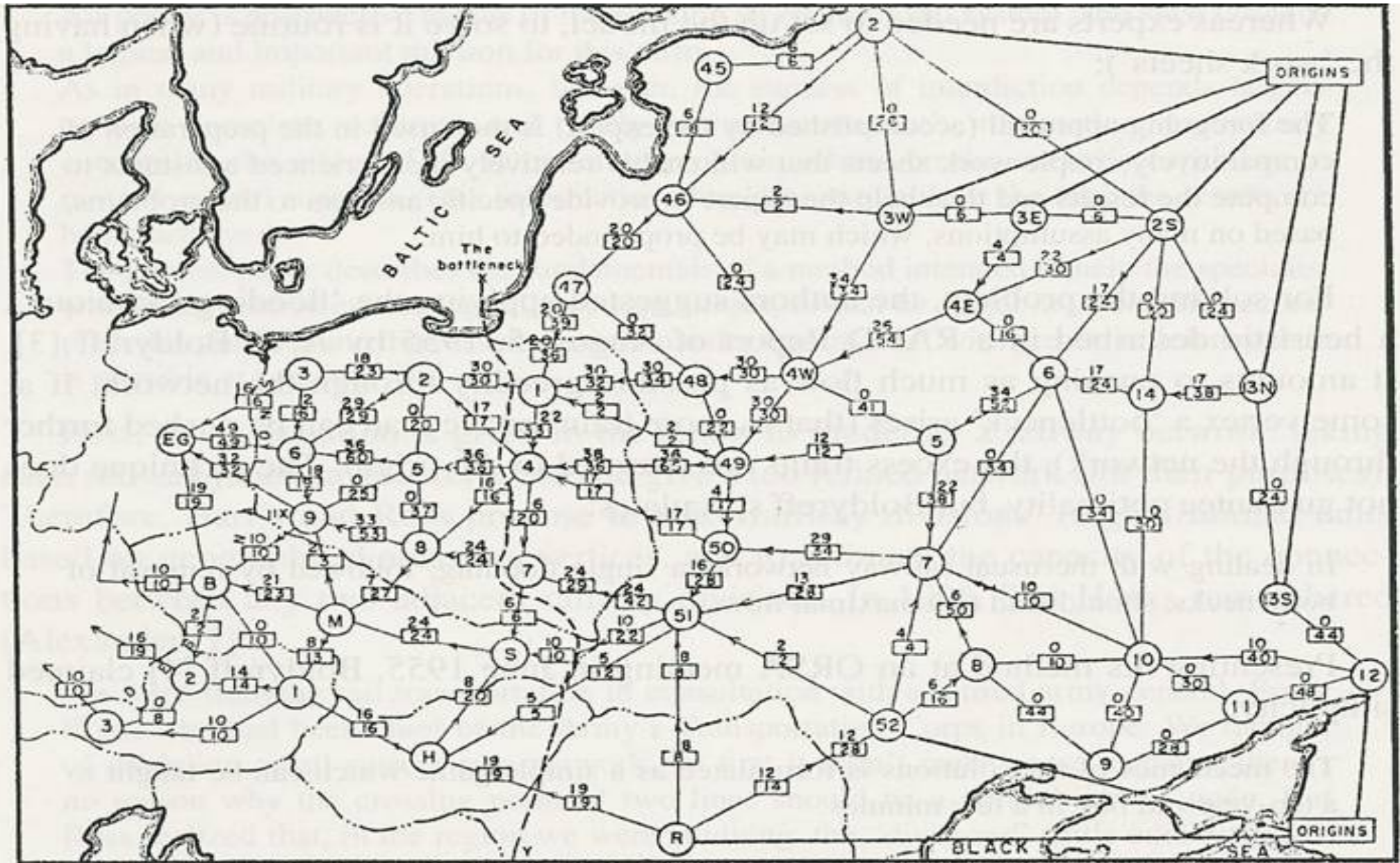
Let's use a historical example to illustrate...

The Russian Rail Network (circa 1955)

Data from Figure 7 of:

Harris, T.E., and Ross, F.S. (1955), *Fundamentals of a Method for Evaluating Rail Net Capacities* (SECRET, declassified 1999), RM-1573, RAND Corp.

What is the capacity of the USSR to deliver materiel to Europe via rail?

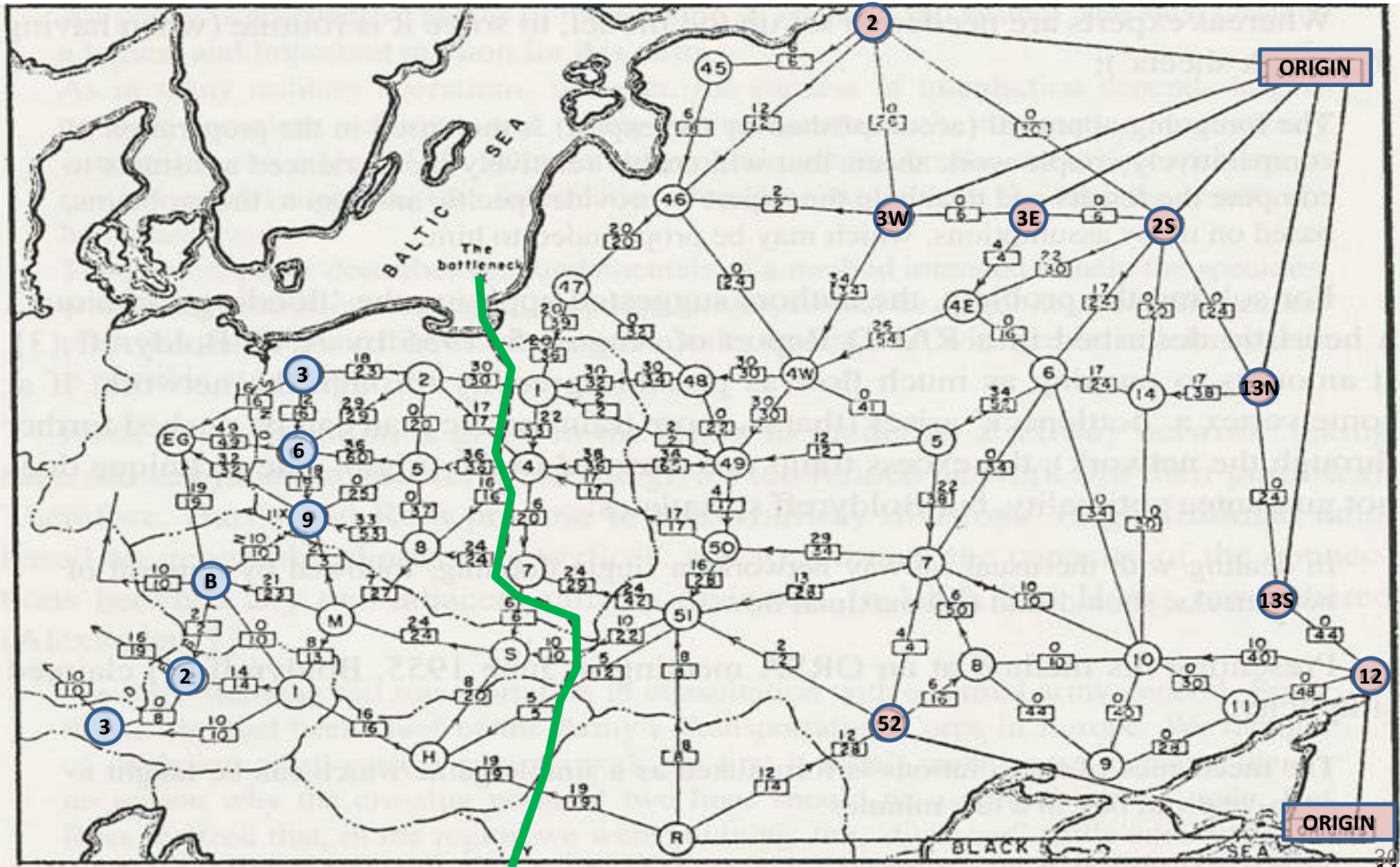


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destination nodes

minimum capacity cut

origin nodes

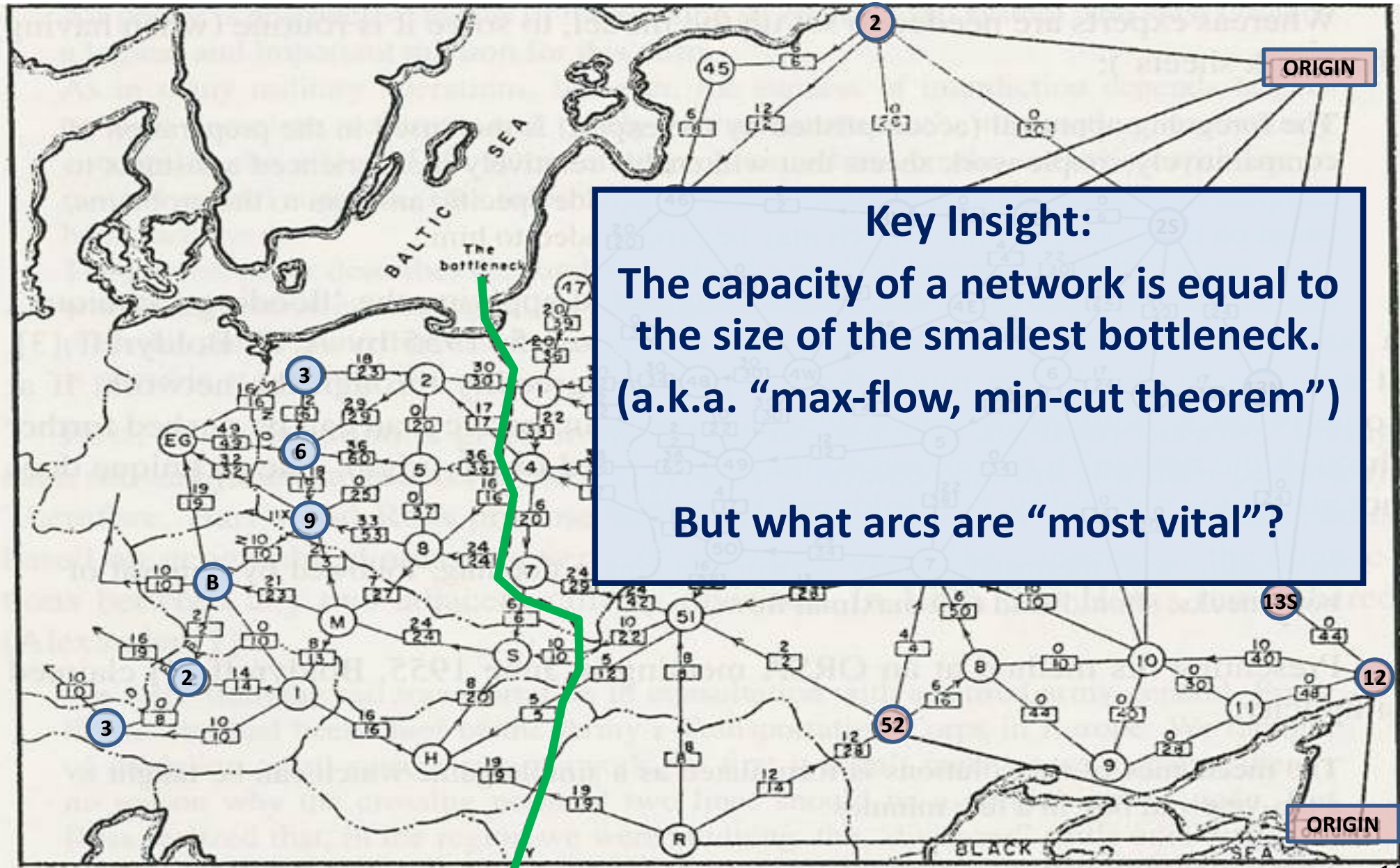


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Finding the “Most Vital” Arc(s) is not trivial!

- It requires you to consider not only the current paths through the network but also any alternate paths
- Because... the system can adjust its flows in response to a disruption!

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Possible “guessing rules” for determining what is most vital
(Ahuja, Magnanti, and Orlin, “Network Flows”, Prentice-Hall, 1993)

- An arc having the *largest capacity*
- An arc carrying the *largest flow in the optimal solution*
- An arc having the *largest capacity in a minimum-capacity cut*
- *Any most-vital arc is in some minimum-capacity cut*

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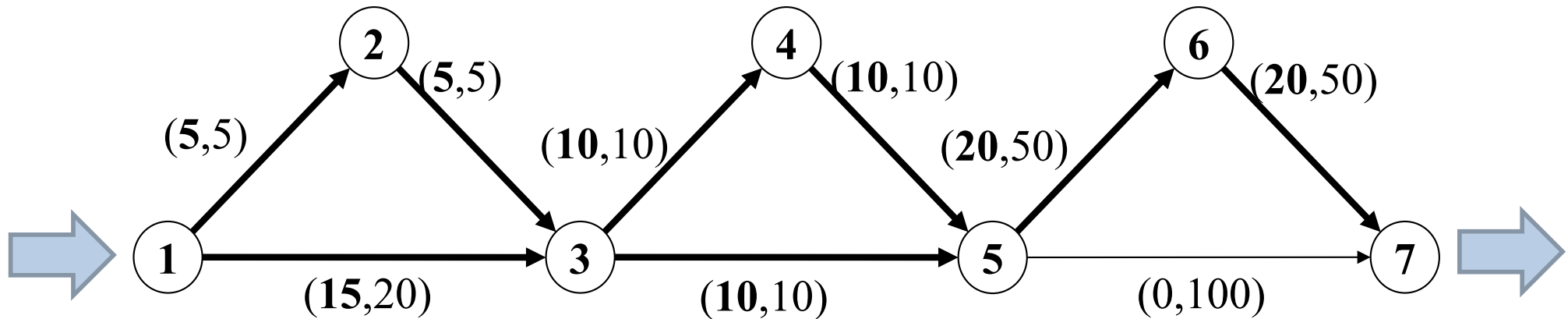
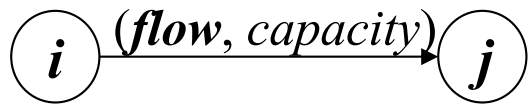
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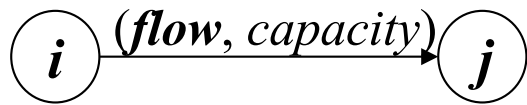
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In general, none of these “guessing rules” work!

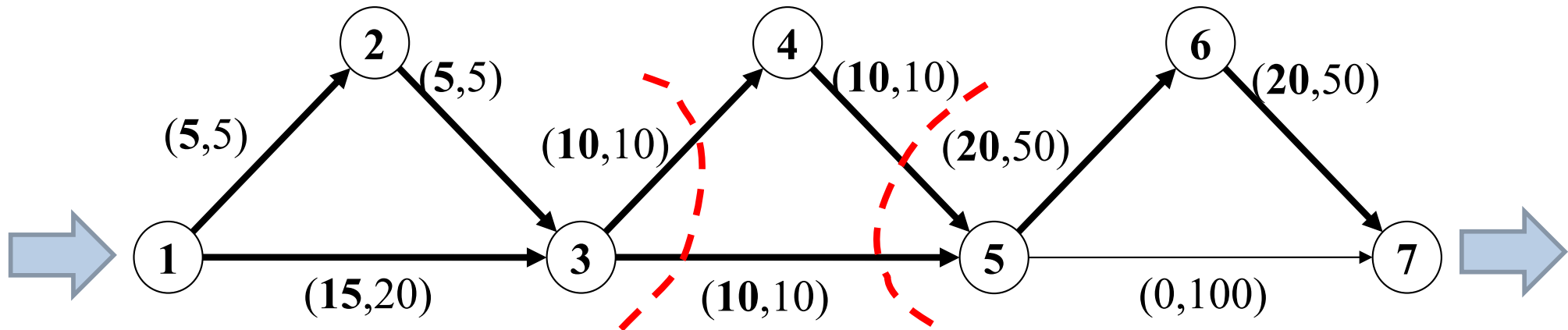
counter-example: guessing to find most vital arc



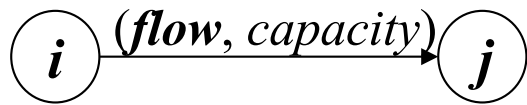
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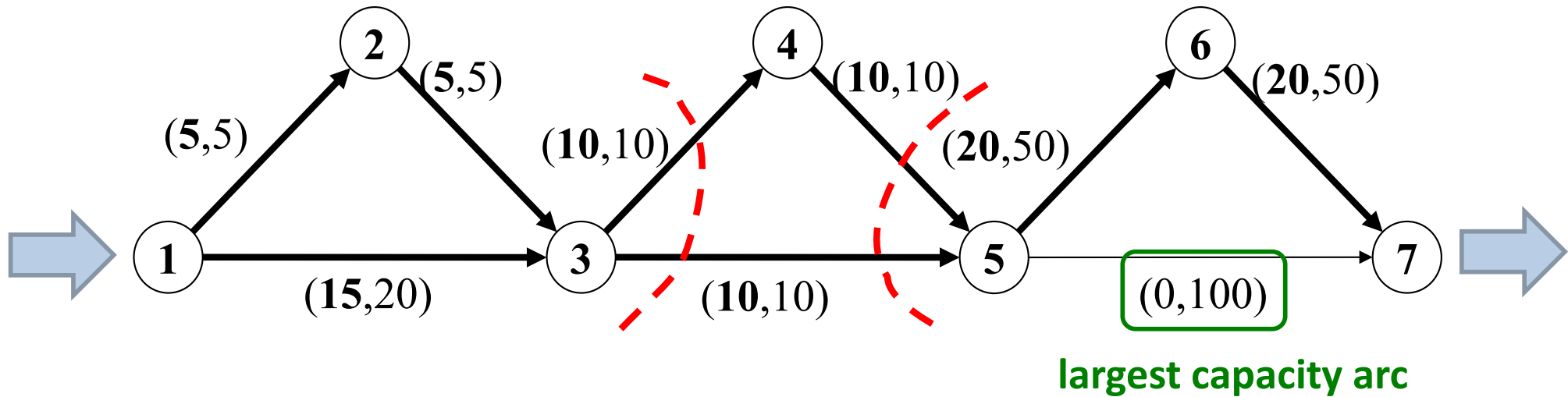
2 minimum capacity cuts !



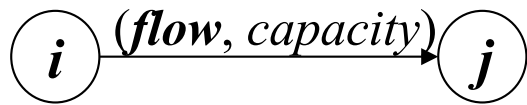
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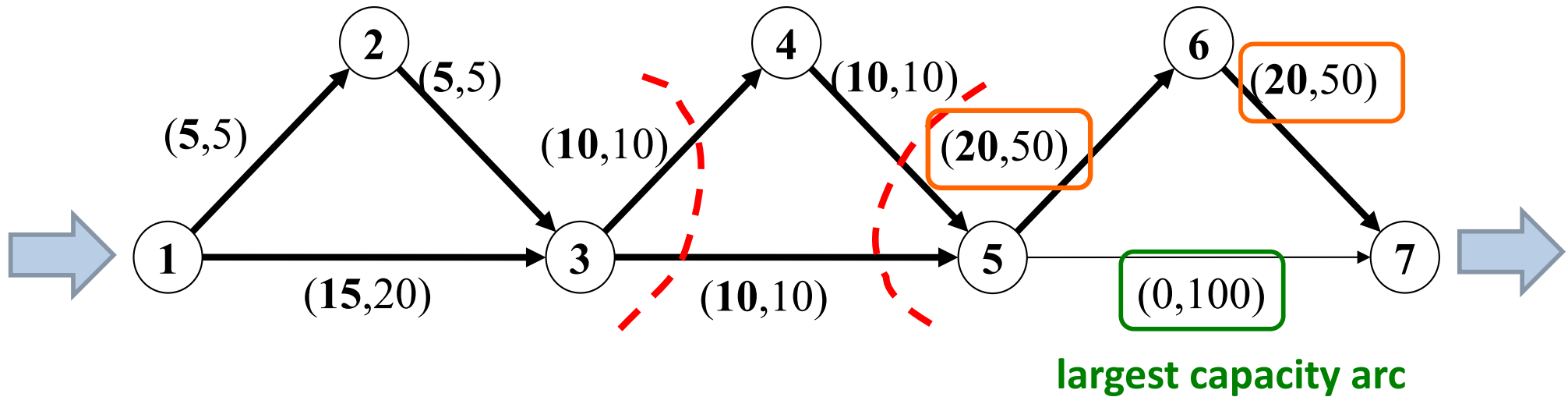


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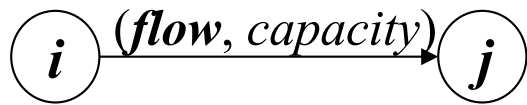


2 minimum capacity cuts !

arcs with largest flow in optimal (maxflow) solution

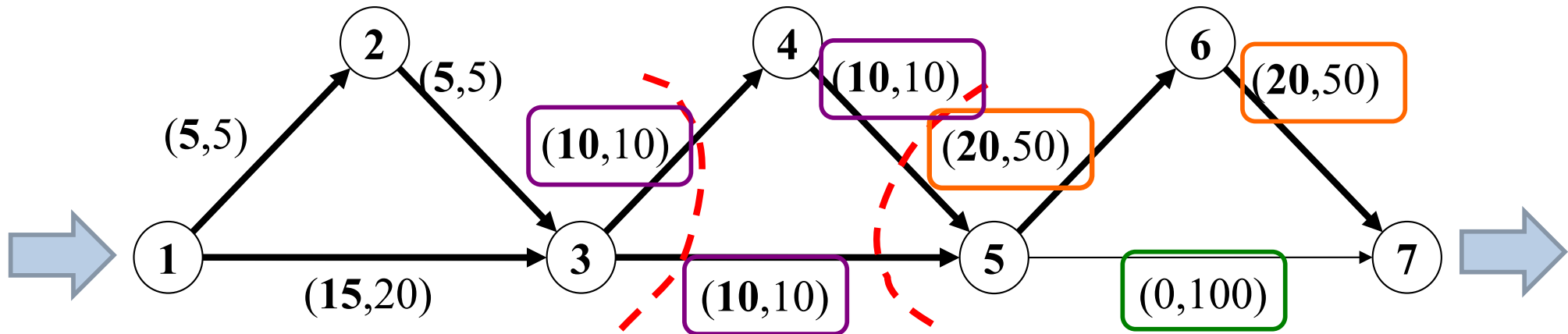


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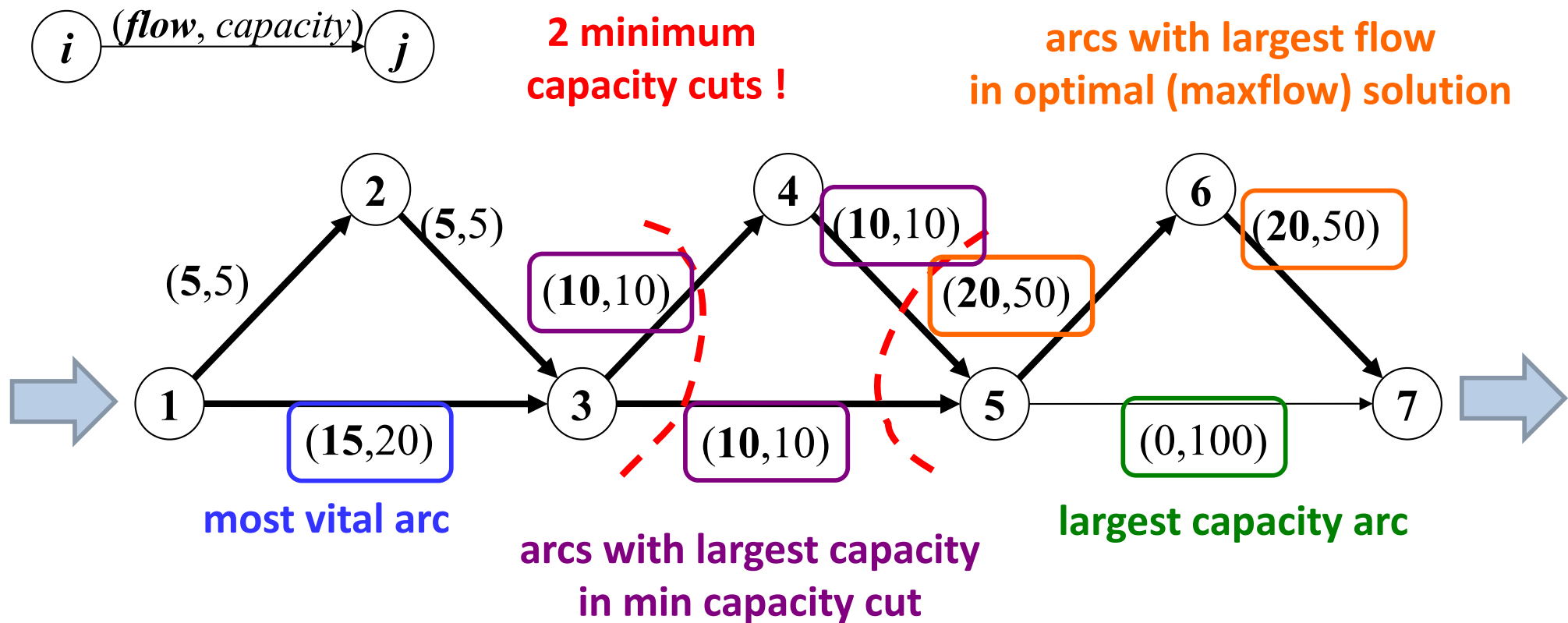
arcs with largest flow in optimal (maxflow) solution



arcs with largest capacity in min capacity cut

largest capacity arc

counter-example: guessing to find most vital arc



In general, you cannot reliably guess. Instead, determining a most vital arc requires solving a *network interdiction problem*.

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We call these Attacker-Defender
and Defender-Attacker-Defender models.

Idea #9: Use an attack-based (adversarial) perspective for planning. (This is also sometimes called “red teaming”.)

- It helps to focus on system operation.
- It helps to discover vulnerabilities.
- It helps to uncover interdependencies.
- It helps to think about mitigation.

Our experience: Large-scale, long-term interruptions in critical infrastructure services can be caused by things much smaller than two Category-5 hurricanes!

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Idea #10: Investing for resilience can work better
when you to think about the system as a whole.

- Hardening (reinforcement)
- Redundancy (backups, spares)
- Capacity expansion
- New infrastructure

This means studying more than just
“how we actually do it now”.

It requires we also consider “how could
we do it now (and in the future)”!

We have used scores of these models to assess resilience for a wide range of systems

Operator Models

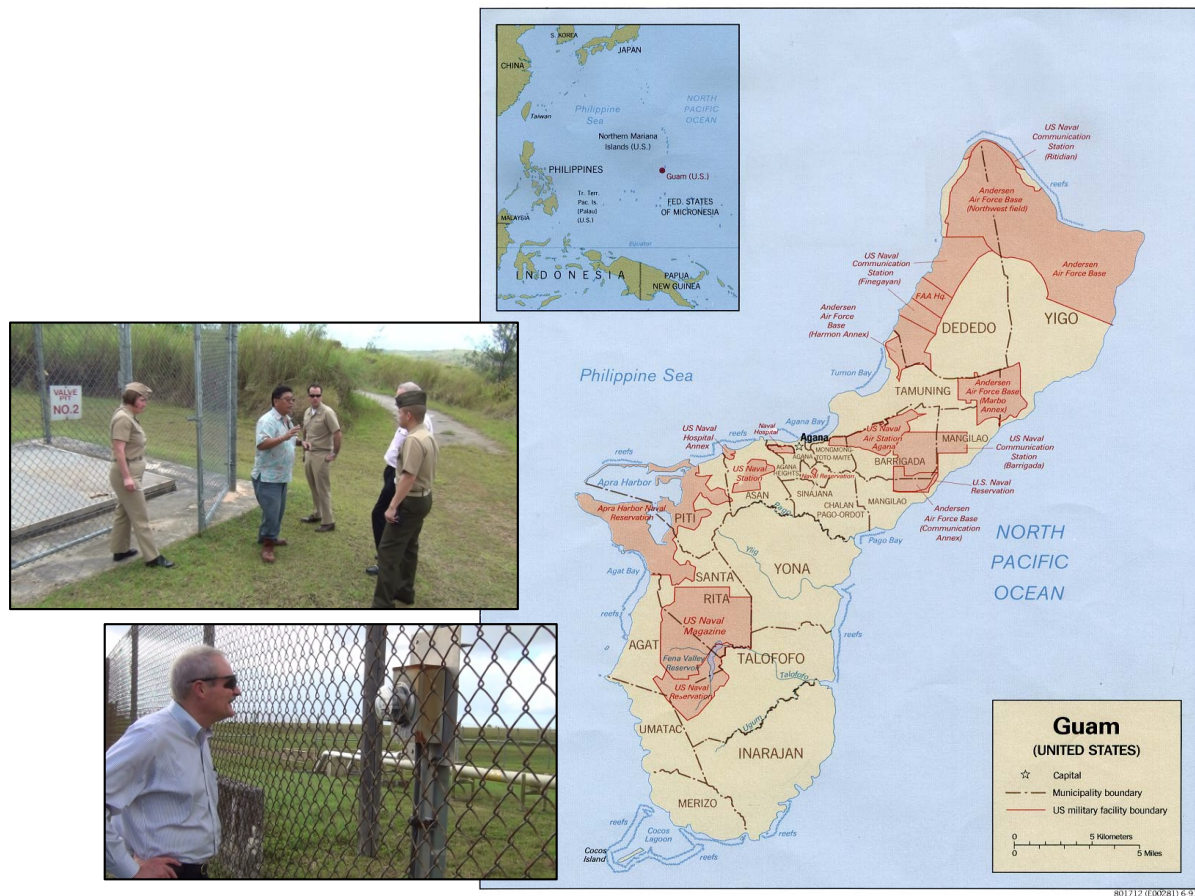
- Shortest-path problems
- Max-flow problems
- Min-cost network flow problems
- Multi-commodity flow problems
- Project scheduling problems
- Linear programs
- Integer-Linear programs
- Nonlinear programs
- Nonlinear-Integer programs

Applications

- Electric power
- Potable water
- Fuel pipelines
- Roadway transportation
- Multi-modal shipping
- Ports
- Supply chains
- Telecommunications
 - Undersea cables
 - Wireless network design
- Interdependent infrastructures

These techniques scale up to realistic size and fidelity, and admit a host of standard models, many already in use by system operators.

Case Study: Guam Power Authority



Guam Power Authority's transmission system (115-13.8 kV):

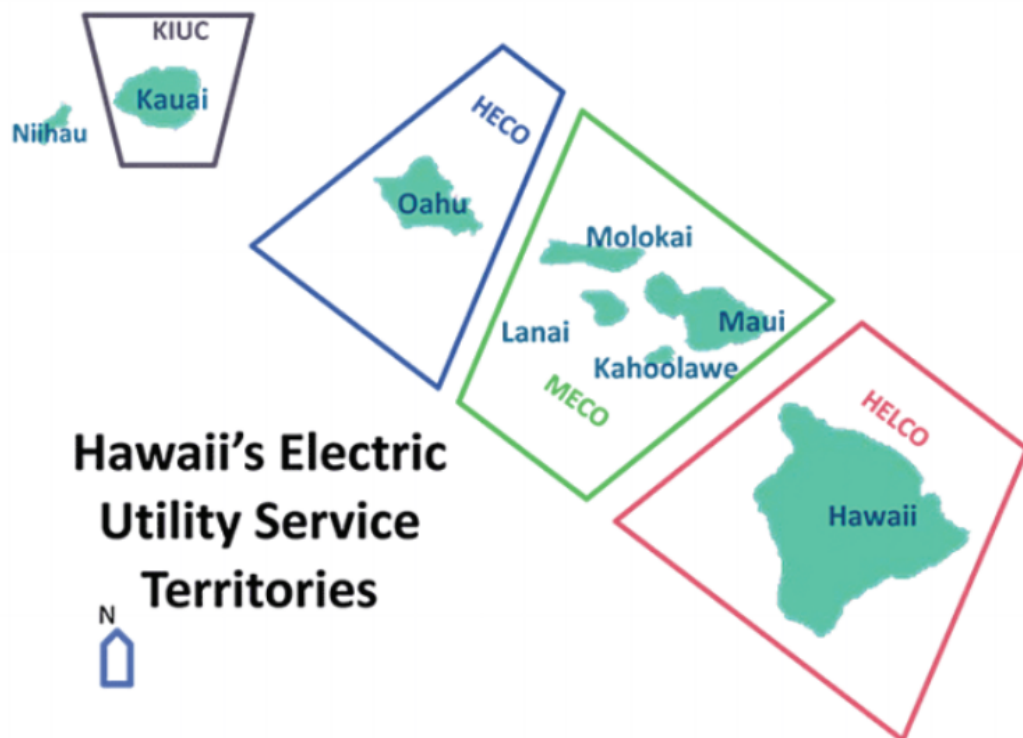
- ~100 buses
- ~50 HV lines
- ~50 transformers
- 10s of substations
- 10s of generating units: >550 MW

Both **Attacker** and **Defender** Analysis

Reference: Salmerón, J., Alderson, D., Brown, G., and Wood, R.K., 2012, **Resilience Report: The Guam Power Authority Electric Power Grid: Analyzing Vulnerability to Physical Attack (U)**, Center for Infrastructure Defense Technical Report NPS-OR-12-002, May. *Distribution authorized to DoD and DoD Contractors only due to infrastructure vulnerability analysis (10 May 2012). Other requests for this document must be referred to President, Code 261, Naval Postgraduate School, Monterey, CA 93943-5000 via the Defense Technical Information Center, 8725 John J. Kingman Rd., STE 0944, Ft. Belvoir, VA 22060-6218.*

Prepared for: Air Force Research Lab (AFRL), Airbase Technologies Division, 139 Barnes Drive, Suite 2, Tyndal Air Force Base, FL 32403-5323.

Case Study: Hawaii



- 10s buses
- ~100 high-voltage AC transmission lines
- no DC lines
- ~100 transformers
- 10s generating units: total gen. capacity of ~2,500 MW
- Total load: ~1,200 MW

Attacker, Defender, & Spare Parts Analysis

Map credit: [“Hawai’i Energy Facts and Figures: May 2015,” Hawai’i State Energy Office](#)

- Can a small number of coordinated attacks inflict significant damage for which repair would require considerable reconstitution time? What is the best means of hardening against such attacks?
- How can a limited stockpile of medium- and high-voltage spare transformers contribute most to mitigating vulnerability, i.e., to “increasing system resilience.”

Reference: Salmerón, J., Alderson, D., and Brown, G., 2018, **Resilience Report: Analysis of Hawaiian Electric Power Grid to Physical Attack (U)**, NPS Technical Report NPS-OR-18-001R, February. Restricted distribution (PCII).



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Goals For This Session

- 10 key ideas for how to assess and improve operational resilience of critical infrastructures
- **Ongoing work in applying these ideas to the USVI**

Our research is part of a broader team effort



FEMA



Our work in the USVI: several related research efforts

Effort 1 - Modeling and analysis of interdependent critical infrastructure systems

- Energy (emphasis on electric power)
- Water (emphasis on potable storage and distribution)
- Transportation
- Telecommunications

Effort 2 - Support for development of a new Hazard Mitigation and Resilience Plan

- in partnership with UVI / VITEMA

Effort 3 - Capacity building & workforce development program

- in partnership with UVI

Our work in the USVI: several related research efforts

| | |
|-------------|---|
| 27 Feb 2018 | Project Start (funds available) |
| 21 Mar | remote participation in USVI Energy Roundtable |
| 26-30 Mar | 1 st NPS site visit to STX, STT |
| 11-15 Jun | 2 nd NPS site visit to STX, STT |
| 14-15 Jun | UVI/VITEMA Hazard Mitigation Workshop |
| 21 Sep | MS Thesis by LCDR Brendan Bunn |
| 20 Oct | Technical report (final draft) |
| 22-26 Oct | 3 rd NPS site visit to STX, STJ, STT |

- Bunn BB, 2018, **“An Operational Model of Interdependent Water and Power Distribution Infrastructure Systems,”** M.S. Thesis in Operations Research, Naval Postgraduate School, Monterey, CA, September 2018.
- Alderson DL, Bunn BB, Eisenberg DA, Howard AH, Nussbaum DE, Templeton JC, **“Interdependent Infrastructure Resilience in the U.S. Virgin Islands: Preliminary Assessment,”** NPS Technical Report, Naval Postgraduate School, Monterey, CA, October 2018 (forthcoming).

Lots of proposed changes!

Open Questions:

- How to assess the impact of these changes (good/bad)?
- How to prioritize?

228 proposed initiatives across a variety of sectors:

- Climate Analysis (5)
- Energy (17)
- Private Sector Comms (14)
- Public Sector Comms (11)
- Transportation (24)
- Water (11)
- SolidWaste and Wastewater (26)
- Housing and Buildings (11)
- Health (21)
- Vulnerable Populations (12)
- Education (20)
- Economy (9)
- Non-profit, Philanthropy, and Voluntary Organizations (6)
- Government Response (41)

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Alderson DL, Bunn BB, Eisenberg DA, Howard AH, Nussbaum DE, Templeton JC, **“Interdependent Infrastructure Resilience in the U.S. Virgin Islands: Preliminary Assessment,”** NPS Technical Report, Naval Postgraduate School, Monterey, CA, October 2018 (forthcoming).

Key Concept: The Need for an Operational View of Resilience

Report Contributions:

1. Explaining the structure, function, and tensions associated with critical infrastructure that were chronic problems prior to the hurricanes.
2. Documenting hurricane response, recovery, and mitigation activities for these infrastructure systems after the hurricanes.
3. Discussing these changes in the context of potential barriers to resilience.

We face several barriers to resilience

Barrier 1: We don't fully understand how vulnerable we are.

- owners, operators, or communities who manage infrastructure often do not have complete knowledge about their vulnerabilities

Barrier 2: We don't know how best to create resilience.

- Tradeoffs/tensions between different mechanisms to achieve resilience
- Prioritization is difficult

Barrier 3: We don't have incentives to create resilience.

- Hard to invest in mitigating something that has never happened
- Moral hazard: disincentives for investment

Barrier 4: We don't know how to govern for resilience.

- Rules/regulations work against implementation of desired changes
- mismatch between infrastructure governance and infrastructure operation

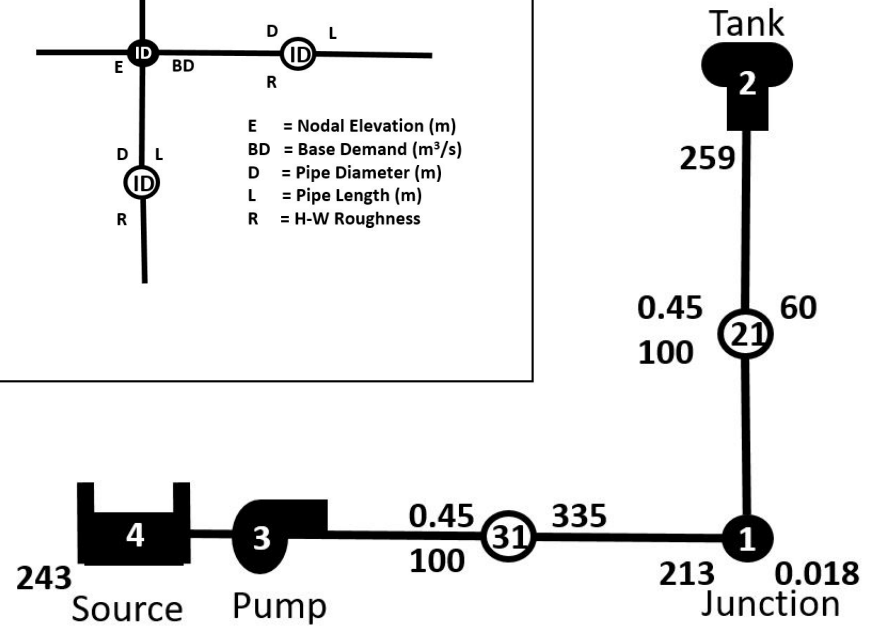
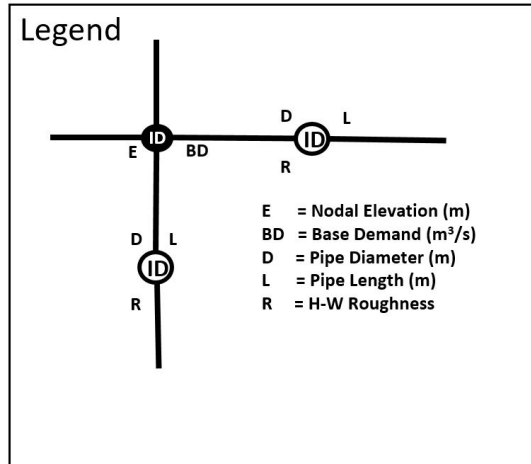
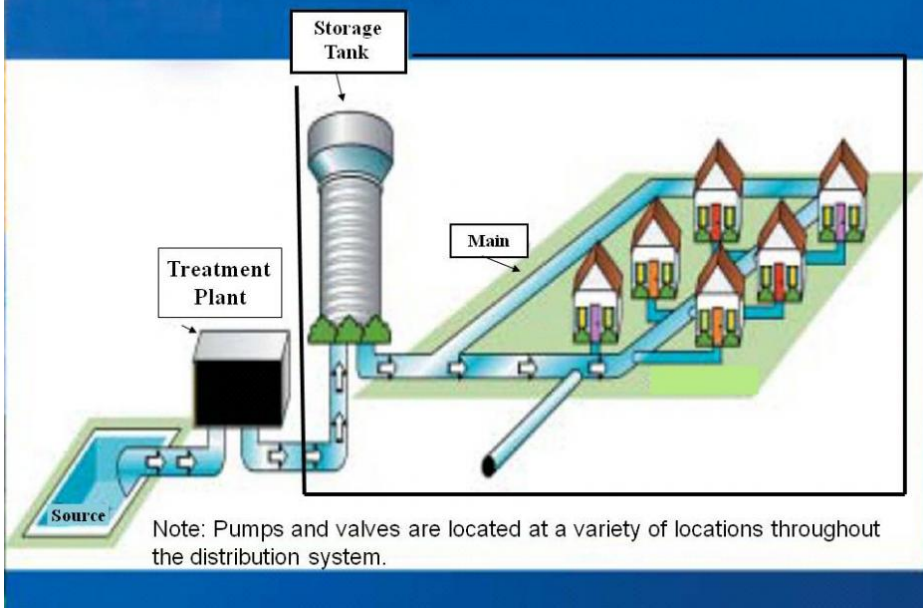
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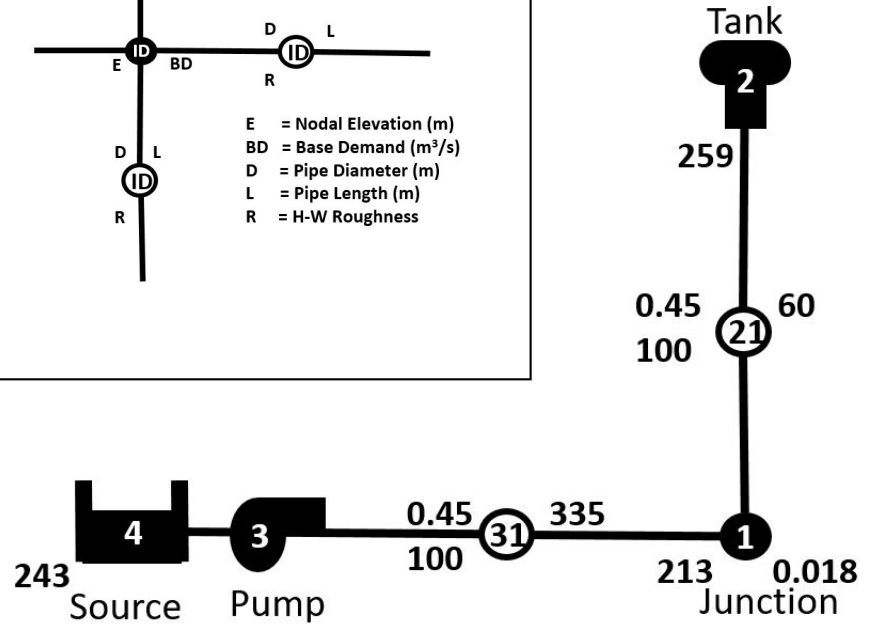
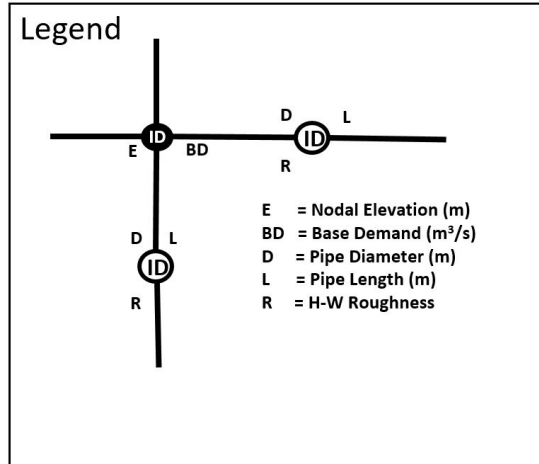
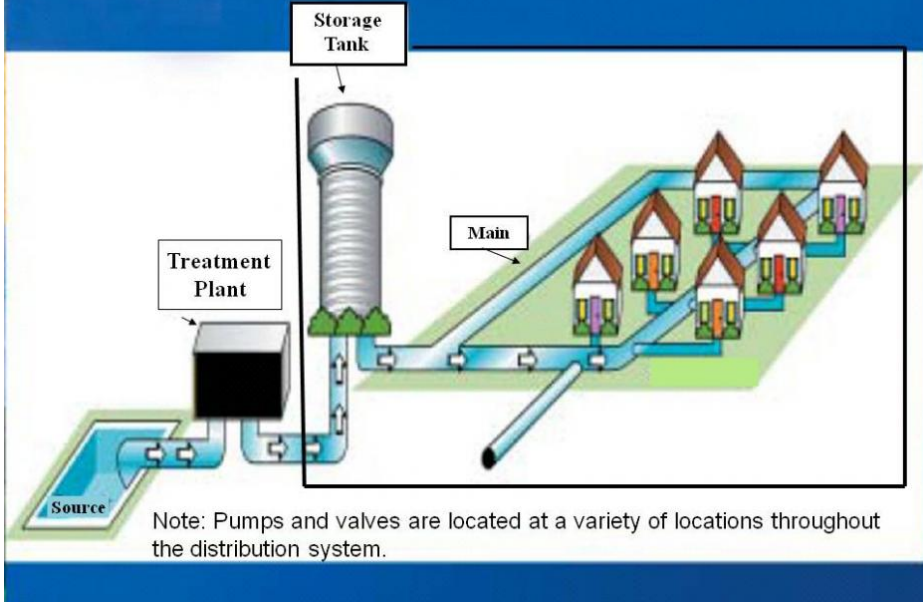
Effort 1 - Modeling and analysis of interdependent critical infrastructure systems

- Energy (emphasis on electric power)
- Water (emphasis on potable storage and distribution)
- Transportation
- Telecommunications

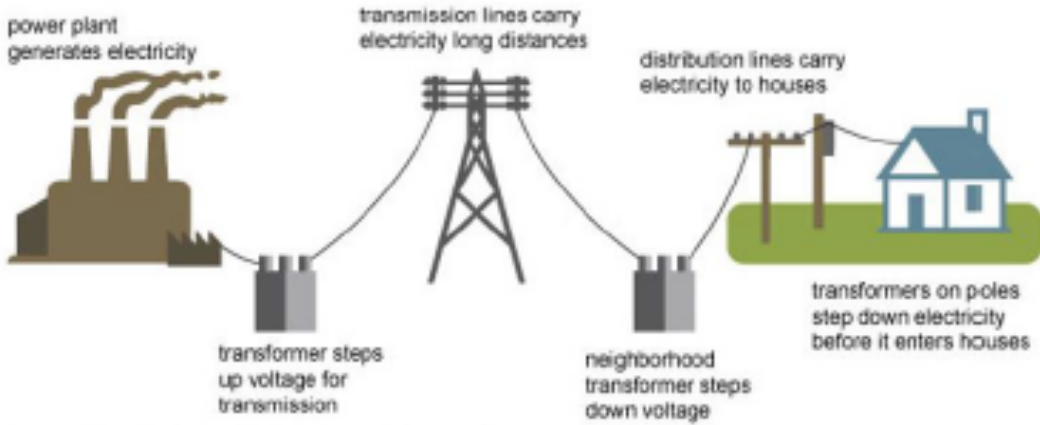
Water Supply Distribution System



Water Supply Distribution System

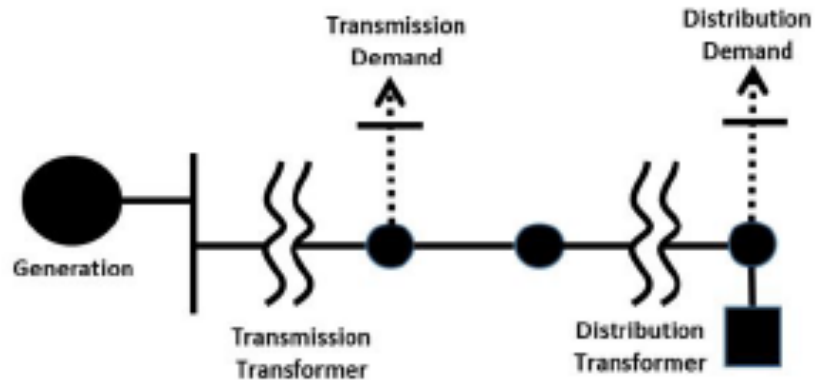


Electricity generation, transmission, and distribution



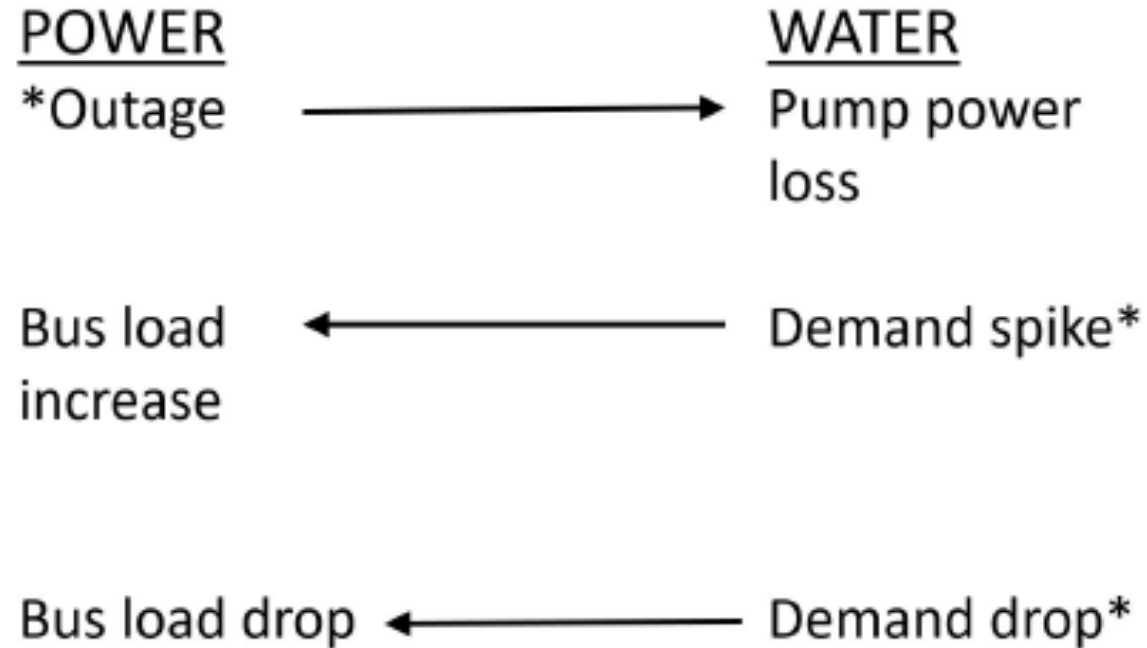
Source: Adapted from National Energy Education Development Project (public domain)

(a)



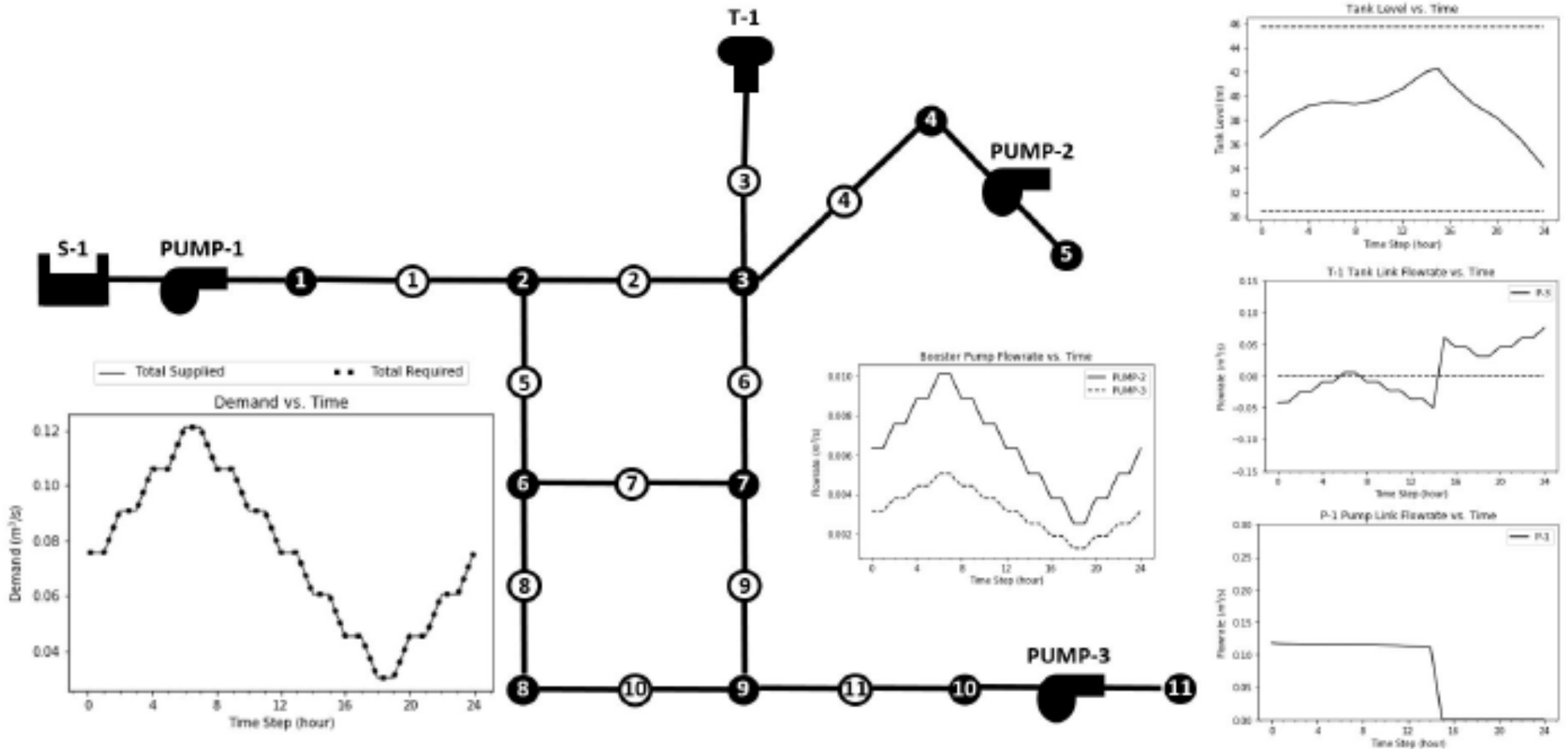
(b)

Power – Water Interdependencies

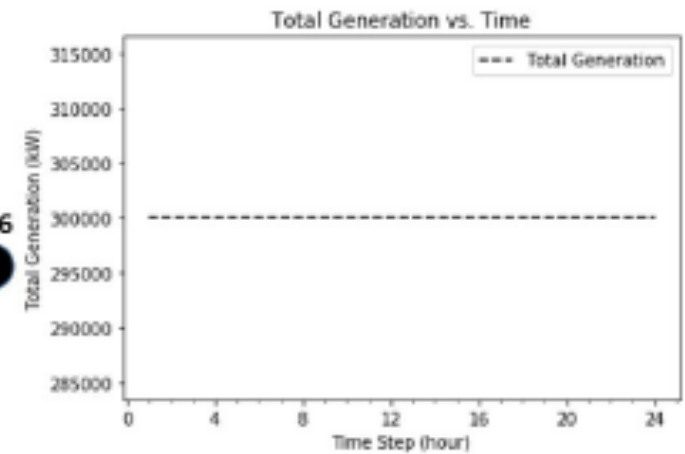
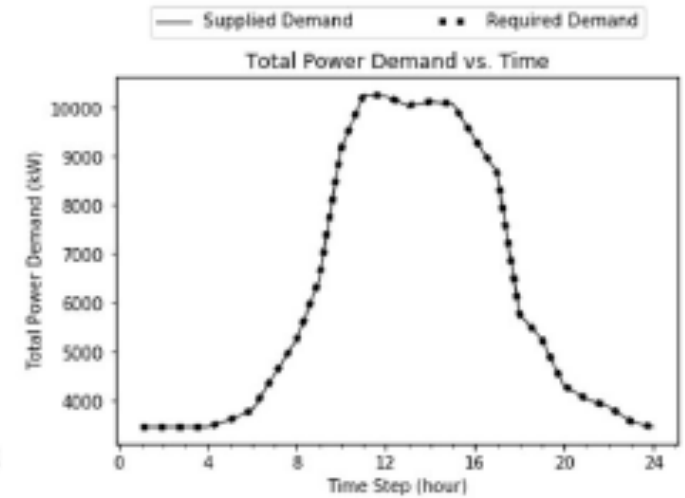
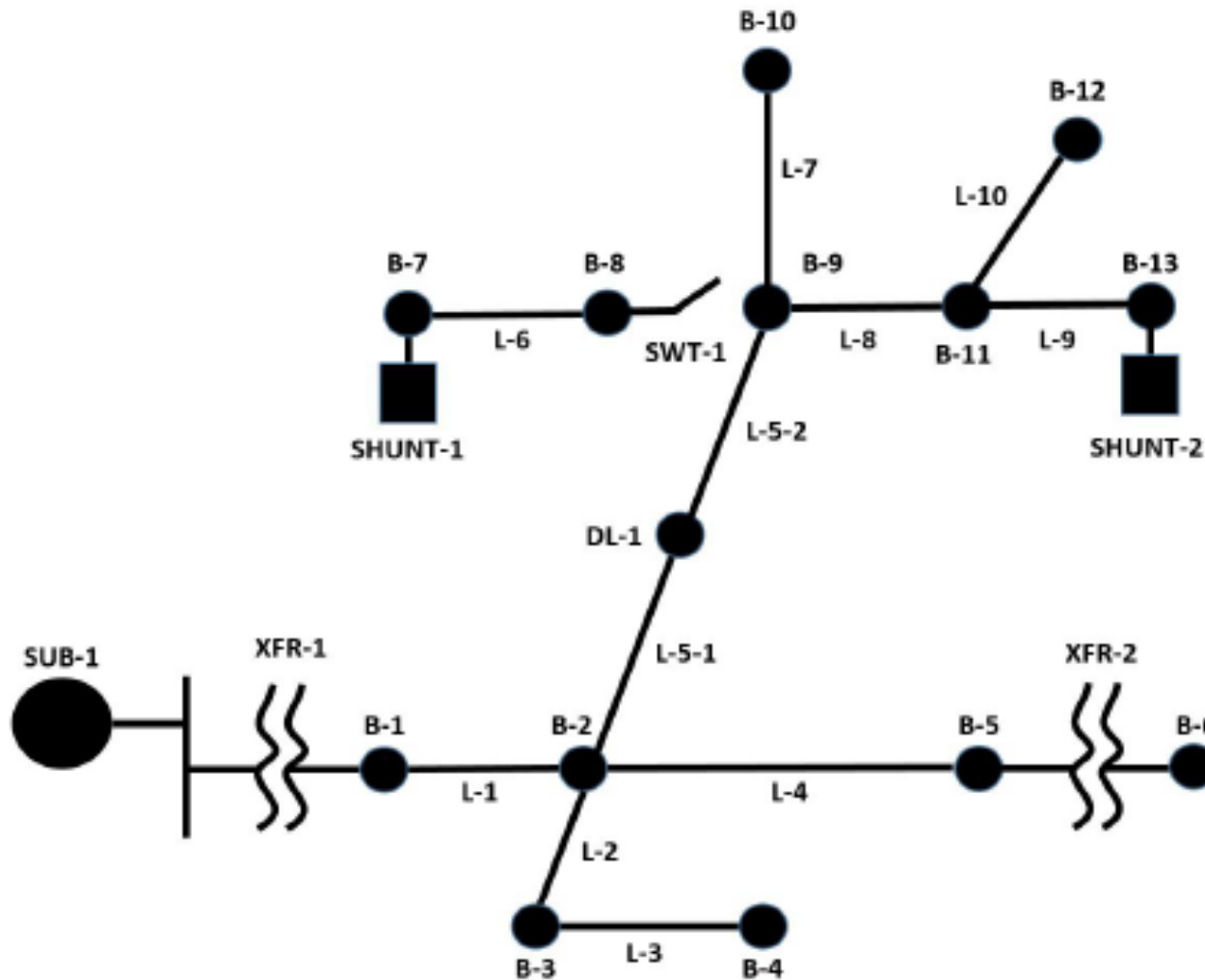


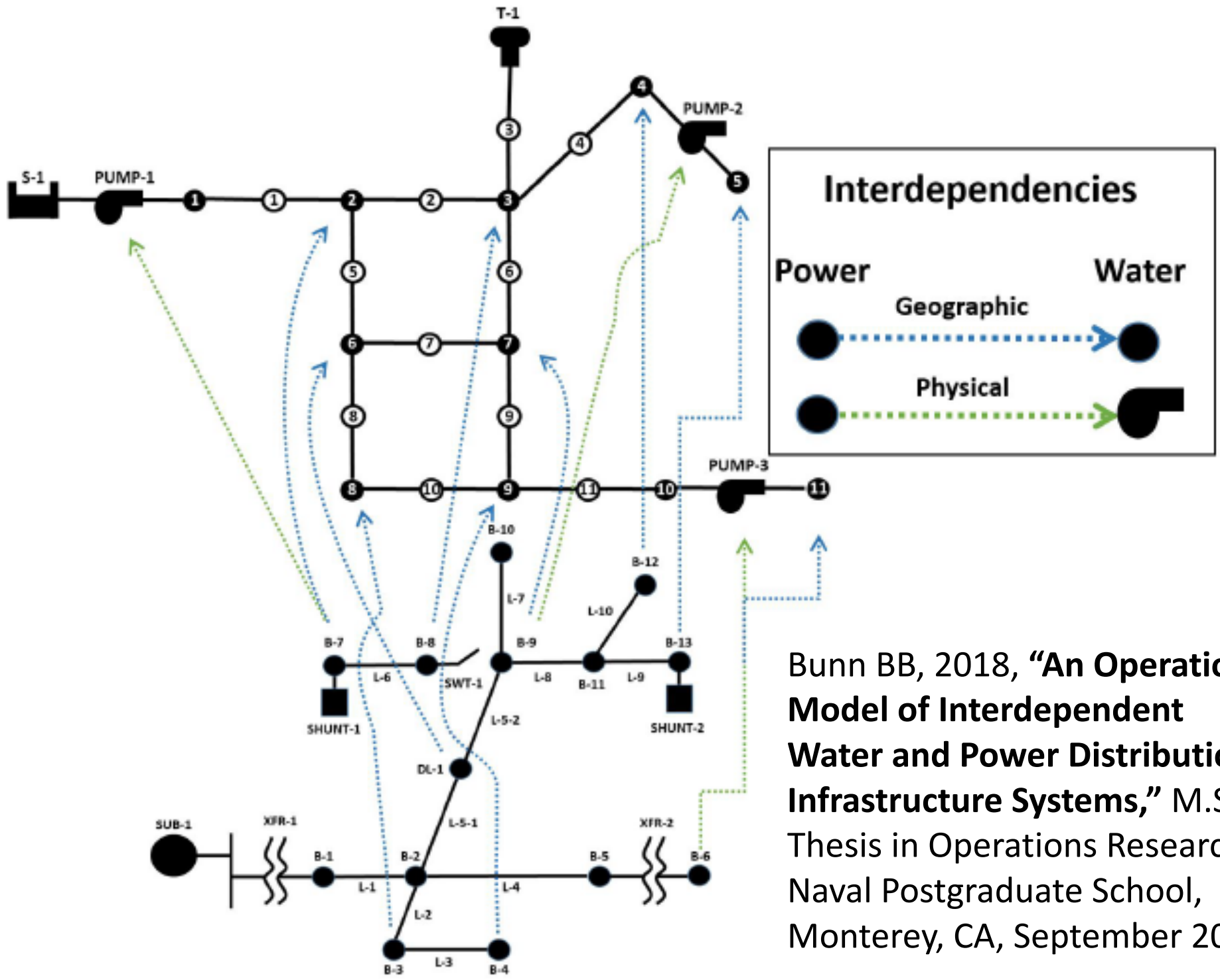
Excursions are denoted by originating failure events (asterisk) and their consequences across system boundaries.

a more realistic (USVI) water distribution system



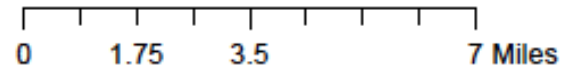
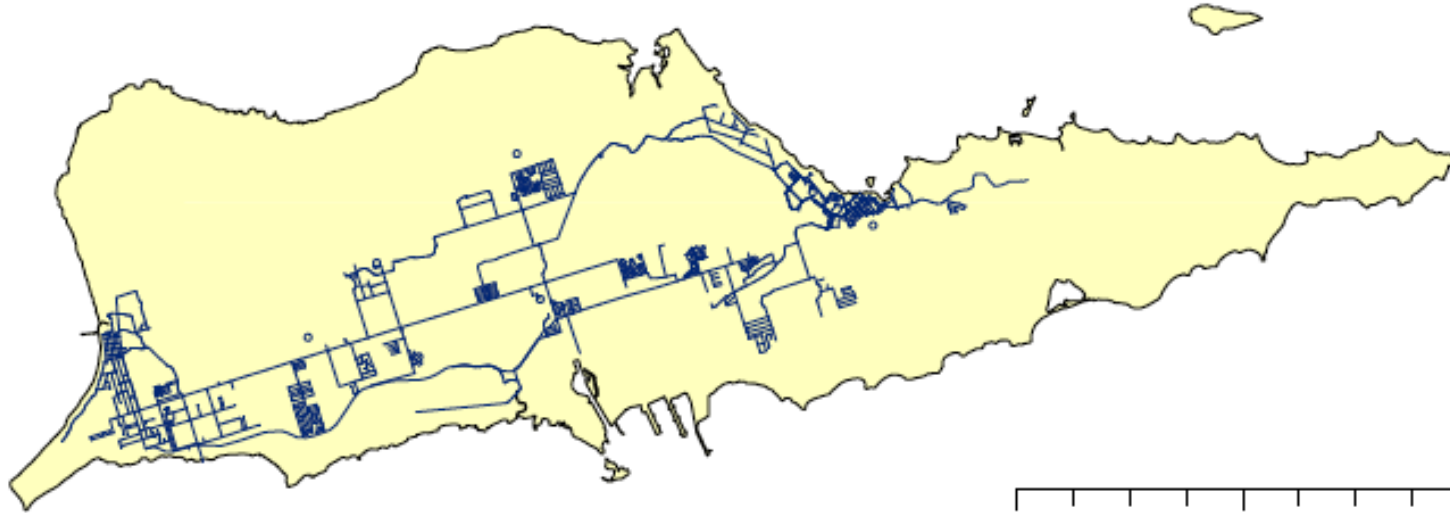
IEEE 13-bus electricity distribution network



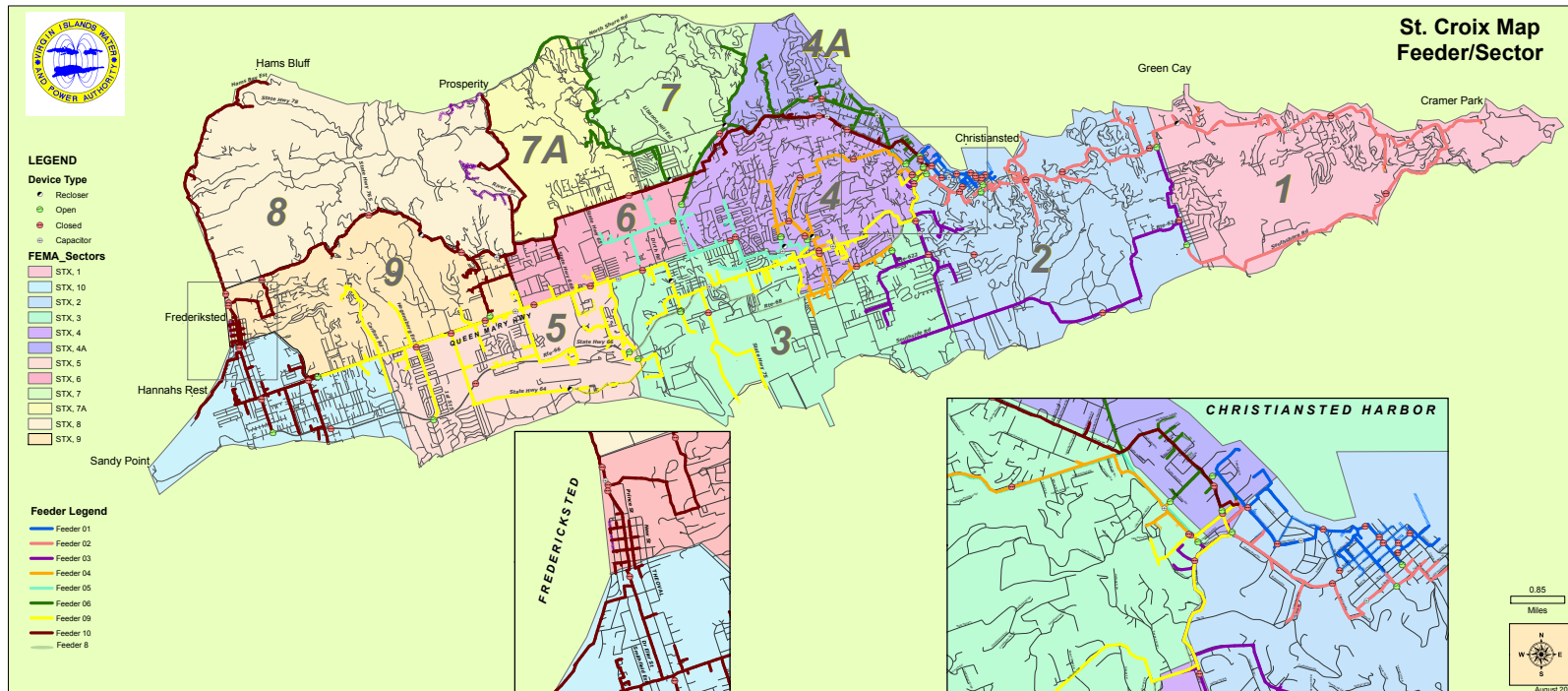


Bunn BB, 2018, "An Operational Model of Interdependent Water and Power Distribution Infrastructure Systems," M.S. Thesis in Operations Research, Naval Postgraduate School, Monterey, CA, September 2018.

Ongoing work: St. Croix electric + water



St. Croix



Our work in the USVI: several related research efforts

Effort 1 - Modeling and analysis of interdependent critical infrastructure systems

- Energy (emphasis on electric power)
- Water (emphasis on potable storage and distribution)
- Transportation
- Telecommunications

Effort 2 - Support for development of a new Hazard Mitigation and Resilience Plan

- in partnership with UVI / VITEMA

Effort 3 - Capacity building & workforce development program

- in partnership with UVI

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<http://www.nps.edu/cid>

References and Acknowledgments

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